

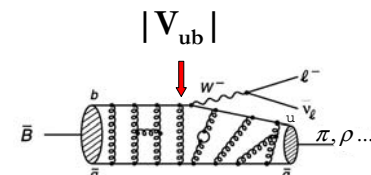
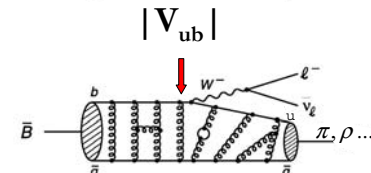
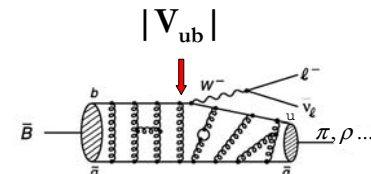
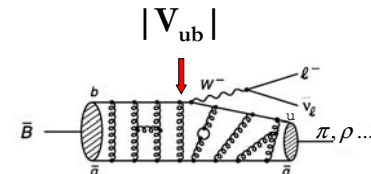
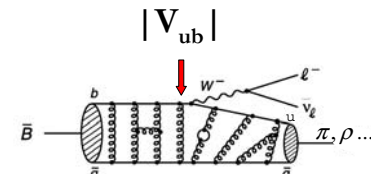
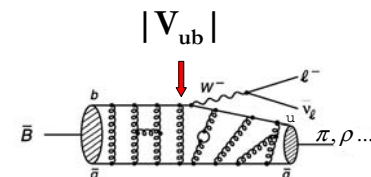
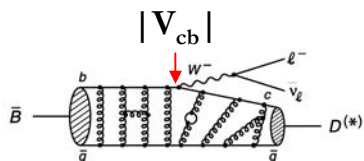
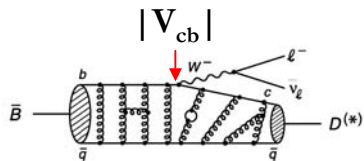
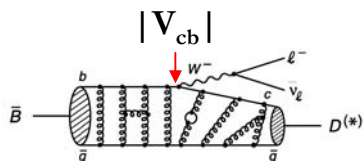
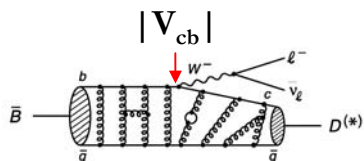
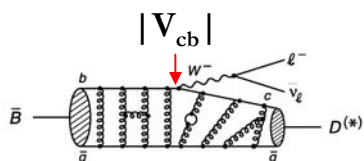
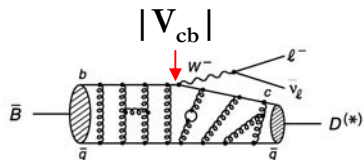
# Measurement of $|V_{cb}|$ and $|V_{ub}|$ at



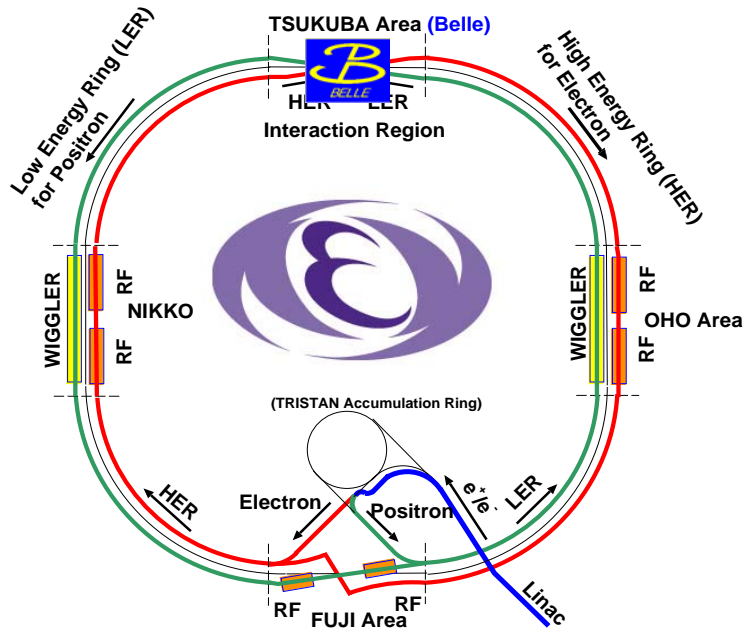
Weak Interactions and Neutrinos 2003

October 7

I. Bizjak, J. Stefan Institute  
for Belle collaboration



# Belle detector @ KEK-B



## Beam energies:

$e^+$  (HER): 8.0 GeV

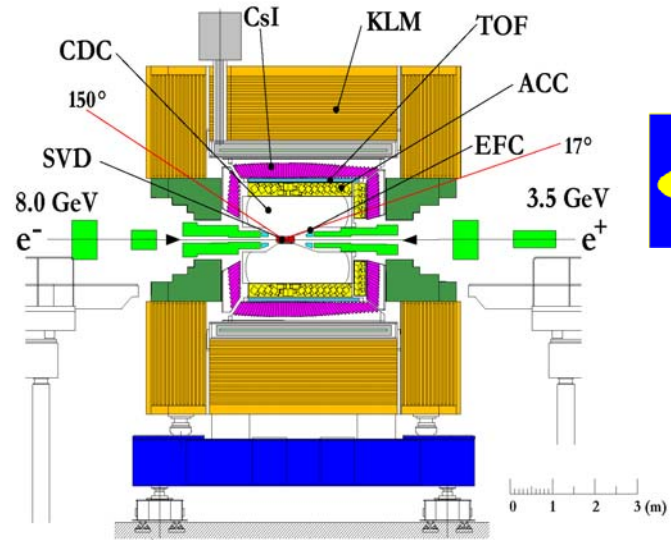
$e^-$  (LER): 3.5 GeV

$E_{CM} = 10.58$  GeV

## 4 years of data taking:

$L_{max} = 10.6 \cdot 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

$L_{int} = 158.7 \text{ fb}^{-1} \dots$  **152 million B meson events**



SVD: Silicon Vertex Detector  
 CDC: Central Drift Chamber  
 CsI: CsI Calorimeter  
 KLM:  $K_p$  and muon detector

TOF: Time of Flight Counter  
 ACC: Aerogel Cherenkov Counter  
 EFC: E-M Forward Calorimeter



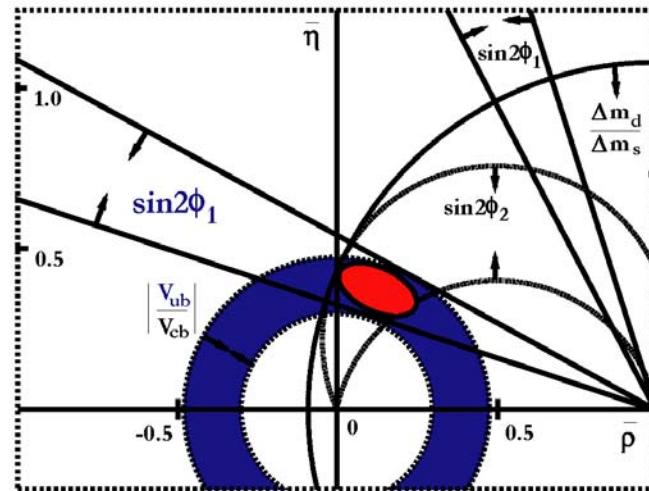
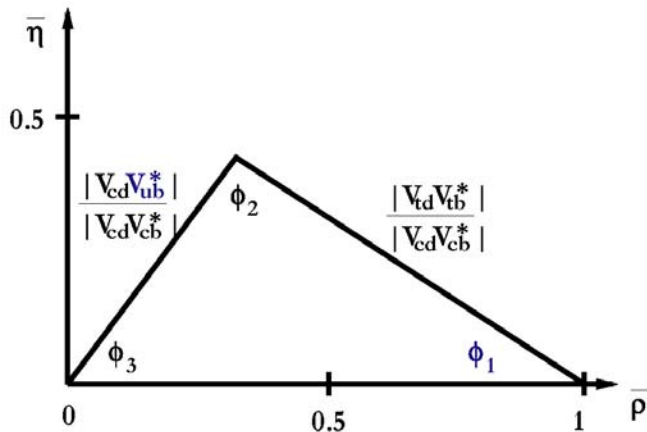
# Measurement of $|V_{cb}|$ and $|V_{ub}|$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

B physics can determine 2/3 real par.

+  
complex phase

$$V = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



# Exclusive $|V_{ub}|$ : evidence for $B^+ \rightarrow \omega l^+ \nu$

Previous exclusive results:

$$\text{Br}(B^0 \rightarrow \pi^- l^+ \nu) = (1.33 \pm 0.11 \pm 0.21) \cdot 10^{-4} \quad (60 \text{ fb}^{-1})$$

$$\text{Br}(B^+ \rightarrow \rho^0 l^+ \nu) = (1.44 \pm 0.18 \pm 0.23) \cdot 10^{-4} \quad (29 \text{ fb}^{-1})$$

## $B^+ \rightarrow \omega l^+ \nu$

Preliminary

- Events with **single lepton (e or  $\mu$ )**

$l^+$

- Reconstructed** neutrino momentum from missing momentum

$${}^3p_{\text{miss}} = {}^3Y(4S) - \sum {}^3p \quad {}^4p_{\text{miss}} = (|p_{\text{miss}}|, {}^3p_{\text{miss}})$$

$$\sigma(p_{\text{miss}}) \approx 140 \text{ MeV}/c$$

$\nu$

$\omega$  decay reconstruction:  $\omega \rightarrow \pi^+ \pi^- \pi^0$

Fully reconstruct the final state

$\omega$

Simultaneous fit of the signal

$m(\pi^+ \pi^- \pi^0), \Delta E, p_1$

in three lepton momentum bins

$p_l$	1.8 – 2.1 GeV/c	2.1 – 2.4 GeV/c	2.4 – 2.7 GeV/c
data	1990	667	75
$B^+ \rightarrow \omega l^+ \nu$	$41 \pm 13$	$68 \pm 21$	$35 \pm 11$
$B \rightarrow X_u l \nu$	$61 \pm 28$	$82 \pm 28$	$21 \pm 5$
$B \rightarrow X_c l \nu$	$1743 \pm 36$	$415 \pm 14$	0
fake, non $B$	$19 \pm 3$	$33 \pm 4$	$3 \pm 1$
continuum	$17 \pm 12$	$61 \pm 23$	$9 \pm 9$
sum	$1881 \pm 49$	$659 \pm 44$	$68 \pm 15$

# Exclusive $|V_{ub}|$ : evidence for $B^+ \rightarrow \omega l^+ \nu$ ( $78 \text{ fb}^{-1}$ )

Simultaneous fit of the signal  
 $m(\pi^+ \pi^- \pi^0), \Delta E, p_1^*$   
 in three lepton momentum bins

form-factor	signal yield	$\mathcal{B}(B^+ \rightarrow \omega l^+ \nu)$
ISGW2	$144 \pm 44$	$(1.00 \pm 0.31) \cdot 10^{-4}$
UKQCD	$145 \pm 44$	$(1.20 \pm 0.37) \cdot 10^{-4}$
LCSR	$176 \pm 52$	$(1.67 \pm 0.50) \cdot 10^{-4}$
average	$155 \pm 47 \pm 15$	$(1.29 \pm 0.39 \pm 0.28) \cdot 10^{-4}$

Preliminary

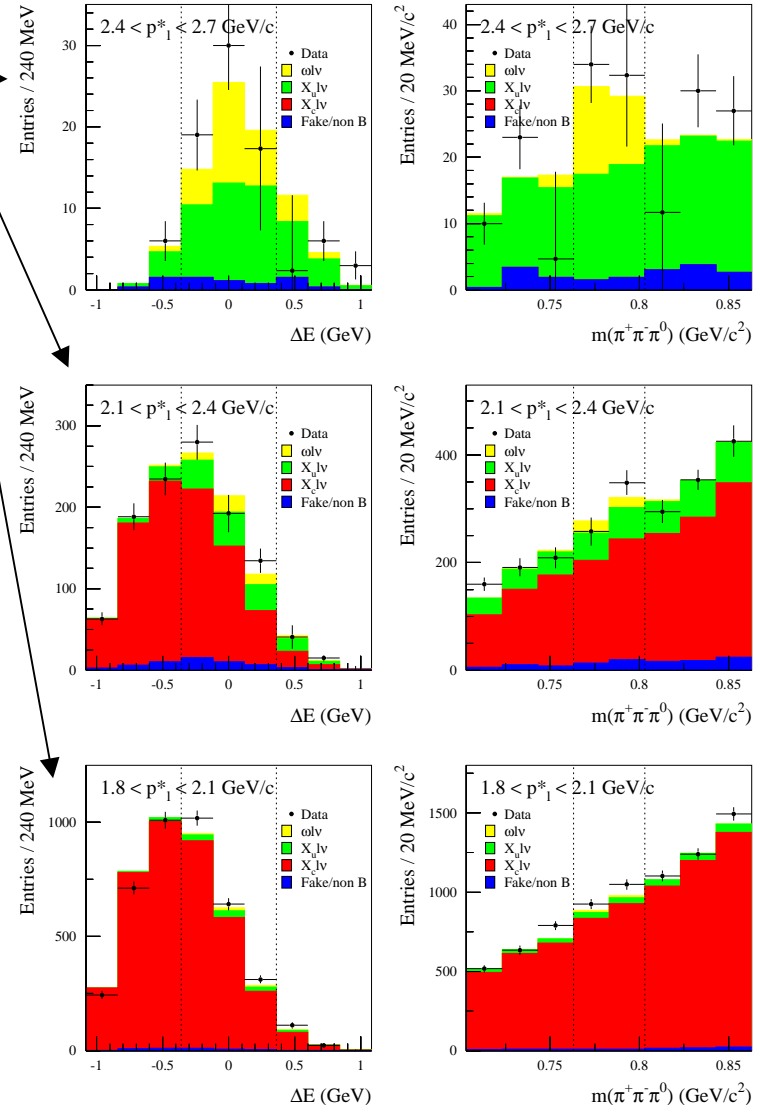
stat. sys. model

$$\text{Br}(B^+ \rightarrow \omega l^+ \nu) = (1.3 \pm 0.4 \pm 0.2 \pm 0.3) \cdot 10^{-4}$$

## Dominant systematic uncertainty:

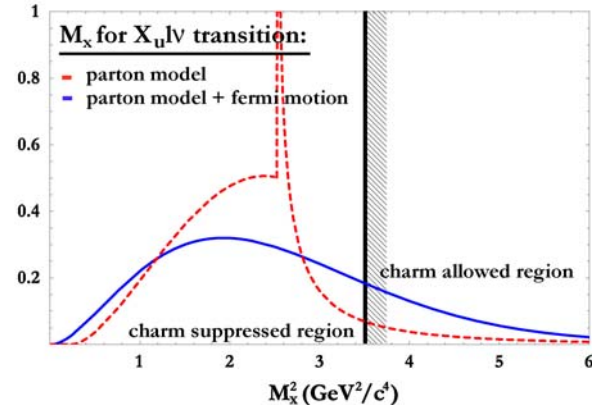
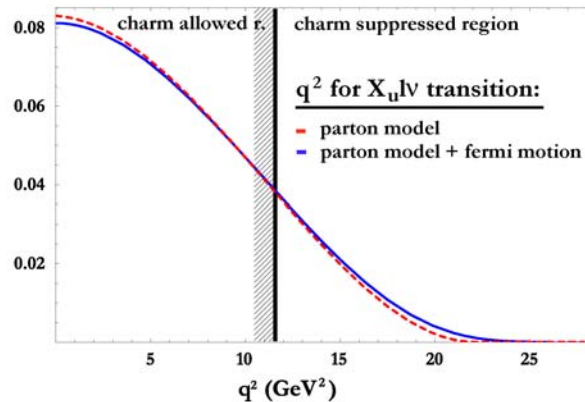
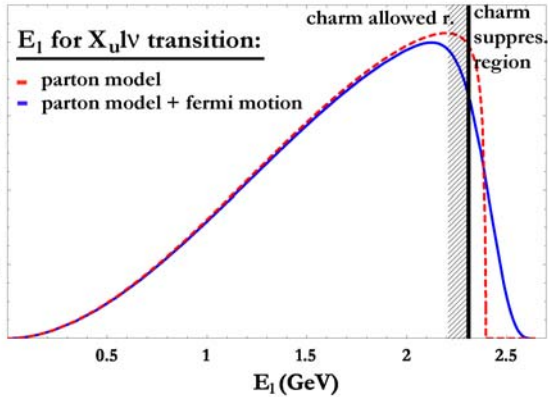
- $B \rightarrow X_u l \nu$  crossfeed ... 14%
- Neutrino reconstruct., track&cluster finding ... 9%

BELLE

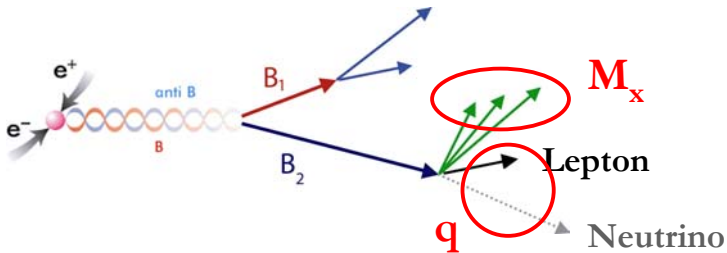


# Inclusive $|V_{ub}|$ : the variables

How to suppress  $B \rightarrow X_c l \nu$ , which is approx. 60 times more abundant than  $B \rightarrow X_u l \nu$ ?



C.W.Bauer, Z. Ligeti, M. Luke: PLB 479,395 (2000)



Part of phase space, where  $b \rightarrow c$  is kinematically suppressed

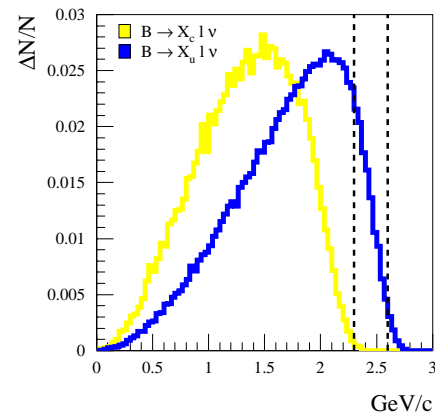
What part of  $b \rightarrow u$  in this phase space

▶ Hadronic invariant mass $M_x$	→	$M_x < M_D$	→	80%
▶ $l^\pm \nu$ invariant mass $q^2$	→	$q^2 > (m_B - m_D)^2$	→	20%
▶ Lepton energy $E_l$	→	$E_l > \frac{(m_B^2 - m_D^2)}{2m_B}$	→	10%

# Electron spectrum endpoint: the method

✓ Using endpoint of momentum spectrum for  $e^\pm$

- Measurement region:  $2.3 \text{ GeV}/c < p_e < 2.6 \text{ GeV}/c$  (CMS)
- Backg. estim. region:  $1.5 \text{ GeV}/c < p_e < 2.2 \text{ GeV}/c$  (CMS)



Deal with large backgrounds:

Non BB backgrounds

- Continuum ( $e^+e^- \rightarrow qq$ )
- QED processes

Fox-Wolfram moments  
 Fisher discriminant:  
 Thrust axis  
 Visible energy  
 Charged multiplicity

+

Subtraction of continuum  
 ( $8.8\text{fb}^{-1}$  of offresonance data)

BB backgrounds

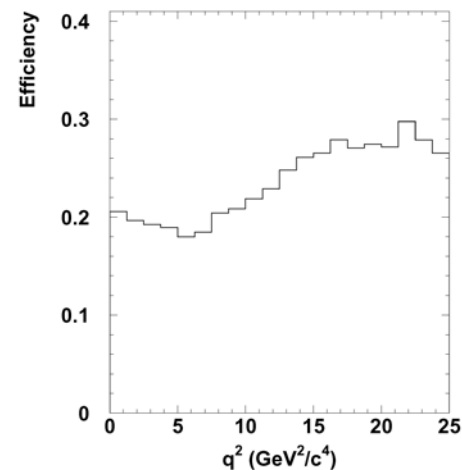
- $B \rightarrow X_c lv$
- Leptons from other decays  
 ( $J/\psi, \gamma$  conv.)
- Fake electrons

MC simulation:  
 $D^{**}ev$  (ISGW2)  
 $D^*ev$  (HQET)  
 $Dev$  (ISGW2)  
 $D^{(*)}\pi$  (Goity-Roberts)

Veto on inv. mass

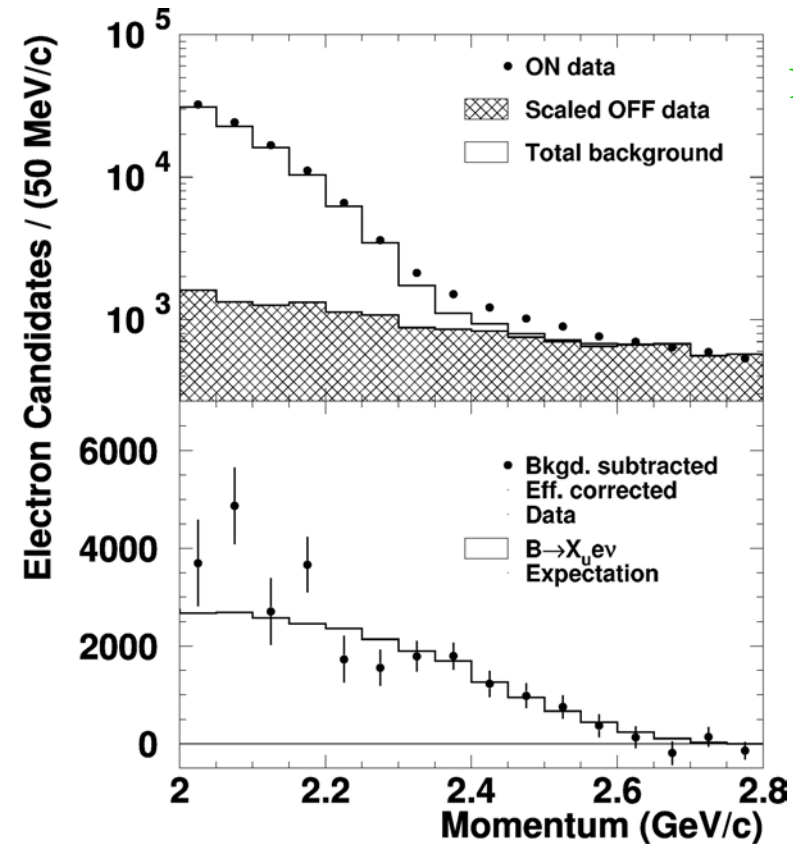
Estimated using  $K_s \rightarrow \pi^+ \pi^-$

Acceptance of selection requirements as a funct. of  $q^2$





# Electron spectrum endpoint: the result ( 27 fb<sup>-1</sup> )



Partial branching fraction:

$$\Delta\text{Br} = \text{Br} (B \rightarrow X_u e \nu: 2.3 \text{ GeV}/c < p_e < 2.6 \text{ GeV}/c)$$

$$\Delta\text{Br} = (1.18 \pm 0.11 \pm 0.10) \cdot 10^{-4}$$

Preliminary

Systematic uncertainty:

Model dependent signal efficiency ... 4.5%

$B \rightarrow X_c l \nu$  background estimation ... 4.3%

Extrapolation to whole momentum space:

Using  $B \rightarrow X_s \gamma$  by CLEO [PRL87,251807 (2001)]

$$\text{Br} (B \rightarrow X_u e \nu) = \Delta\text{Br} / f_u = (1.60 \pm 0.15 \pm 0.14 \pm 0.44) \cdot 10^{-4}$$

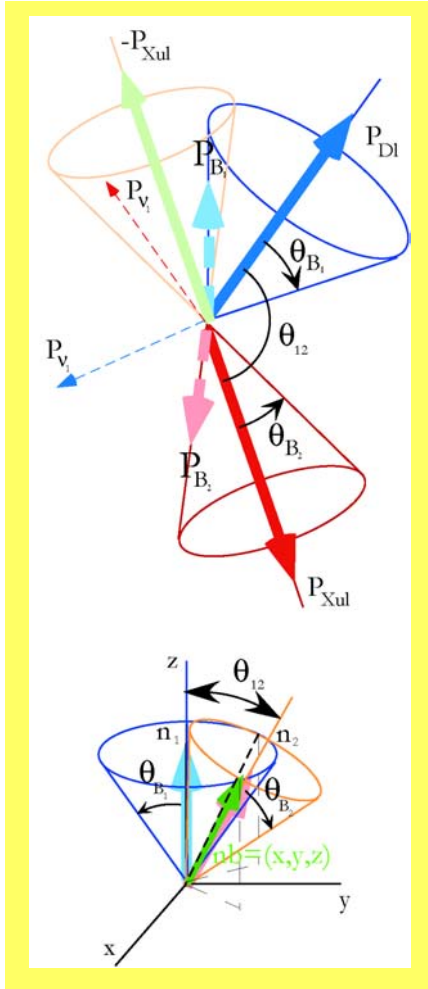
Preliminary

$$|V_{ub}| = (3.96 \pm 0.18 \pm 0.17 \pm 0.55 \pm 0.22) \cdot 10^{-3}$$



# D(\*)lv tag : the method

- Tag events with both B decaying semileptonically



Tag side  $\rightarrow$   $(B \rightarrow D^{(*)} lv)$  &  $(B \rightarrow X lv)$   $\leftarrow$  Signal side

Requirements:

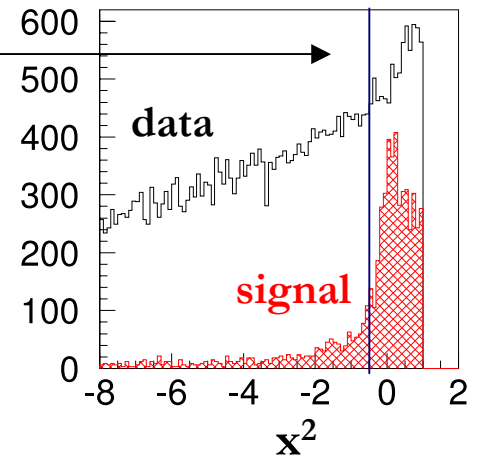
Reconstructed  $D^{(*)}$  meson and 2 leptons with opposite charge

Kinematics solvable, if:

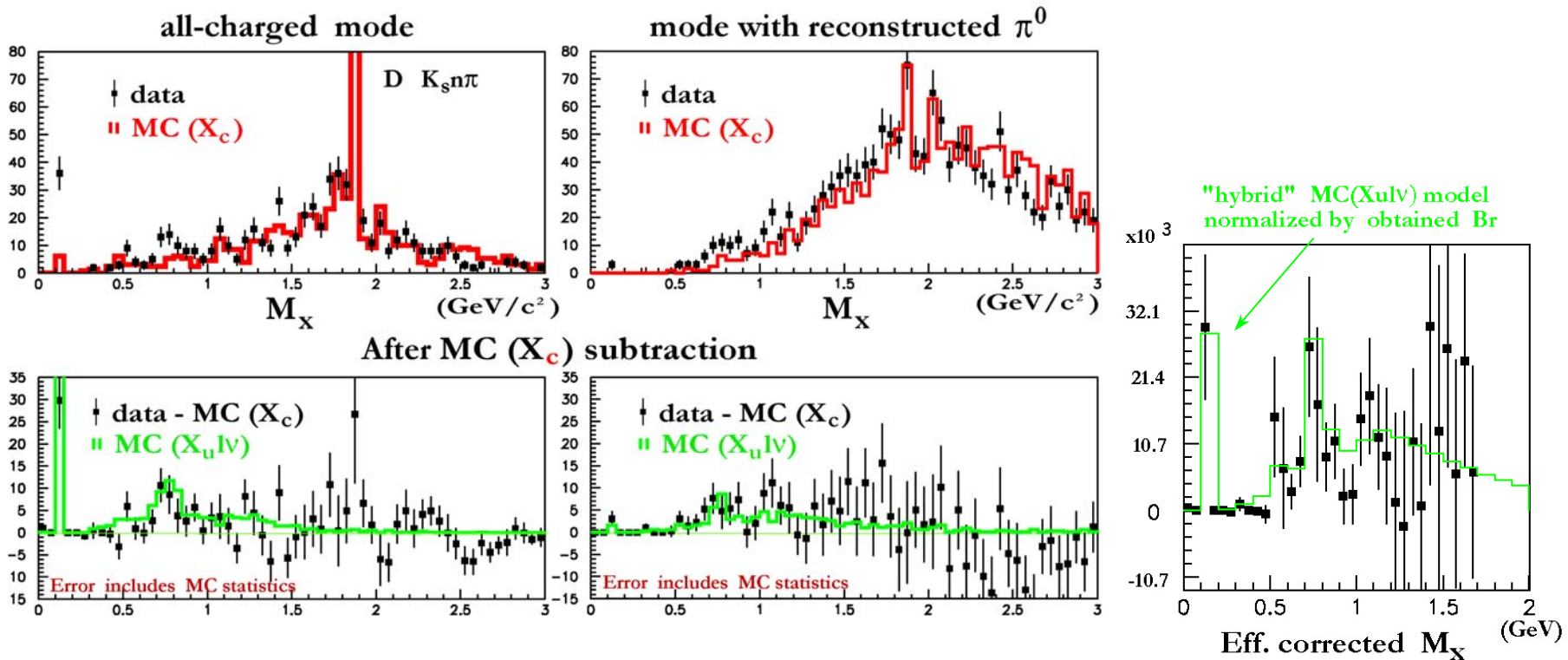
$$x^2 = 1 - (\cos^2\theta_{B1} + \cos^2\theta_{B2} - 2 \cos\theta_{B1} \cos\theta_{B2} \cos\theta_{12}) / \sin^2\theta_{12}$$

Due to experimental  
resol. : cut  $x^2 > -0.2$

$X_u/X_c$  separation by demanding  
no detected  $K^\pm$  on the signal side



# $D^{(*)}lv$ tag : the result ( $78 \text{ fb}^{-1}$ )



$$N(B \rightarrow X_u lv: m_x < 1.5 \text{ GeV}/c^2, p_1 > 1 \text{ GeV}/c, \text{ all charged}) = 82 \pm 19$$

$$N(B \rightarrow X_u lv: m_x < 1.5 \text{ GeV}/c^2, p_1 > 1 \text{ GeV}/c, \pi^0 \text{ associat.}) = 92 \pm 21$$

Preliminary

$$\text{Br}(B \rightarrow X_u lv) = (2.62 \pm 0.63 \pm 0.23 \pm 0.05 \pm 0.41) \cdot 10^{-4}$$

stat. sys. model  
b→c b→u

exp. theo.

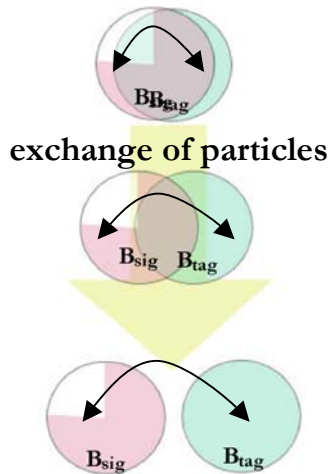
$$|V_{ub}| = (5.0 \pm 0.64 \pm 0.53) \cdot 10^{-3}$$

# Advanced $\nu$ reconstruction tag : the result ( $78 \text{ fb}^{-1}$ )

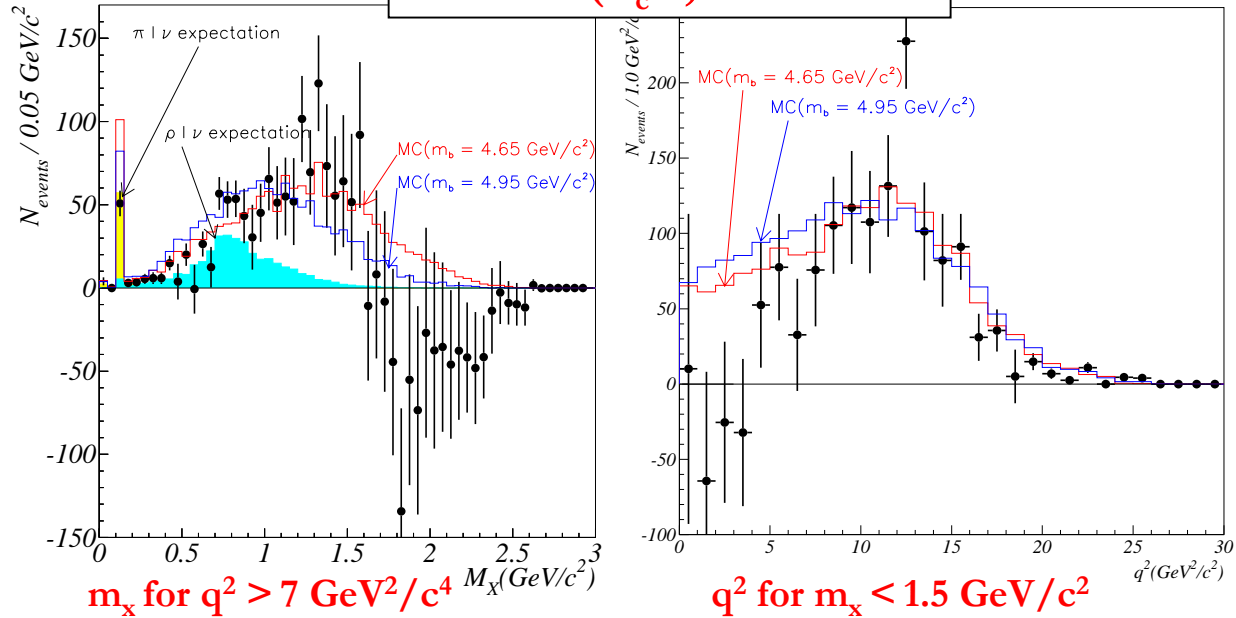
by minimising:

$$W = \frac{\text{PDF}(\text{random})}{\text{PDF}(\text{rand.}) + \text{PDF}(\text{correct})}$$

$$\text{PDF}(p_B, E_B, M_{\text{miss}}, \dots)$$



After MC( $X_c l \nu$ ) subtraction



$$N(\text{B} \rightarrow X_u l \nu: m_x < 1.5 \text{ GeV}/c^2 \quad q^2 > 7 \text{ GeV}^2/c^4) = 1148 \pm 98$$

Preliminary

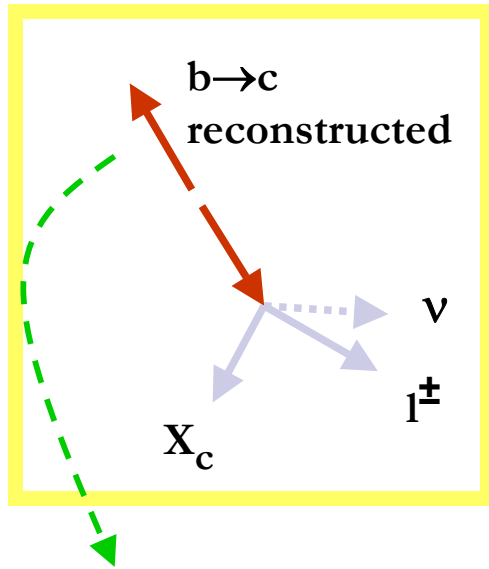
$$\text{Br}(\text{B} \rightarrow X_u l \nu) = (1.64 \pm 0.14 \pm 0.36 \pm 0.28 \pm 0.22) \cdot 10^{-4}$$

stat.
sys.
model
b→c
b→u

exp. theo.

$$|V_{ub}| = (3.96 \pm 0.47 \pm 0.52) \cdot 10^{-3}$$

# $B \rightarrow X_l \nu$ using full reconstruction of the other B



- Measuring B flavour/ lepton charge correlation
- Lepton momentum measurement in B rest-frame

- Subtraction of continuum ( $8.8 \text{ fb}^{-1}$  of offresonance data)
- Taking into account other background:  
Leptons from  $J/\psi$ ,  $\gamma$  conv., upper vertex charm
- Numbers corrected for mixing in the  $B^0$  case

## Reconstructed channels:

$B^0 \rightarrow D^{*+}\pi^- / D^{*+}\rho^- / D^{*+}a_1^- ; D^+\pi^- / D^+\rho^- / D^+a_1^-$

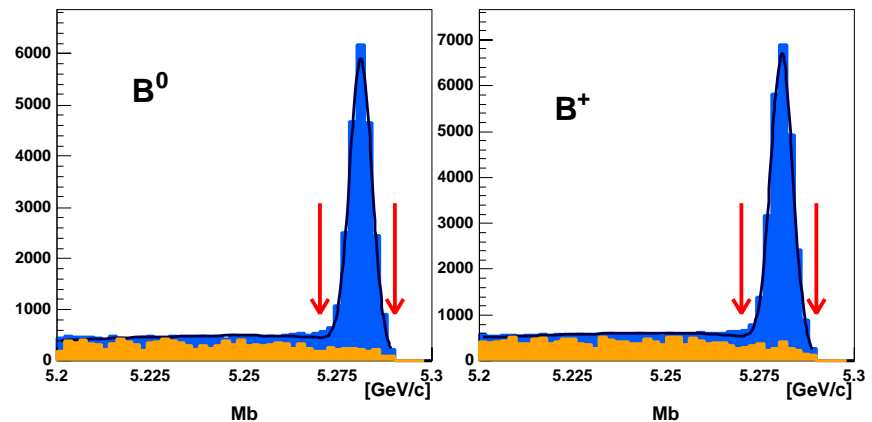
$B^- \rightarrow D^{*0}\pi^- / D^{*0}\rho^- / D^{*0}a_1^- ; D^0\pi^-$

( $B^- \rightarrow D^+\rho^- / D^+a_1^-$  not used due to low purity)

$D^* \rightarrow D^0\pi$

$D^0 \rightarrow K\pi / K\pi\pi^0 / K\pi\pi\pi / K_s\pi\pi$

Beam constrained mass:  $\sqrt{(E_{\text{beam}} - p_B)^2}$

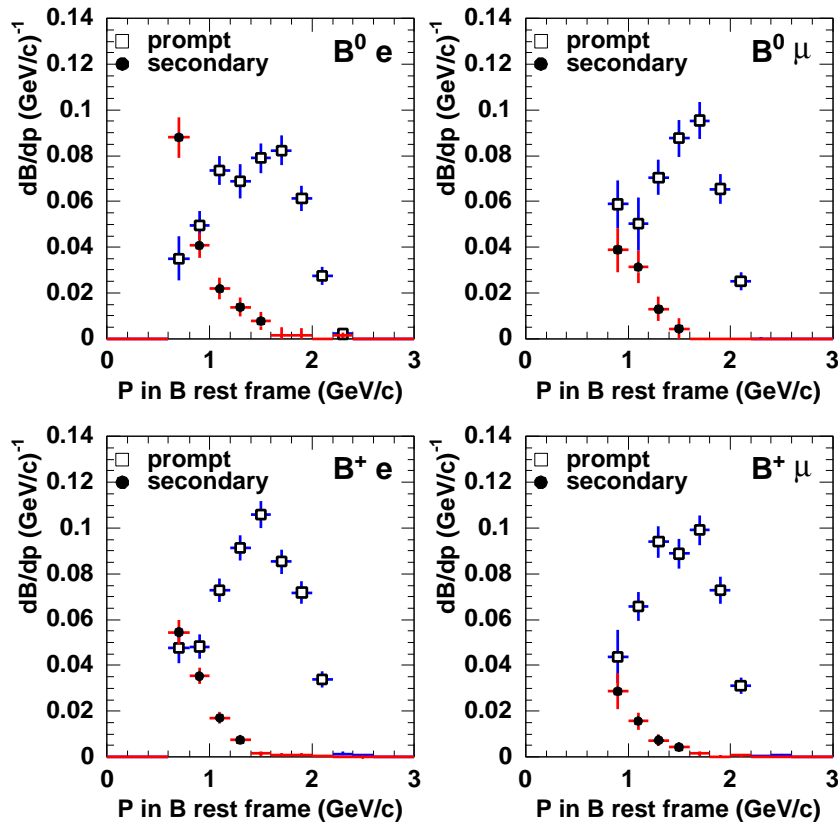


$N(B^0) = 21915 \pm 202$

$N(B^+) = 24529 \pm 227$

# B → Xlv using full rec. of the other B: the results ( 78 fb<sup>-1</sup> )

Lepton momentum in B rest frame



$$\text{Br}(B^0 \rightarrow Xlv) = (10.32 \pm 0.32 \pm 0.29)\% \quad \begin{matrix} \text{stat.} \\ \text{sys.} \end{matrix}$$

$$\text{Br}(B^+ \rightarrow Xlv) = (11.77 \pm 0.26 \pm 0.32)\%$$

Preliminary

$$\text{Br}(B \rightarrow Xlv) = (11.19 \pm 0.20 \pm 0.31)\% \quad \begin{matrix} \text{stat.} \\ \text{sys.} \end{matrix}$$

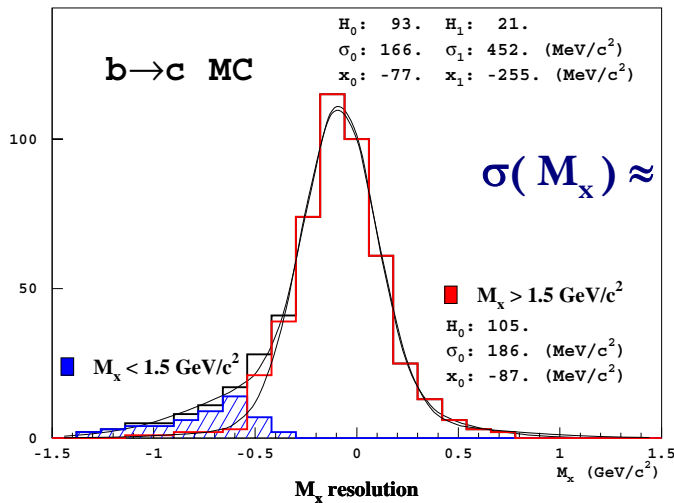
$$\text{Br}(B^+)/\text{Br}(B^0) = 1.14 \pm 0.04 \pm 0.01$$

Consistent with B<sup>+</sup>/B<sup>0</sup> lifetime ratio

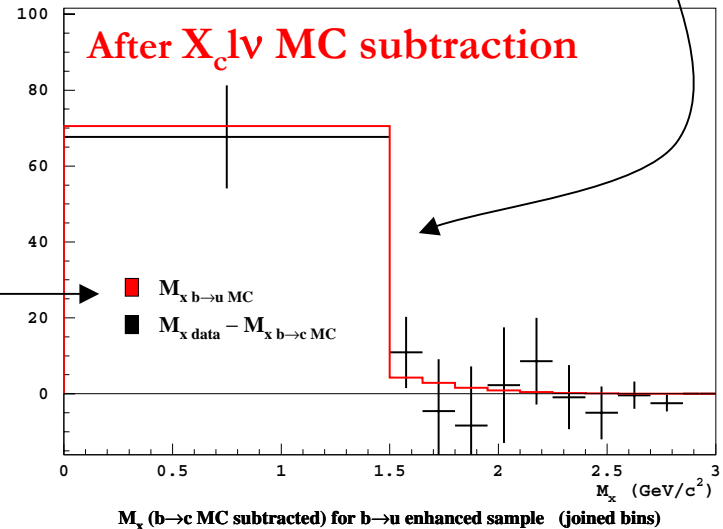
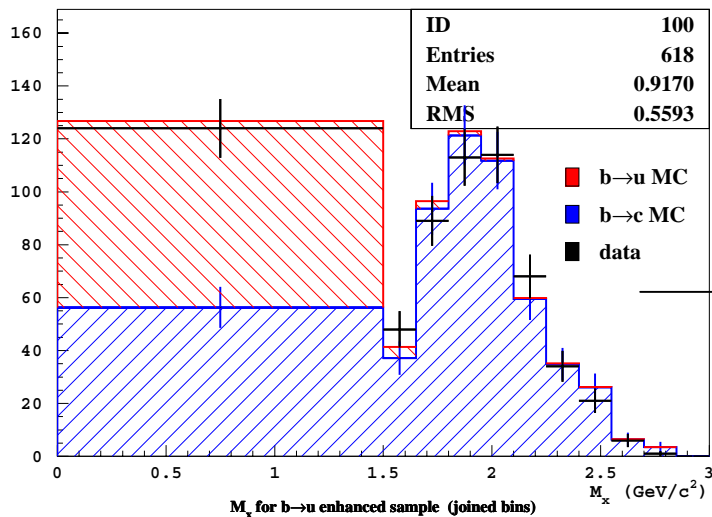
Preliminary

$$|V_{cb}| = (4.13 \pm 0.07 \pm 0.25) \cdot 10^{-2} \quad \begin{matrix} \text{exp.} \\ \text{theo.} \end{matrix}$$

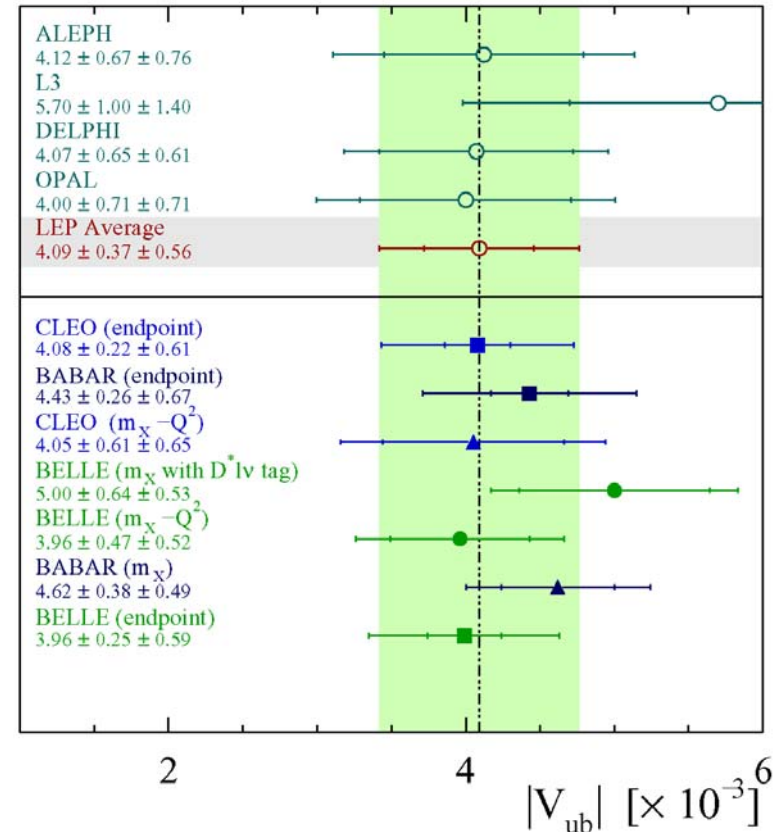
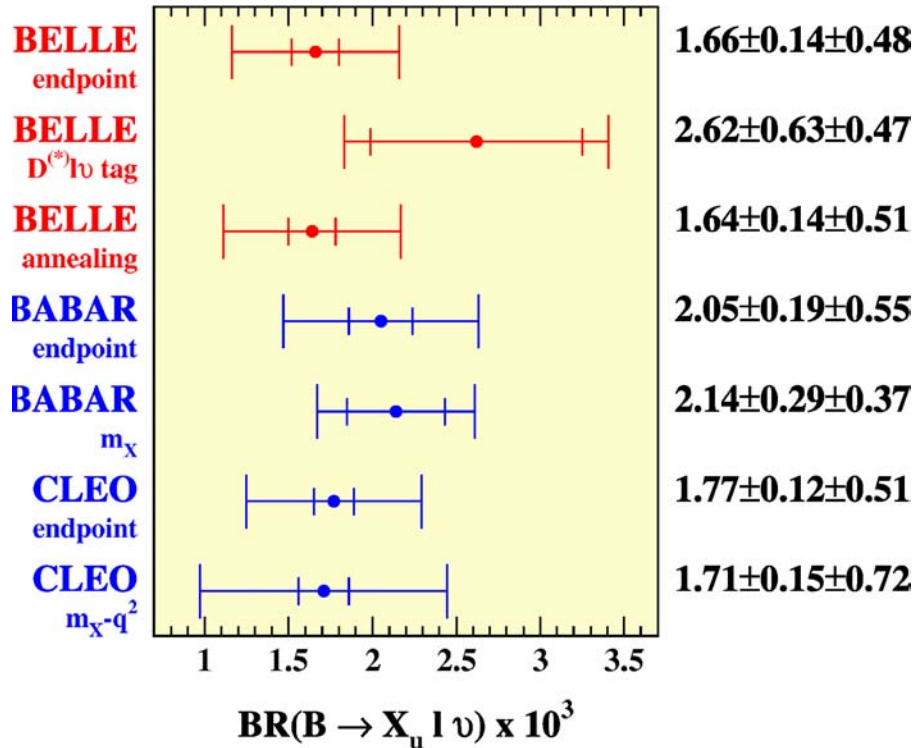
# Full reconstruction tag: $|V_{ub}|$ pre-release



- Good  $M_x$  resolution
- Observed excess of events in the low  $M_x$



# $|V_{ub}|$ Results

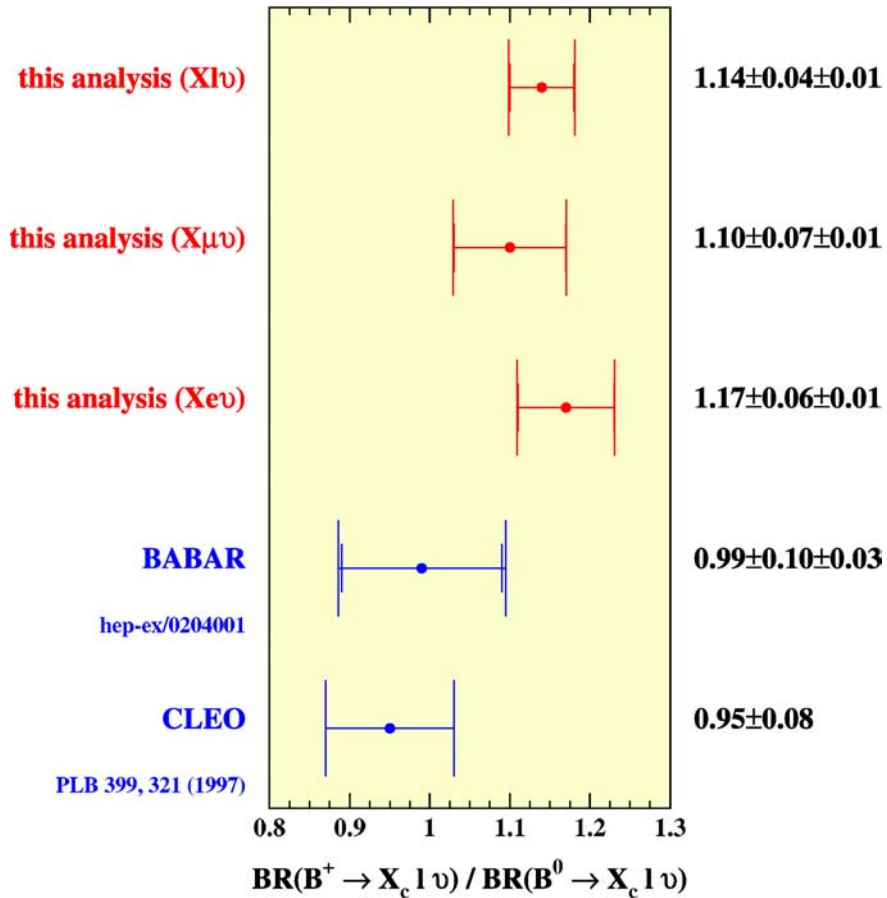
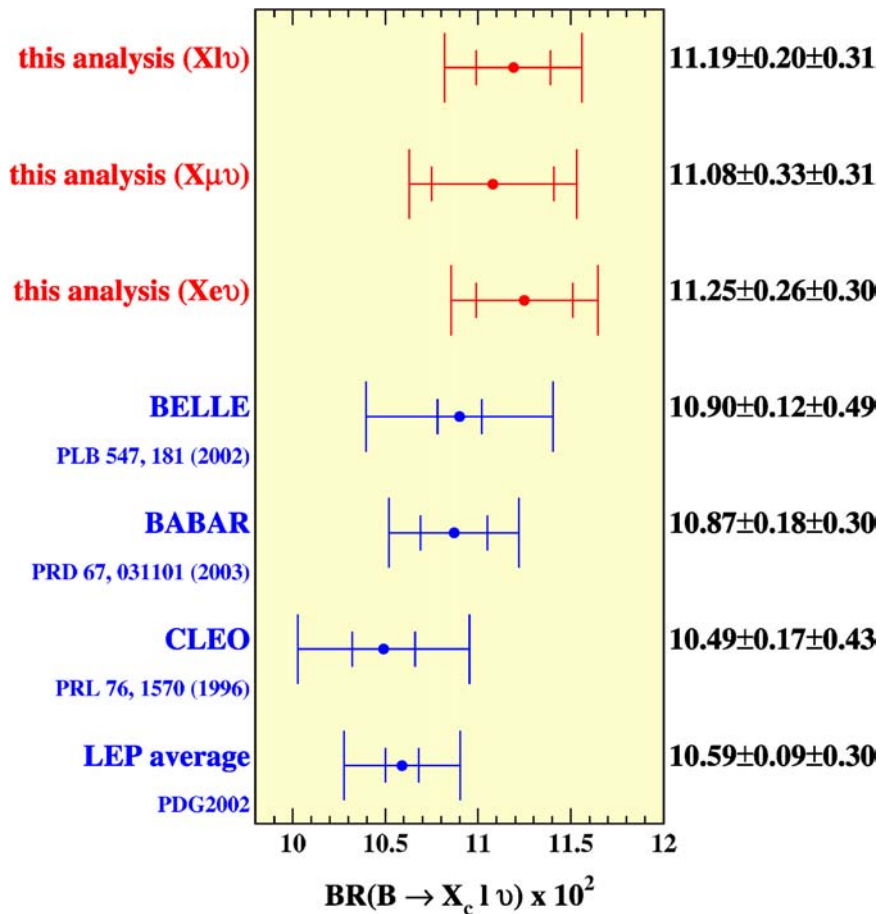


## Exclusive:

$$\text{Br}(B^+ \rightarrow \omega l^+ \nu) = (1.3 \pm 0.4 \pm 0.2 \pm 0.3) \cdot 10^{-4}$$



# $|V_{cb}|$ Results



Preliminary

$$|V_{cb}| = (4.13 \pm 0.07 \pm 0.25) \cdot 10^{-2}$$

exp.      theo.

# Conclusion

$$|V_{ub}|$$

Inclusive measurements by using  $M_x / q^2$

Lepton endpoint measurement

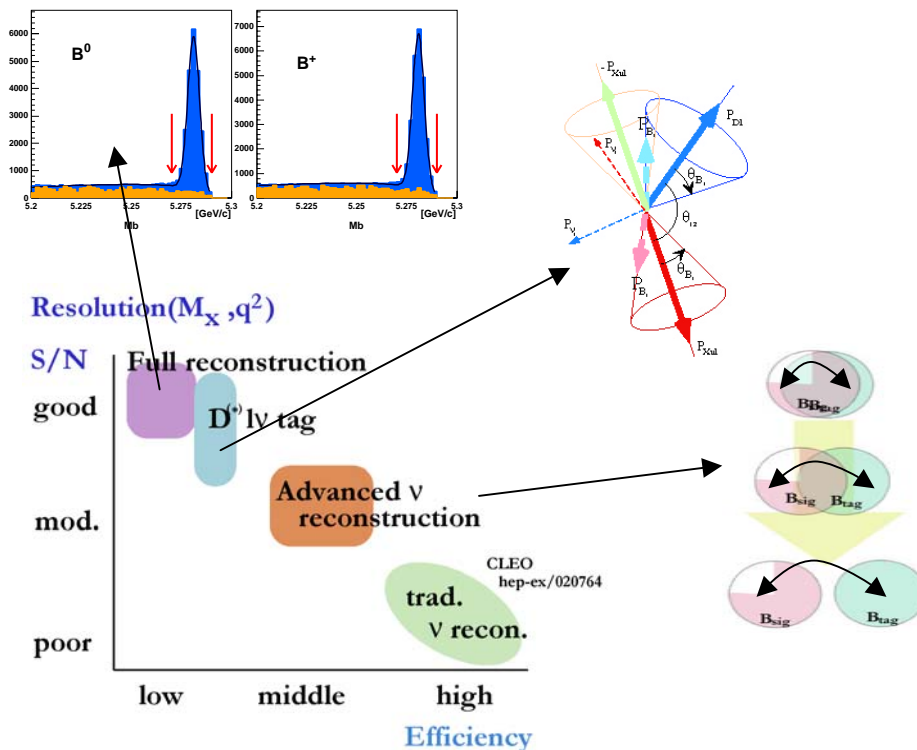
Exclusive result for  $\omega l^+ \nu$

$$|V_{cb}|$$

Inclusive measurement on fully recon. sample

Finalise the analyses + use the whole data set

Preliminary number for  $|V_{ub}|$  with full reconstruction method out soon



## Future