



Study of $B \rightarrow KKl\nu_l$ Decays at Belle

Matic Lubej

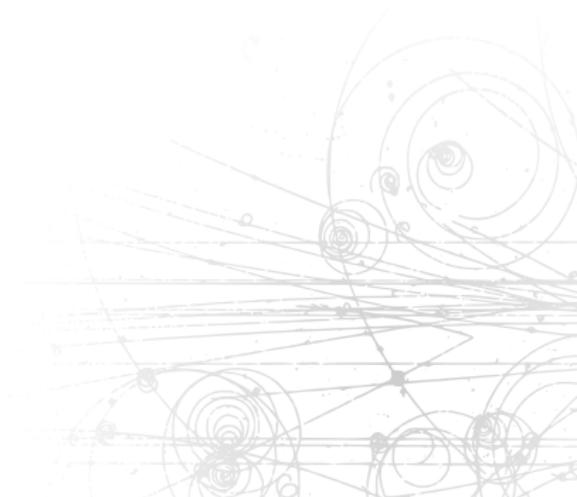
PhD Thesis Defense

Ljubljana, November 22nd, 2018



Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup
- 4 Analysis Procedure
- 5 Parameter Extraction
- 6 Systematic Uncertainties
- 7 Results



Introduction I – Standard Model

- The Standard Model (SM) is a basic theory which describes elementary particles and interactions between them
- Quarks: can be grouped into baryons ($q_1q_2q_3$) or mesons (\bar{q}_1q_2)
- Focus of this analysis are B mesons: B^+ ($\bar{b}u$) and B^- ($b\bar{u}$)

	1 st	2 nd	3 rd					
LEPTONS	0.51 M e -1 1/2 electron	105.66 M μ -1 1/2 muon	1.78 G τ -1 1/2 tau	0 γ 0 1 photon	125.09 G H 0 0 higgs	electromagnetic interaction		
	< 2 ν_e 0 1/2 e neutrino	< 0.19 M ν_μ 0 1/2 μ neutrino	< 18.2 M ν_τ 0 1/2 τ neutrino	80.38 G W -1 1 W boson			91.19 G Z 0 1 Z boson	weak nuclear interaction
	FERMIONS			BOSONS				
QUARKS	2.2 M u +2/3 1/2 up	1.28 G c +2/3 1/2 charm	173.1 G t +2/3 1/2 top	Mass: eV/c ² Charge Spin Name				
	4.7 M d -1/3 1/2 down	96 M s -1/3 1/2 strange	4.18 G b -1/3 1/2 bottom	0 g 0 1 gluon		strong nuclear interaction		

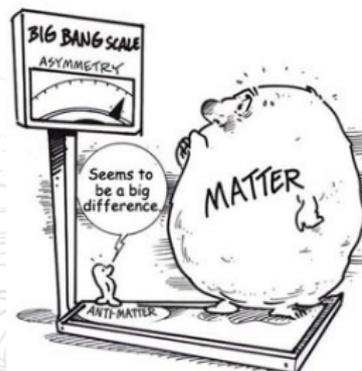
Introduction II – CP Violation

- C (charge conjugation), P (parity) and T (time reversal) symmetries were believed to be conserved individually (based on EM interaction, 1954)
- Observation of P symmetry violation confused physicists (1956)
- Observation of CP symmetry violation confused physicists even more (1964)

CP symmetry? → A sort of a “physics mirror”, stating that the laws of physics should be the same if observed through said mirror.



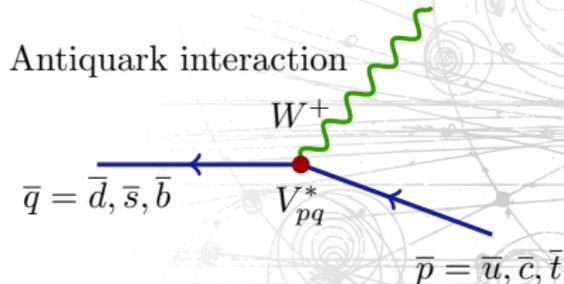
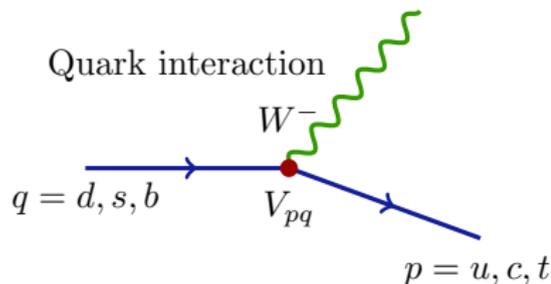
- CP violation one of the necessary conditions for matter and antimatter asymmetry in the universe
- This analysis is one of the many steps toward a better understanding of our universe



Introduction III – CKM Matrix

- CP violation is described by the Cabibbo-Kobayashi-Maskawa (CKM) matrix
- It is a complex and unitary matrix
- Contains transition probabilities from one quark to the other (charged weak interaction)

$$V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}, \quad |V_{ij}|^2 \propto q_i \leftrightarrow q_j \text{ transition probability}$$

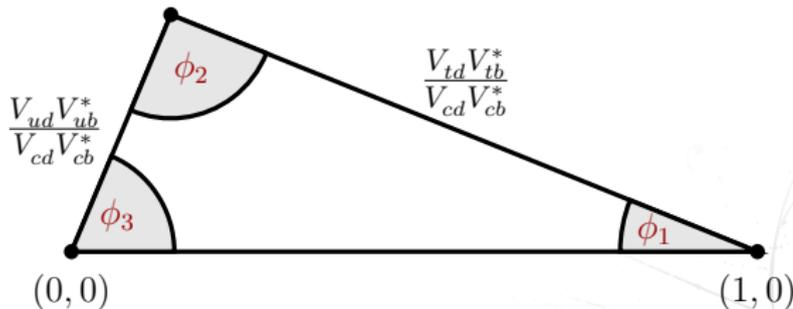


Introduction IV – Unitarity Triangle

- The most relevant unitarity condition of the CKM matrix for this analysis is

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

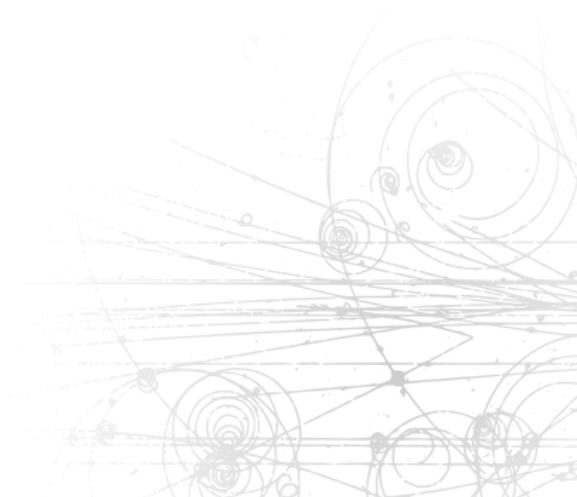
$$(\bar{\rho}, \bar{\eta}) \approx (\rho, \eta) + \mathcal{O}(\lambda^2)$$



- By measuring the sides and angles of the triangle, we can overconstrain it and check if all the sides meet
- CKM matrix elements are not determined by theory or experiment alone, but by their joint effort

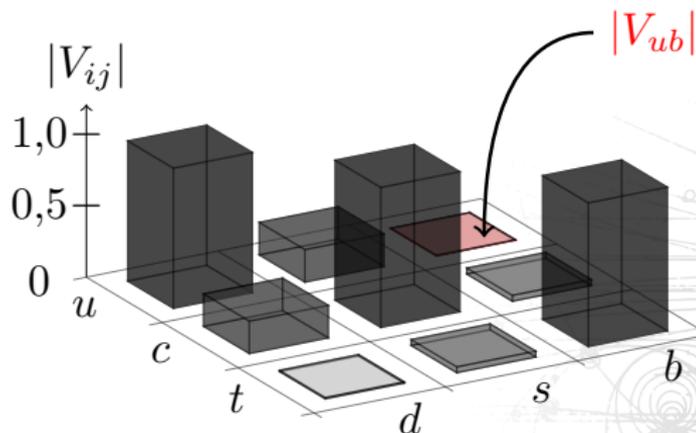
Overview

- 1 Introduction
- 2 Motivation**
- 3 Experimental Setup
- 4 Analysis Procedure
- 5 Parameter Extraction
- 6 Systematic Uncertainties
- 7 Results



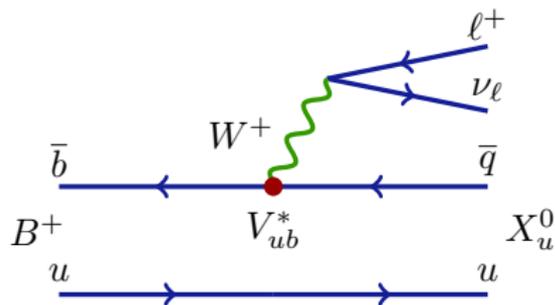
Motivation I – Why V_{ub} ?

- The magnitude of CP violation that we know of is not large enough to account for the matter and antimatter asymmetry
- We are searching for new physics (NP) processes, which are not described by our current model
- $|V_{ub}|$ has the smallest value and the largest uncertainty of all the CKM matrix elements, precision measurements require better accuracy



Motivation II – Why B Mesons?

- B mesons exhibit a rich spectrum of decay modes, out of which many allow the study of the underlying physics processes
 - Decays are deeply connected to the CKM matrix
- We focus on the charmless semileptonic B meson decays of the form $B^+ \rightarrow X_u^0 \ell^+ \nu_\ell$ (inclusion of charge conjugated B^- decays is implied)
 - Such decays are used to determine the $|V_{ub}|$ CKM matrix element



Reliable **experimental measurements** along with precise **theoretical calculations** enable the determination of the $|V_{ub}|$

$$d\Gamma \propto G_F^2 |V_{ub}|^2 |L^\mu \langle X_u | \bar{u} \gamma_\mu \frac{1}{2} (1 - \gamma_5) b | B \rangle|^2,$$

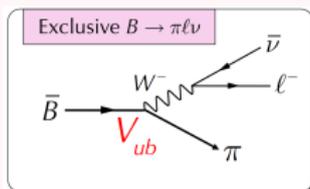
Γ is the decay width, L^μ is the leptonic current and $\langle \dots \rangle$ is the hadronic current.

Motivation III – Why This Analysis?

There are two common methods of $|V_{ub}|$ determination

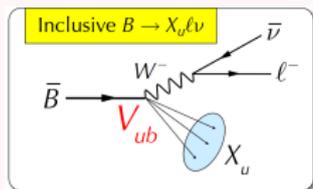
Exclusive

- B decays to a specific hadronic final state X_u (such as π or ρ)



Inclusive

- B meson decays to any hadronic final state X_u



Both methods require different experimental and theoretical approaches, therefore yield largely independent results

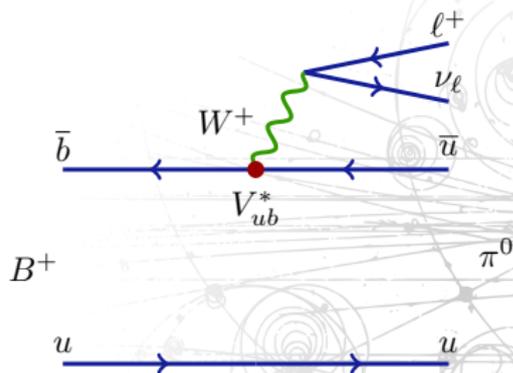
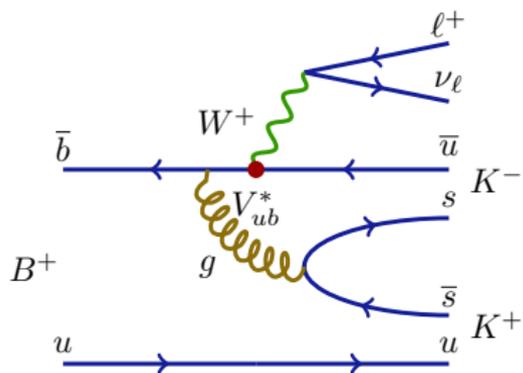
$$|V_{ub}|_{\text{excl.}} = (3.65 \pm 0.09 \pm 0.11) \times 10^{-3},$$

$$|V_{ub}|_{\text{incl.}}^{\text{GGOU}} = \left(4.52 \pm 0.15 \begin{matrix} +0.11 \\ -0.14 \end{matrix}\right) \times 10^{-3},$$

However, they agree only at a 3σ level \rightarrow The V_{ub} puzzle

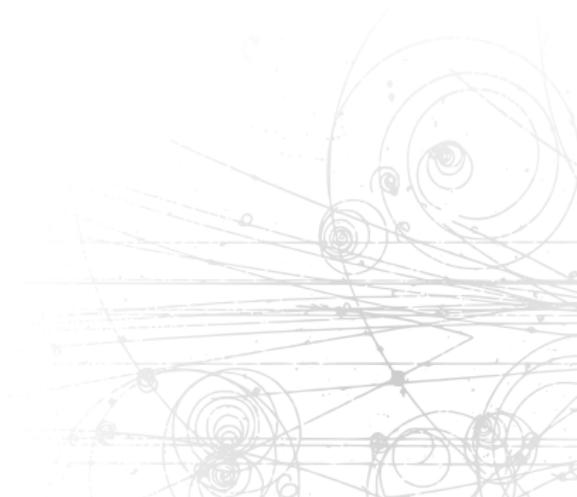
Motivation IV – Why This Decay?

- Primary: The decay has not been observed yet
- The decay $B \rightarrow KK\ell\nu$ is similar to the $B \rightarrow \pi\ell\nu$ decay, so a similar analysis process can be applied
- Kaons ($K^+(u\bar{s})$) are usually present in $b \rightarrow c(\rightarrow s)$ decays, so a K -veto is used to remove such background cases in inclusive V_{ub} studies
 → **but this is a charmless process ($b \rightarrow u$) with kaons in the final state!**
- Secondary: Impact of not taking these decays into account?



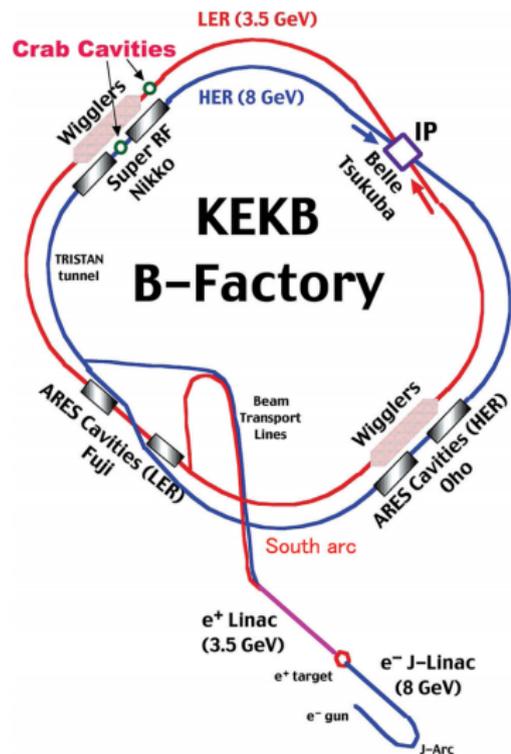
Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup**
- 4 Analysis Procedure
- 5 Parameter Extraction
- 6 Systematic Uncertainties
- 7 Results



Experimental Setup I – KEKB Accelerator

- Two rings (e^+ and e^-) with a diameter ≈ 1 km
- Particles are produced in events when e^+ and e^- collide
- Energy in the center-of-mass frame is 10.58 GeV
 - corresponds to $\Upsilon(4S)$ meson mass
- B factories are known for abundant production of B mesons

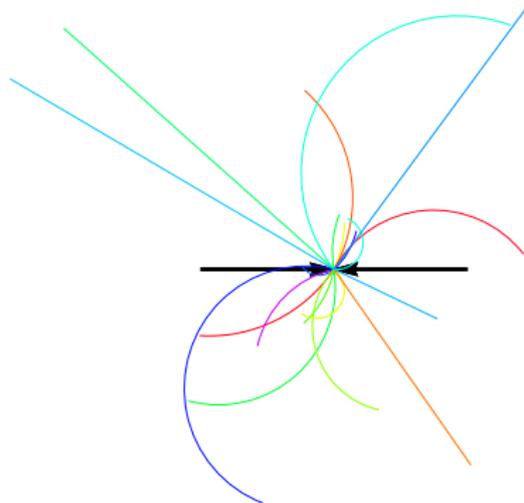


Experimental Setup II – Particle Detection



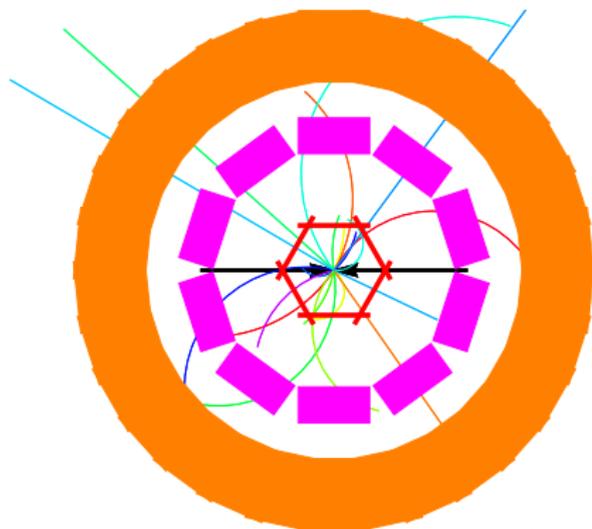
- Event – collision of e^+ and e^-

Experimental Setup II – Particle Detection



- Event – collision of e^+ and e^-
- Production of new particles

Experimental Setup II – Particle Detection



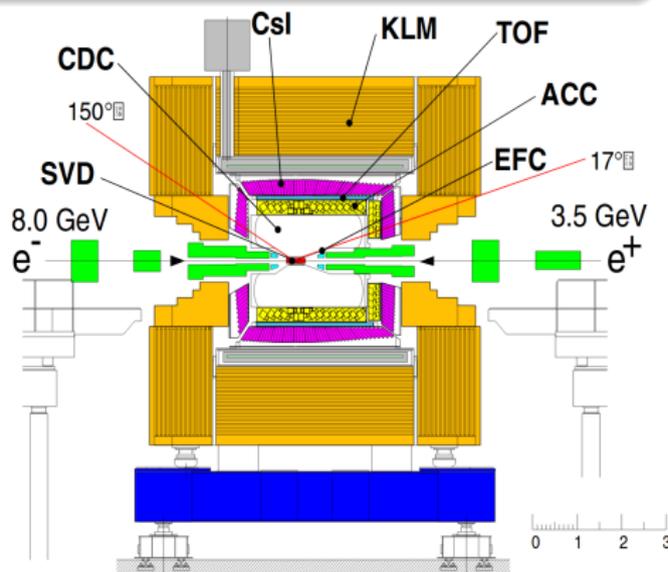
- Event – collision of e^+ and e^-
- Production of new particles
- Detection of final, stable particles

Experimental Setup III – Belle Detector

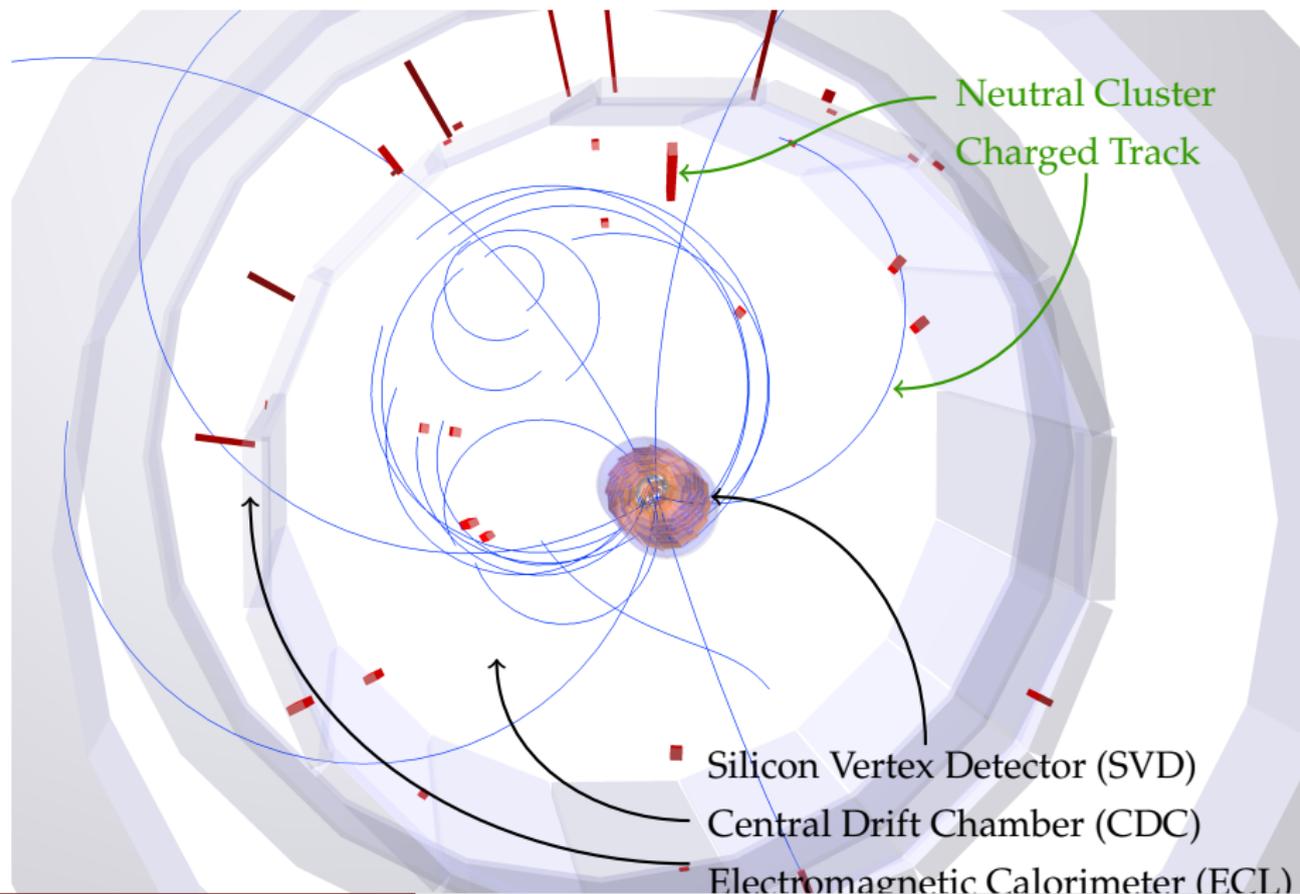
- A cylindrically symmetric magnetic spectrometer
- Wide solid angle coverage ($\sim 92\%$)
- Specialized for e^+e^- collisions
- Constructed from several subdetectors, each with its own purpose

Belle II detector subsystems:

- Decay vertex determination
- Tracking
- Particle identification
- Calorimetry

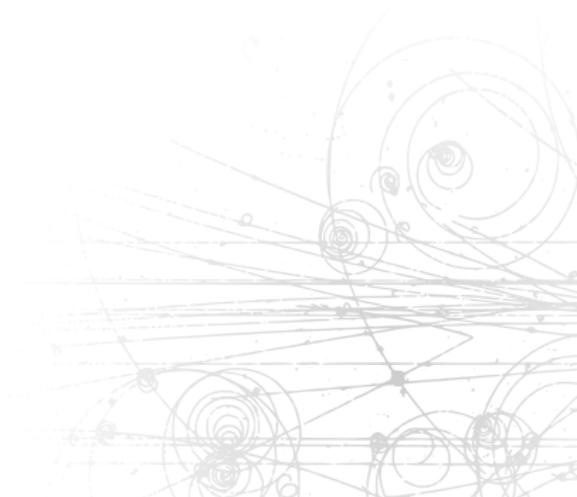


Experimental Setup III – Belle Detector Subsystems



Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup
- 4 Analysis Procedure**
- 5 Parameter Extraction
- 6 Systematic Uncertainties
- 7 Results

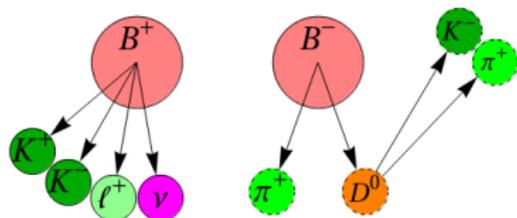


Analysis I – Method overview

- Initial state well known: $e^+e^- \rightarrow \Upsilon(4S) @ E_{CMS} \approx M_{\Upsilon(4S)}$
- $\Upsilon(4S)$ at rest $\rightarrow B\bar{B}$
- Kaons K and the leptons e and μ produce tracks \rightarrow **easily detectable**
- Neutrinos ν interact weakly and escape the detector \rightarrow **missing energy and momentum**

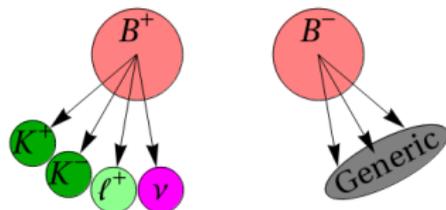
Reconstruction methods

Tagged measurement



Example scheme
of a tagged mode

Untagged measurement



Companion B
not reconstructed

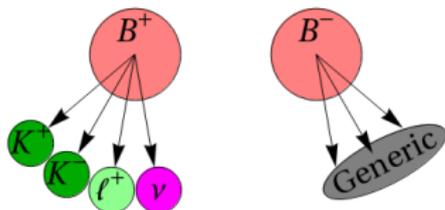
Analysis I – Method overview

- Initial state well known: $e^+e^- \rightarrow \Upsilon(4S) @ E_{CMS} \approx M_{\Upsilon(4S)}$
- $\Upsilon(4S)$ at rest $\rightarrow B\bar{B}$
- Kaons K and the leptons e and μ produce tracks \rightarrow easily detectable
- Neutrinos ν interact weakly and escape the detector \rightarrow missing energy and momentum

Reconstruction methods

Untagged measurement

We opt for this method \rightarrow
Neutrino 4-momentum is inferred
from missing momentum in event
(assuming only 1 neutrino missing)



Companion B
not reconstructed

Analysis II – Particle Reconstruction

Part I: Final State Particles (FSP)

- Charged particles like K , e and μ are reconstructed from tracks, a quality selection is performed
- Neutrinos are weakly interacting and escape detection

Part II: FSP Combinations

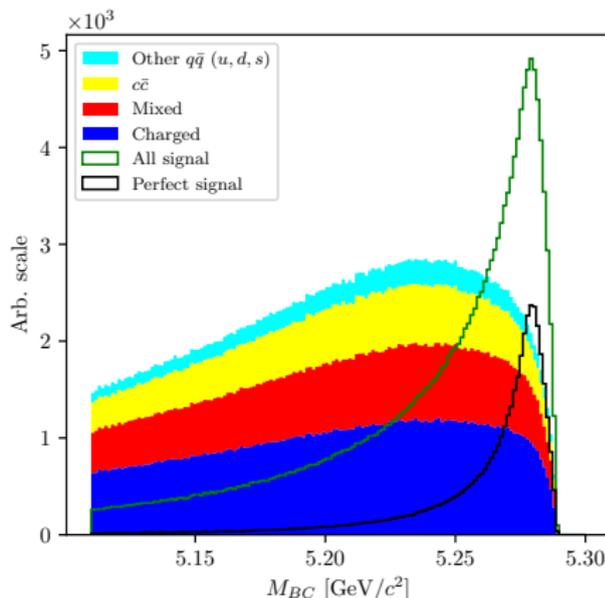
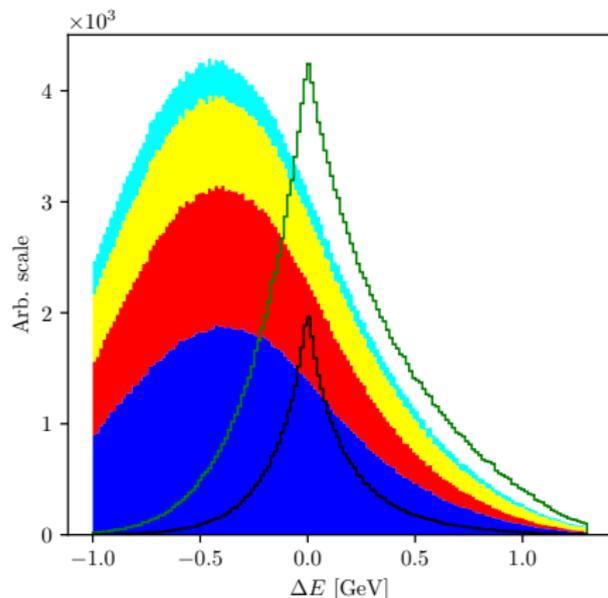
- Combinations of FSP particles KKe and $KK\mu$ represent first B meson candidates with a missing neutrino

Part III: Loose Neutrino Reconstruction

- Rest of Event (ROE) are all the tracks (charged particles) and clusters (neutral particles) which were not used in the reconstruction
- ROE is needed to reconstruct the missing neutrino momentum, where all tracks and clusters from ROE are summed up together

Analysis III – B meson specific variables

$$\Delta E = E_B - E_{CMS}/2, \quad M_{BC} = \sqrt{(E_{CMS}/2)^2 - |\vec{p}_B|^2}$$

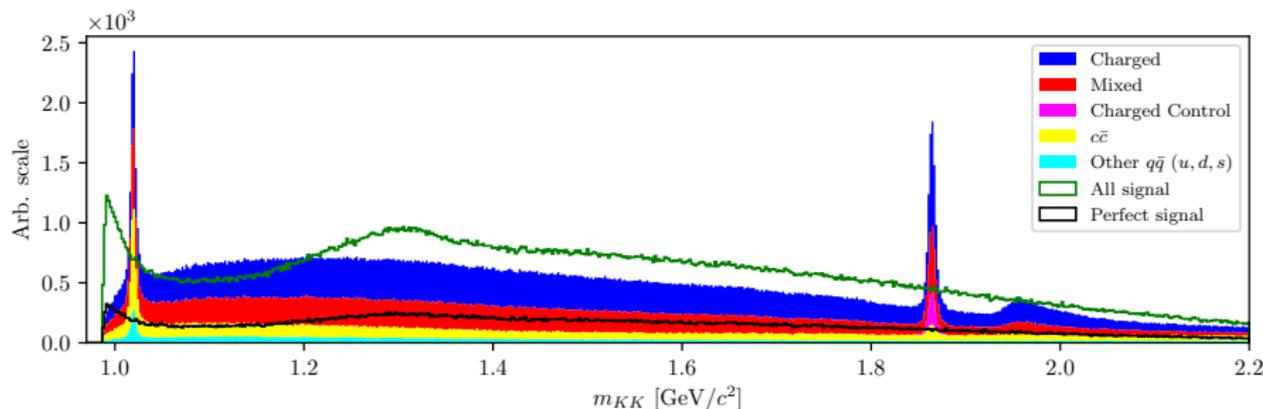


Signal is scaled up. Correctly reconstructed candidates have $\Delta E \approx 0$ and $M_{BC} \approx m_B$

Analysis IV – Control Decay

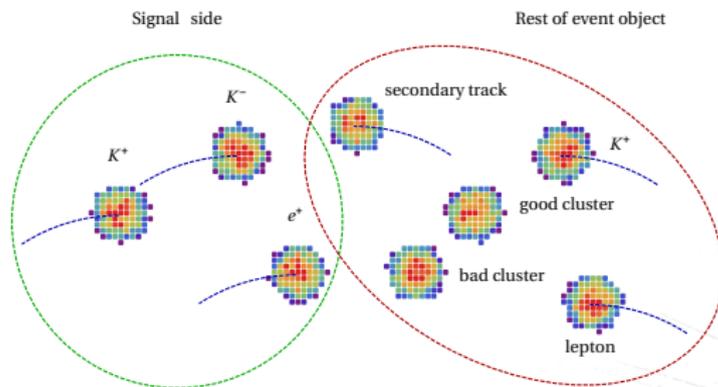
We define a control decay mode, similar to our signal decay mode.

- The decay mode is $B^+ \rightarrow \bar{D}^0 \ell^+ \nu$, $D^0 \rightarrow K^+ K^-$
- The properties of the control and signal decay are very similar
- Its purpose is to continuously check the consistency between simulation (Monte Carlo or MC) and measured data



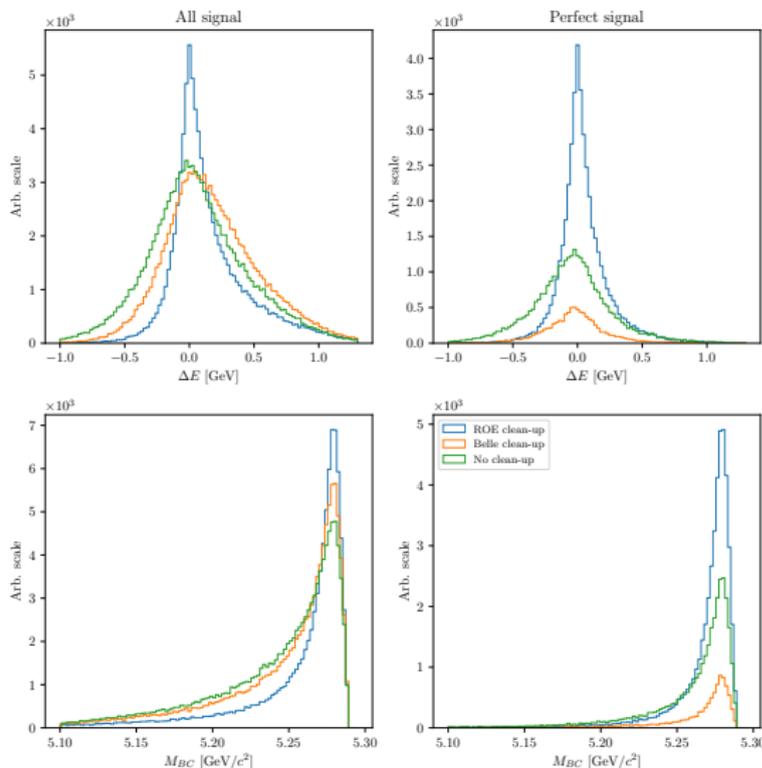
Analysis V – ROE Clean-up

- Rest of Event (ROE) are all the tracks (charged particles) and clusters (neutral particles) which were not used in the reconstruction
- ROE is needed to reconstruct the missing neutrino momentum



- Why? Extra tracks and clusters should not be taken into account when calculating the neutrino 4-momentum
- How? We apply machine learning in several steps of the ROE clean-up in order to efficiently clean it

Analysis VI – ROE Clean-up Results

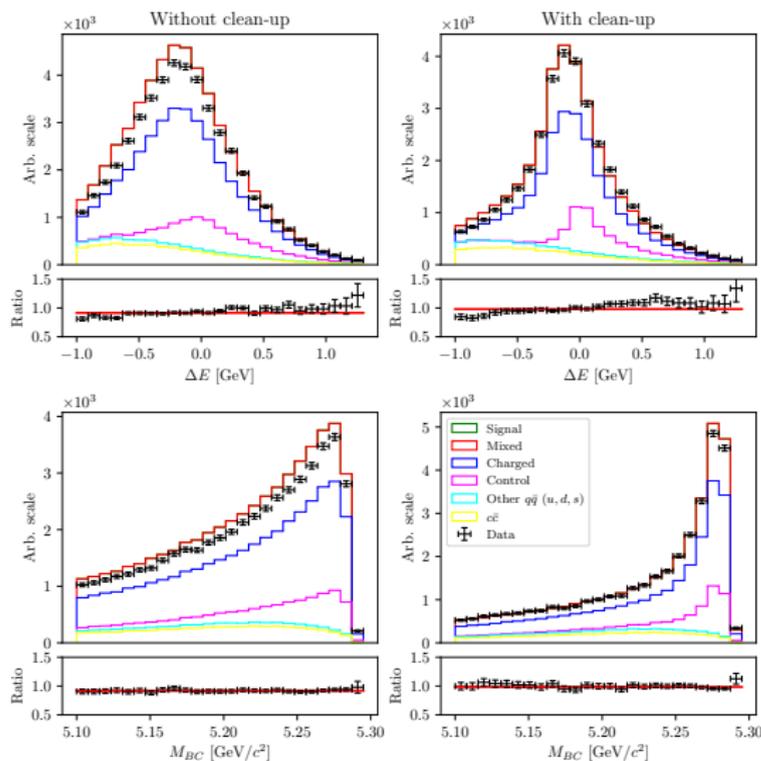


- The procedure **improves the resolution** of signal distribution
- It performs **better** than the standard Belle procedure
- **The efficiency of perfectly reconstructed signal increases**

	ϵ	FWHM
Belle	28.5 %	75.0 %
ROE	140.1 %	35.0 %

Perfectly reconstructed signal candidates are signal candidates from events, where all tracks and clusters are accounted for

Analysis VI – ROE Clean-up Results



- We validate the ROE clean-up procedure on the **control mode**
- ROE clean-up performs well on MC as well as on Daa
- The clean-up procedure does not introduce differences between MC and Data

Analysis VII – Background Suppression

In order to further suppress various sources of background, we use *machine learning algorithms*:

These algorithms take multiple properties of candidates as input and produce an output variable, similar to a signal probability

Boosted Decision Trees (BDT) algorithms are commonly used in the field

Continuum Suppression

- Events of the form $e^+e^- \rightarrow q\bar{q}$, where $q \in [u, d, s, c]$
- Energy and momentum distribution of such events differ from $e^+e^- \rightarrow B\bar{B}$ events

$B\bar{B}$ Suppression

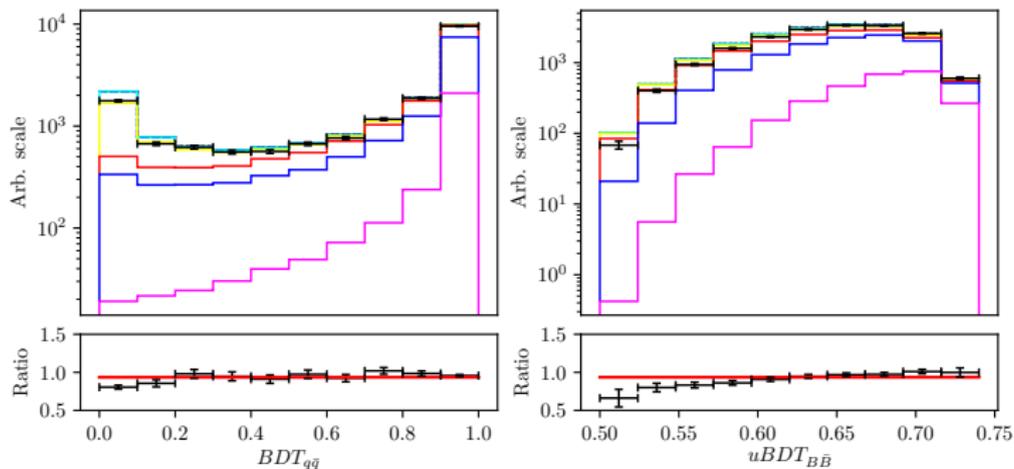
- Deeper look into the properties of the signal decay enable separation of signal from other $e^+e^- \rightarrow B\bar{B}$ events

Analysis VII – Background Suppression

In order to further suppress various sources of background, we use *machine learning algorithms*:

These algorithms take multiple properties of candidates as input and produce an output variable, similar to a signal probability

Boosted Decision Trees (BDT) algorithms are commonly used in the field

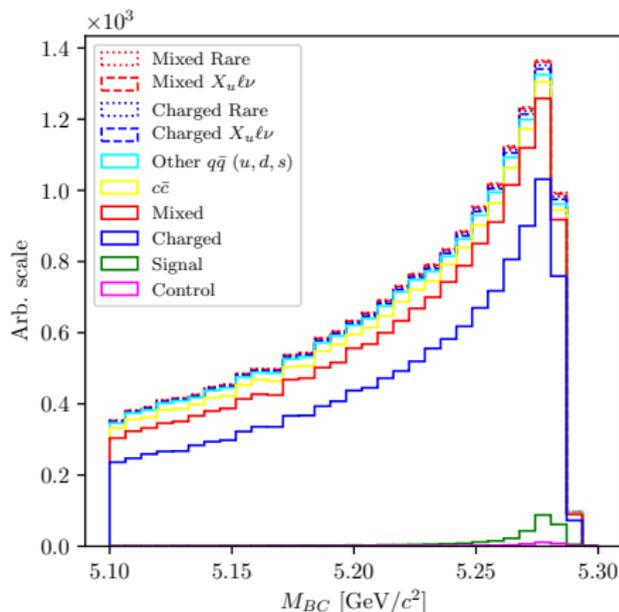
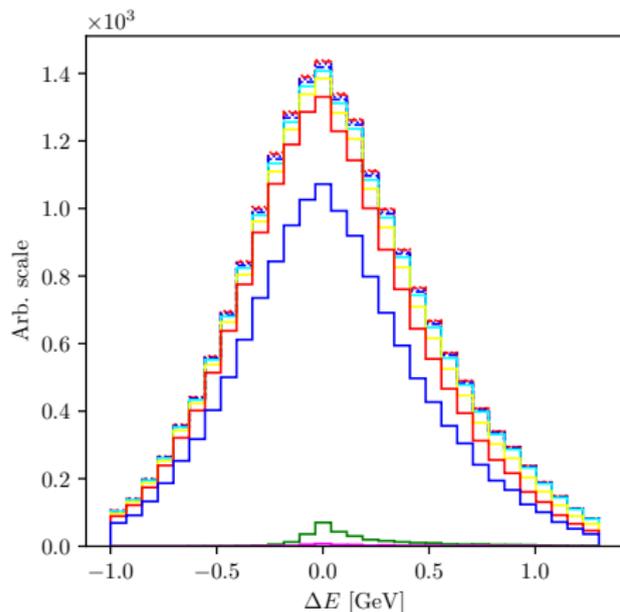


Continuum (left) and $B\bar{B}$ (right) suppression BDT variable. Signal is more likely distributed on the right side of the variables.

Analysis VIII – Final Selection

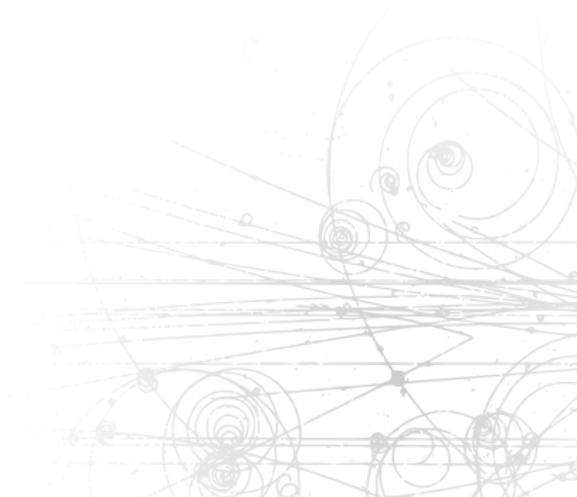
Sample composition after background suppression:

$$N_{\text{sig}} = 264, \quad \frac{N_{\text{sig}}}{N_{\text{bkg}}} = 1.33 \times 10^{-2}$$



Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup
- 4 Analysis Procedure
- 5 Parameter Extraction**
- 6 Systematic Uncertainties
- 7 Results



Parameter Extraction I – Fit Method

- Define “templates” which describe distribution shapes (signal, background, ...)
- For each histogram bin define Poisson probability for it's content w.r.t. the measurement
- Obtain the combination of template yields which maximise the probability

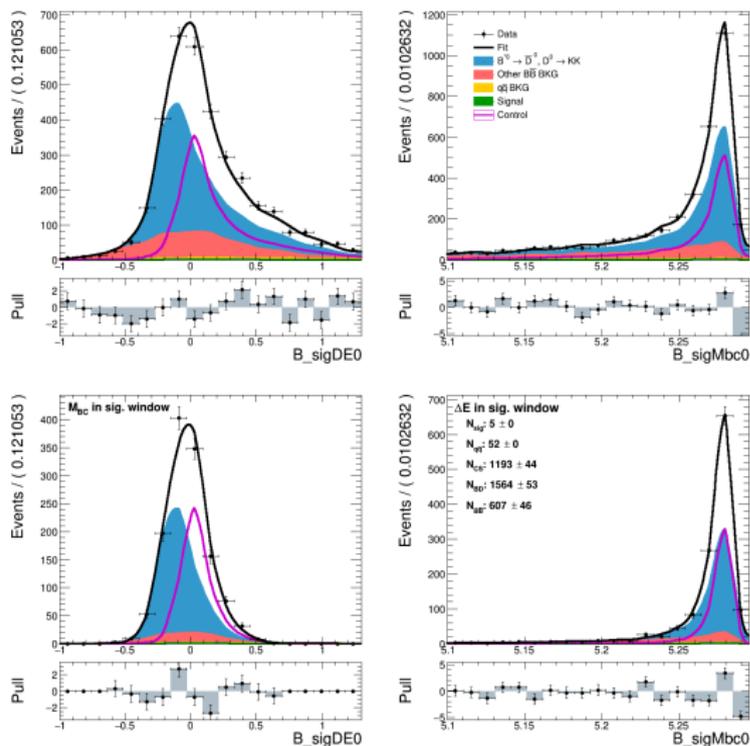
Templates in the signal fit:

- signal
 - continuum
 - well-defined sources \rightarrow of background
 - other $B\bar{B}$ background
- control decay,
 - $B \rightarrow \bar{D}^* \ell^+ \nu, D^0 \rightarrow K^- K^+,$
 - $B \rightarrow \bar{D}^{(*)} \ell^+ \nu, D^0 \rightarrow K^- \pi^+,$
 - $B \rightarrow \bar{D}^{(*)} \ell^+ \nu, D^0 \rightarrow K^- K^+ \pi^0, K^- \pi^+ \pi^0,$
 - $B \rightarrow \bar{D}^{(*)} \ell^+ \nu, D^0 \rightarrow K^- \ell^+ \nu,$
 - $B^0 \rightarrow D^{(*)-} \ell^+ \nu, D^+ \rightarrow K^- K^+ \pi^+, K^- \pi^+ \pi^+,$
 - other $B \rightarrow \bar{D}^{(*)} \ell^+ \nu$ decays,

Yields of all templates are floated, except in the well-defined cases, where yields are constrained by world measurements.

Parameter Extraction II – Control Fit Results

Results of the control decay fit to DATA

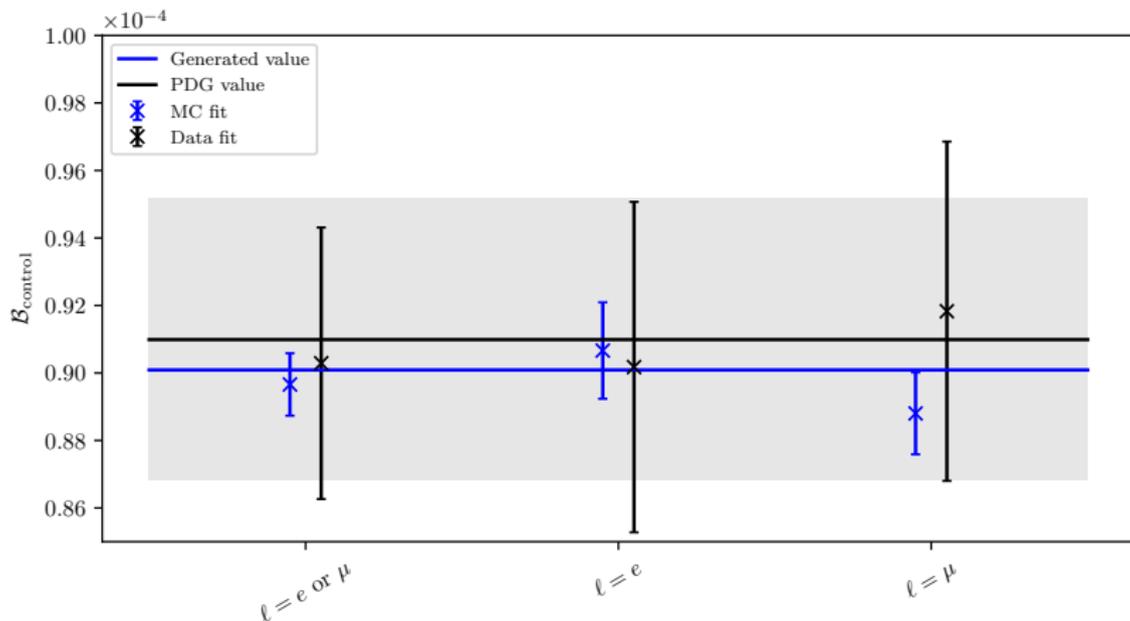


- Plot: White part represented by the **control decay**, which is drawn separately
- **Blue contribution** mostly from $B \rightarrow D^* \ell \nu$, shift in ΔE due to a missing particle (π^\pm)
- Templates are appropriately summed to best fit the measurement
- The fit behaves well, no strange artefacts in pulls

pulls \propto differences between the function and the points

Parameter Extraction II – Control Fit Results

Control decay branching ratio measurement

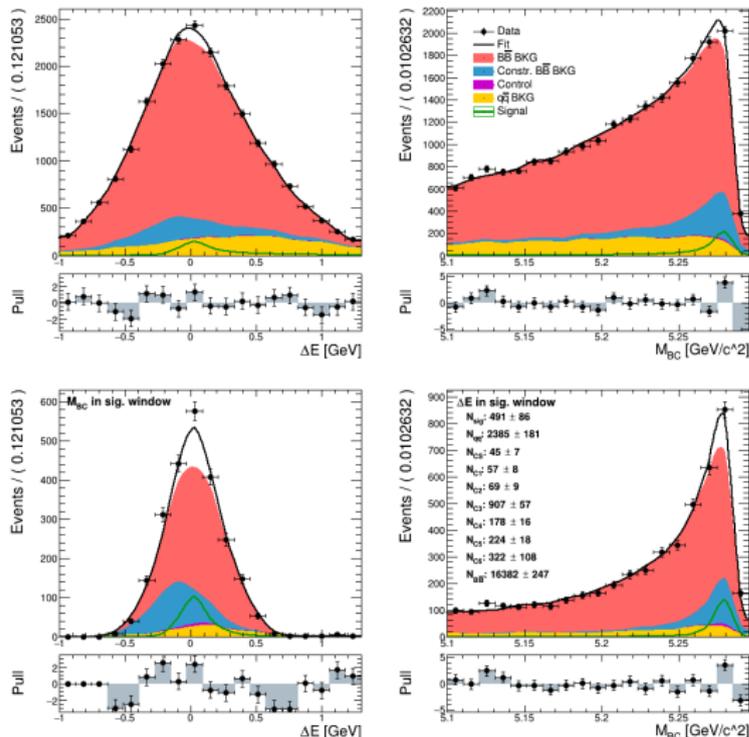


The simulated and measured values of the control decay branching ratio seems to agree well with the generated value and the world average from PDG (<http://pdglive.lbl.gov>).

Parameter Extraction III – Signal Fit Results

Results of the signal decay fit to DATA

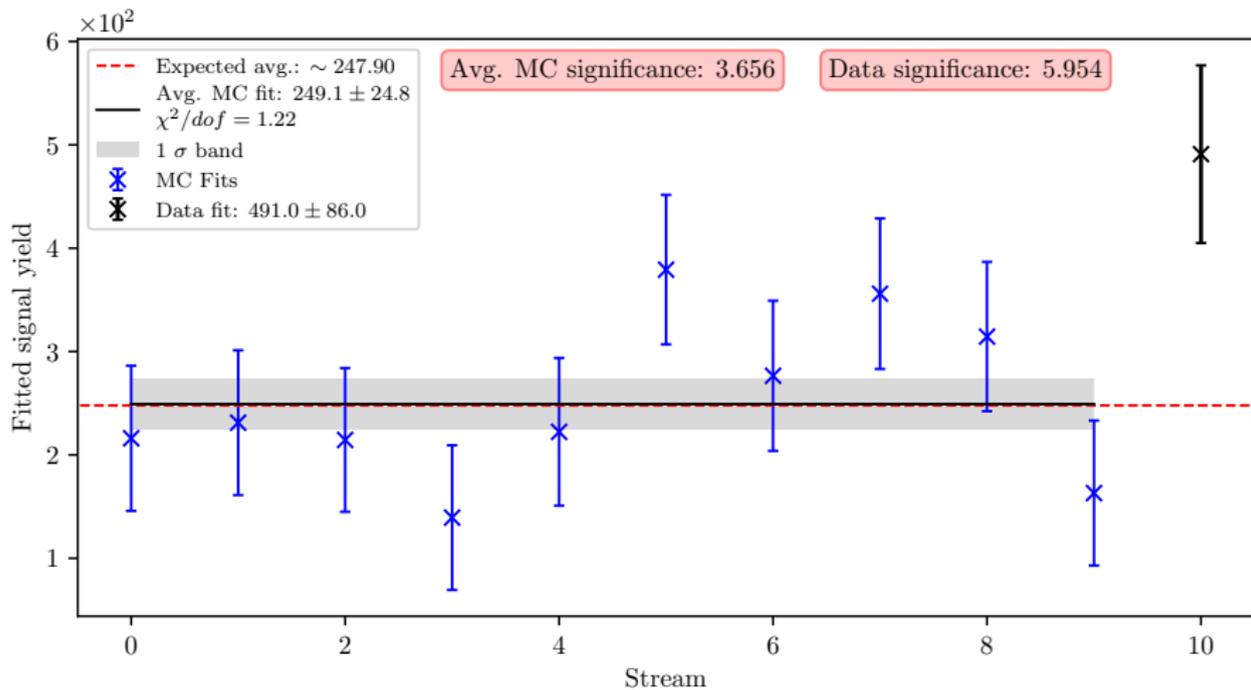
White part represented by the **signal decay**, which is drawn separately



Category	Fit Yield
Signal	491 ± 86
$q\bar{q}$ bkg	2385 ± 181
C_0	45 ± 7
C_1	57 ± 8
C_2	69 ± 9
C_3	907 ± 57
C_4	178 ± 16
C_5	224 ± 18
C_6	322 ± 108
Other BB bkg	16382 ± 247

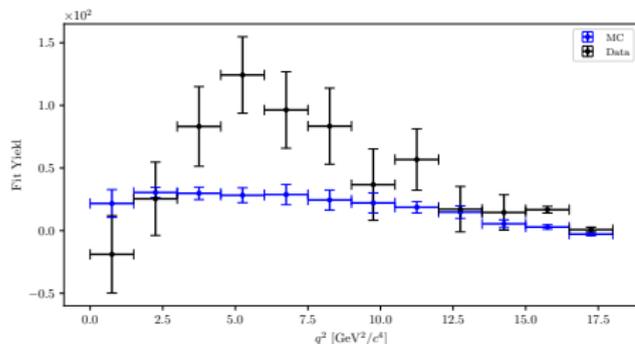
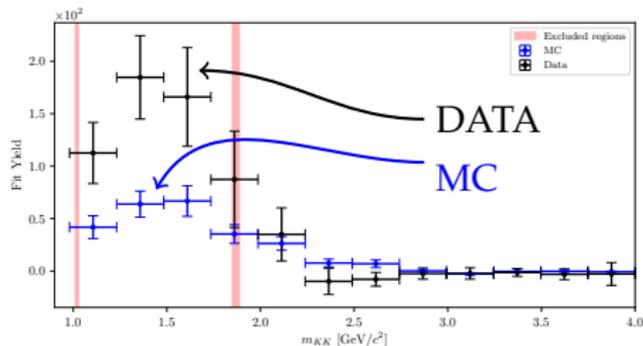
Parameter Extraction III – Signal Fit Results

Signal fit to measured data and 10 equal samples of simulated data (streams)



Much more signal in measured data than expected from simulation!

Parameter Extraction IV – Signal Distributions



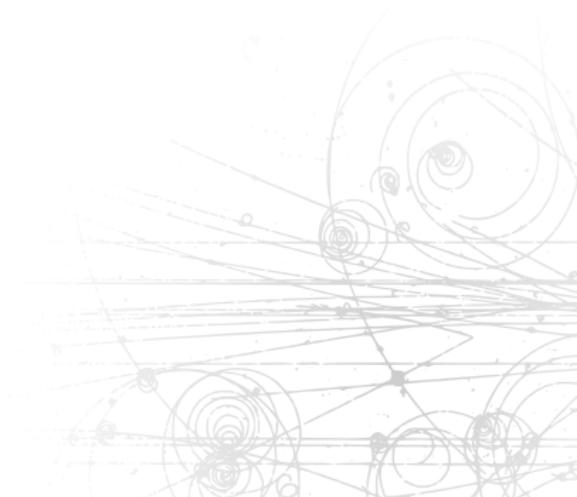
- Invariant mass of two kaons
- Distributions are similar
- Signal much more abundant in DATA

- q is the 4-momentum transferred to the lepton pair
- Distributions are quite different
- Signal much more abundant in DATA

Such measurements help improve future models and minimize difference between data and simulations.

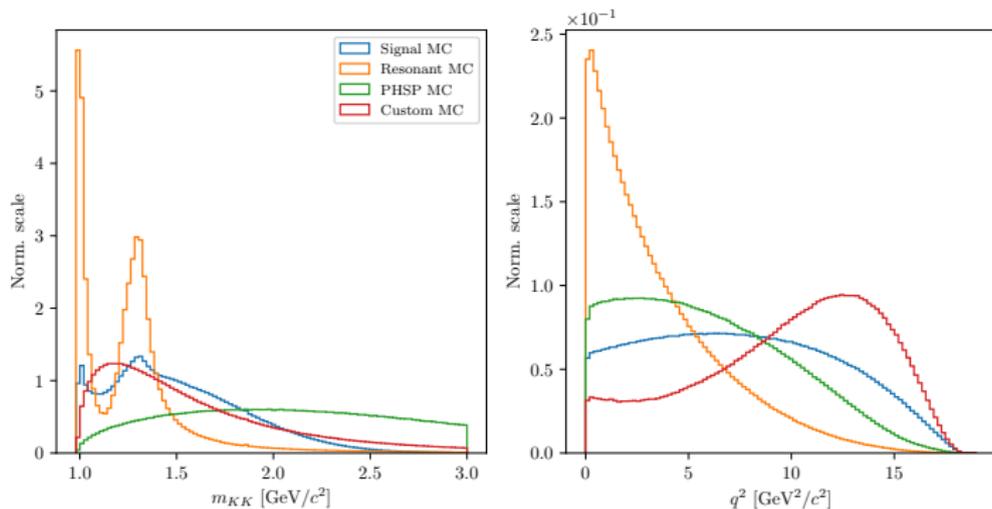
Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup
- 4 Analysis Procedure
- 5 Parameter Extraction
- 6 Systematic Uncertainties**
- 7 Results

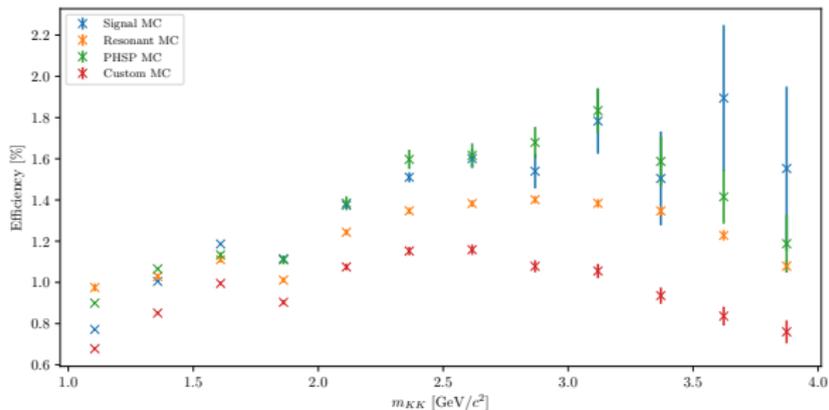
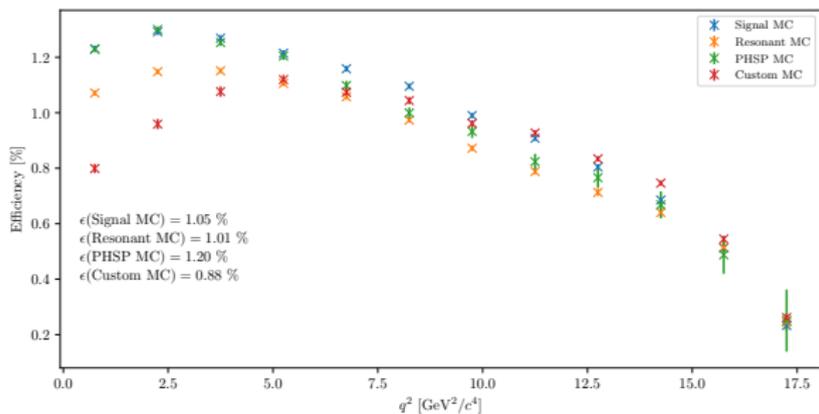


Systematic Uncertainties I – Model Dependency

- Largest source of uncertainty in this analysis
- ISGW2 model for signal decay is not the most reliable, try to not depend on it
- Three additional signal models are used to estimate dependency, used as substitute templates
- Different models have different signal efficiencies



Systematic Uncertainties I – Model Dependency

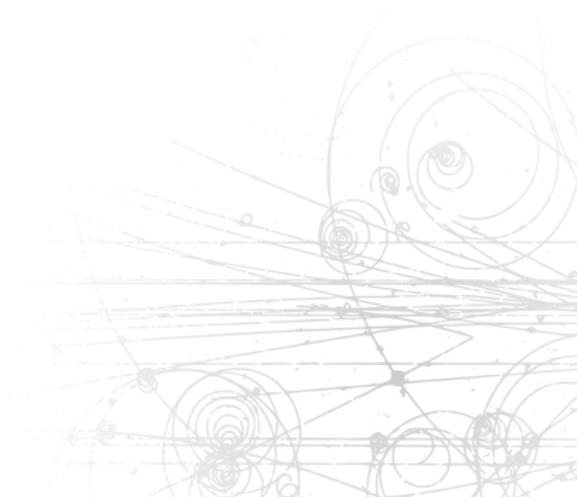


Systematic Uncertainties II – All Sources

Source	Absolute (σ)	Relative (δ) [%]
PID	10	2.0
Fit Bias	+7 -10	+1.5 -2.0
Gaussian Constraints	26	5.4
Template Smearing	+41 -33	+8.3 -6.7
Template Offset	+41 -31	+8.4 -6.3
Finite MC Effects	26	5.3
MVA Selection	5	1.0
Model Shape	+45 -39	+9.3 -8.0
Model Efficiency	+70 -79	+14.3 -16.2
Total	+109 -107	+22.2 -21.9

Overview

- 1 Introduction
- 2 Motivation
- 3 Experimental Setup
- 4 Analysis Procedure
- 5 Parameter Extraction
- 6 Systematic Uncertainties
- 7 Results**



Results I – Branching Ratio of Signal Decay

Calculated branching ratio from simulated data is:

$$\mathcal{B}^{\text{MC}}(B^+ \rightarrow K^+ K^- \ell^+ \nu) = (1.55 \pm 0.15) \times 10^{-5},$$

And on data, after taking all uncertainties into account:

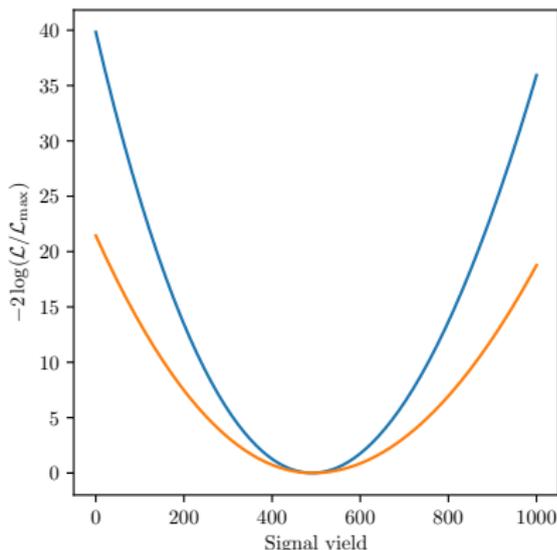
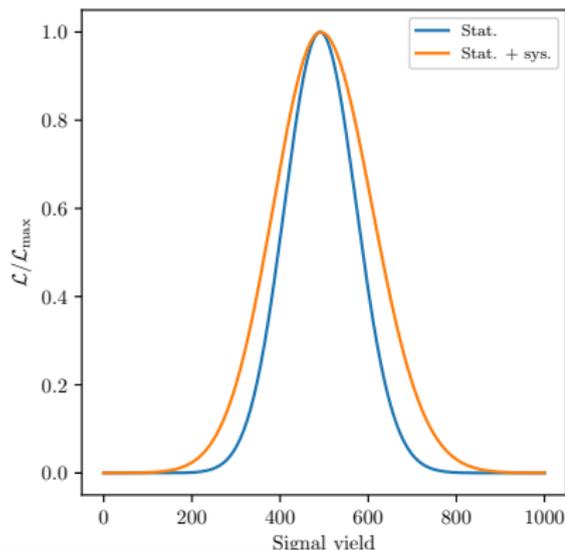
$$\mathcal{B}(B^+ \rightarrow K^+ K^- \ell^+ \nu) = (3.04 \pm 0.51 \pm_{-0.66}^{+0.67}) \times 10^{-5},$$

where the first and the last error are statistical and systematic, respectively.

Almost a factor of 2 difference!

Results II – Signal Significance

- Profile likelihood gives the value of likelihood at different expected yields of signal, used for significance estimation
- Statistical significance corresponds to 6.3σ
- Systematic uncertainties are incorporated via a convolution
- Overall signal significance $4.6\sigma \rightarrow$ evidence!



Summary

- Improvement in the untagged method with the ROE clean-up
- Demonstration of the aid of machine learning algorithms in such analyses
- Evidence for the previously unstudied decay mode $B^+ \rightarrow K^+ K^- \ell^+ \nu_\ell$ (and c.c.), with additional insight into signal distributions
- Current studies underestimate the amount of charmless semileptonic B meson decays with kaons in the final state. Future analyses can take such decay modes into account and produce more quantitative results.

Thank you!



THE BEST THESIS DEFENSE IS A GOOD THESIS OFFENSE.

<https://xkcd.com/1403/>

BACKUP

Backup – Selection Criteria

Selection:

- FSP particles:
 - electrons: $|d_0| < 0.1 \text{ cm}$, $|z_0| < 1.5 \text{ cm}$, $p > 0.6 \text{ GeV}/c$, $p_{CMS} \in [0.4, 2.6] \text{ GeV}/c$, $eID > 0.9$,
 - muons:
 $|d_0| < 0.1 \text{ cm}$, $|z_0| < 1.5 \text{ cm}$, $p_{CMS} \in [0.6, 2.6] \text{ GeV}/c$, $\mu ID > 0.97$,
 - kaons: $|d_0| < 0.15 \text{ cm}$, $|z_0| < 1.5 \text{ cm}$, $p_{CMS} < 2.5 \text{ GeV}/c$, $K/\pi ID > 0.6$, $K/p ID > 0.1$,
- B meson candidates:
 - standard selection:
 $P(\chi^2, DOF) > 6 \times 10^{-3}$, $|\cos \theta_{BY}| < 1.05$, $|m_{miss}^2| < 0.975 \text{ GeV}/c^2$,
 - fit region selection:
 $\Delta E \in [-1.0, 1.3] \text{ GeV}$, $M_{BC} \in [5.1, 5.295] \text{ GeV}/c^2$,
 - signal region selection: $|\Delta E| < 0.126 \text{ GeV}$, $M_{BC} > 5.271 \text{ GeV}/c^2$,
 - charge categorization: $q_{B\pm} q_{B\mp} = -1$.

Backup – Generated m_{KK} Distribution

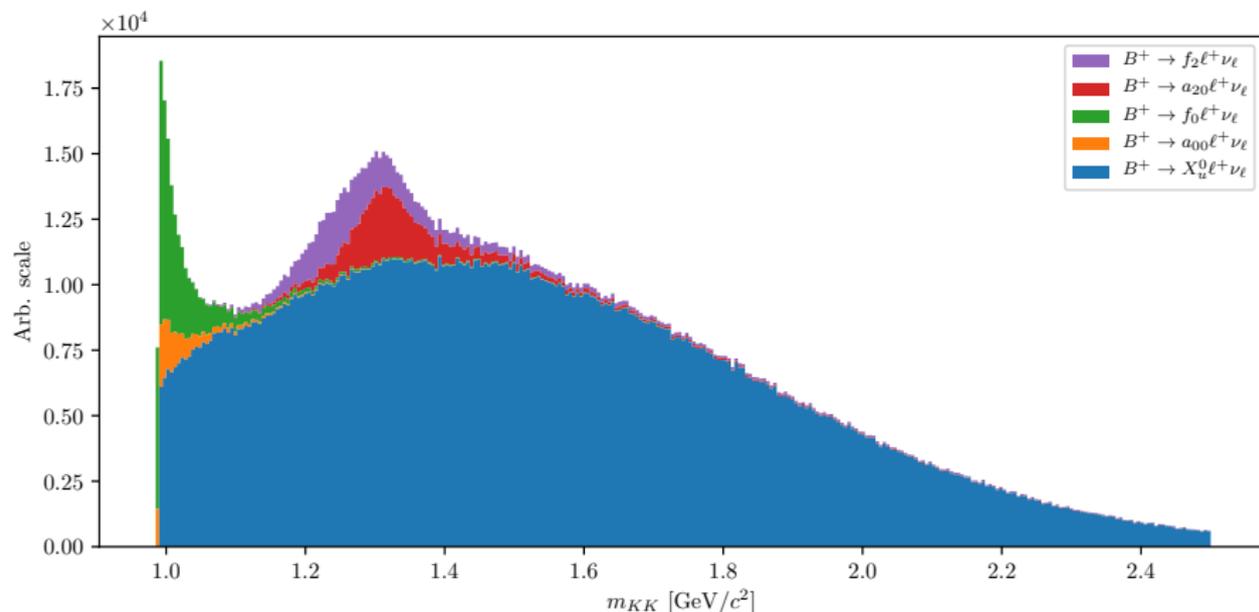


Figure: Invariant mass of the KK pair from various contributions of the MC generator. The light unflavored states have small contributions with resonant structure, while KK pairs from the X_u^0 state are more abundant and follow a wider and smoother distribution.

Backup – Other KK decays

Channel	Ratio [%]	Channel	Ratio [%]
K^+K^-	28.14	$K^+K^-\rho^0$	1.93
$K^+K^-\pi^0$	8.94	$K^+\bar{K}^0\rho^-$	1.84
$K^+\bar{K}^0\pi^-$	8.71	$K^0K^-\rho^+$	1.83
$K^0K^-\pi^+$	8.70	$K^0\bar{K}^0\rho^0$	0.00
$K^+K^-\pi^+\pi^-$	4.15	$K^+K^-\pi^0\pi^0$	0.86
$K^0\bar{K}^0$	3.32	$K^+K^-\pi^+\rho^-$	0.69
$K^0\bar{K}^0\pi^0$	3.26	$K^+K^-\rho^+\pi^-$	0.68
$K\bar{K}$ pair with η	7.08		
$K\bar{K}$ pair with ω	5.33		
Other	14.53		

Table: Relative branching fractions of $B \rightarrow KKXl\nu$ decays by channel.

Backup – B2BII Tracks

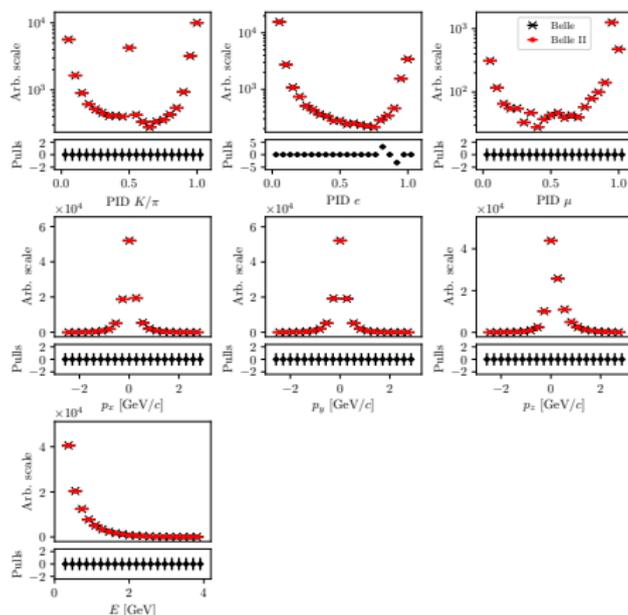
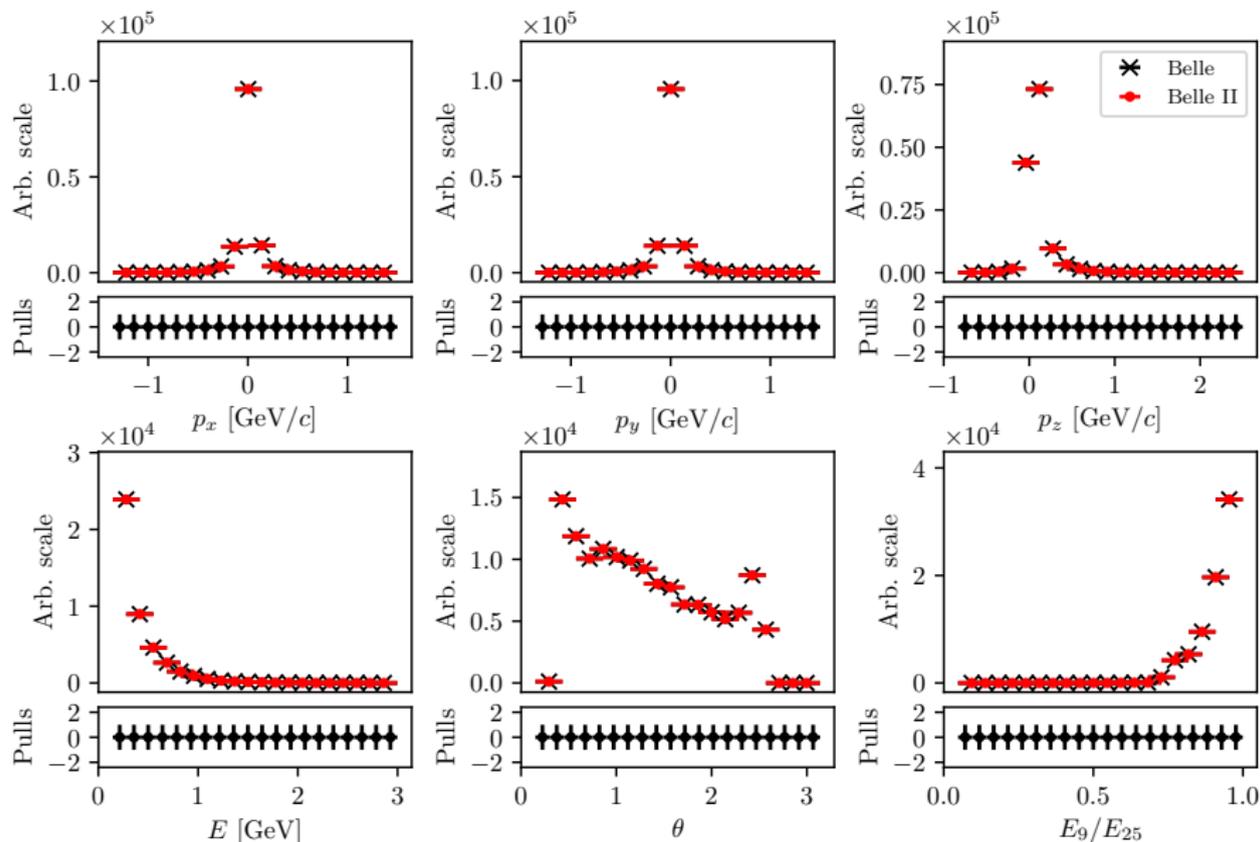


Figure: Some of the more important physical properties of tracks for Belle and Belle II in the conversion process. The histograms seem to overlap and the conversion is assumed to be successful.

Backup – B2BII Clusters



Backup – q^2 Calculation

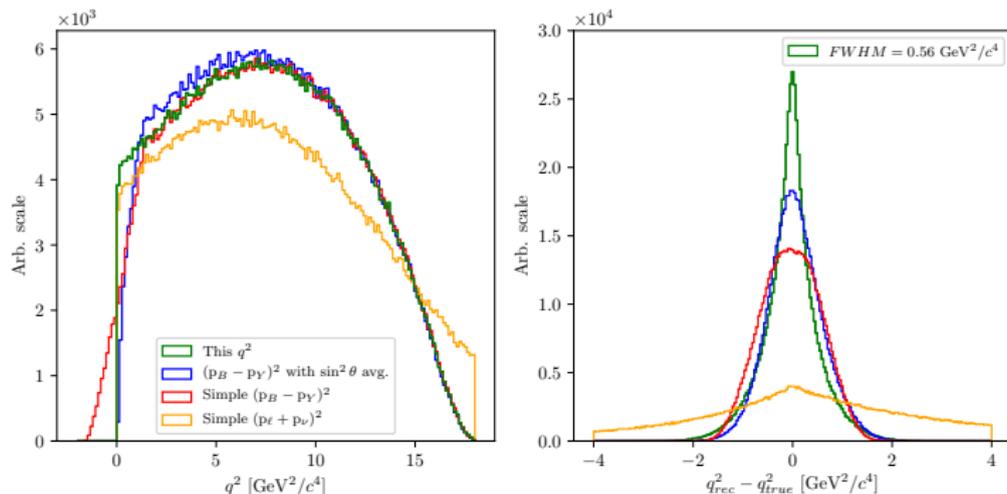


Figure: Distributions of q^2 (left) and q^2 resolution (right) for various methods of q^2 calculation. The green distribution follows the procedure in [1], the blue distribution takes into account the weighted average of the B meson direction [2], and the red and orange distributions are straight-forward calculations with available information in the reconstruction. The q^2 calculation in red assumes a resting B meson in the CMS frame, and the calculation in orange uses the neutrino four-momentum summed up tracks and clusters in ROE.

Backup – Signal Window Definition

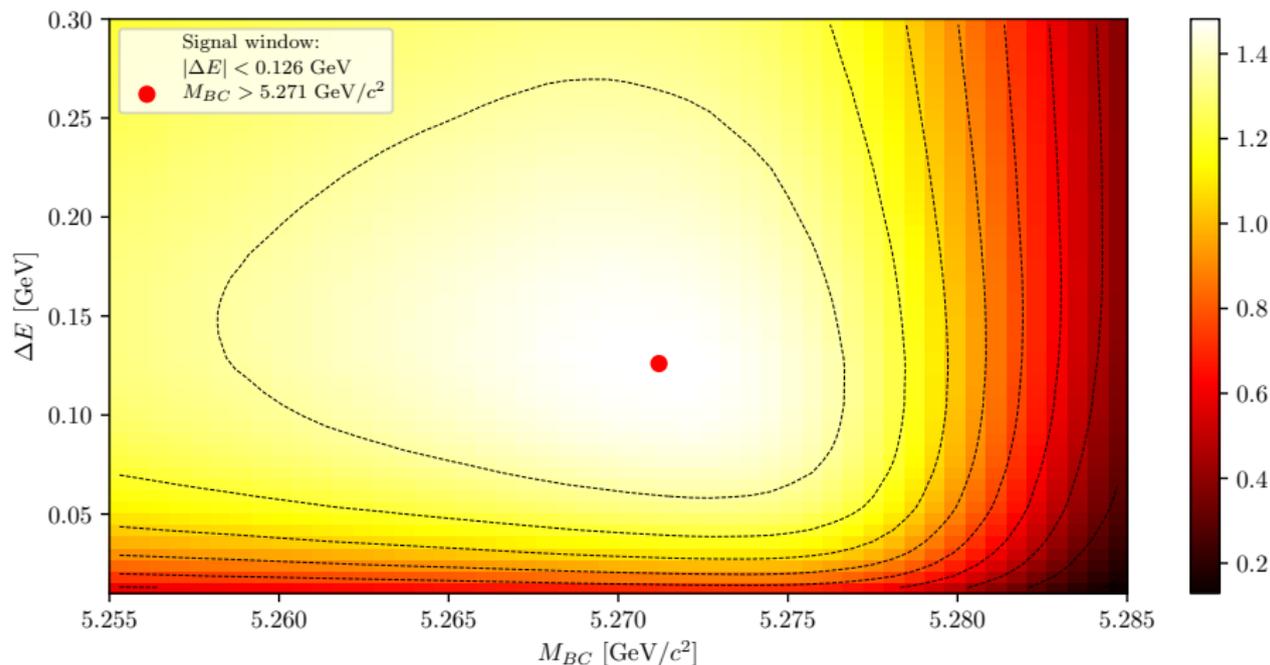


Figure: 2D FOM optimization of the signal region definition, where most of the perfectly reconstructed candidates are located.

Backup – ROE Clean-up Validation (Split)

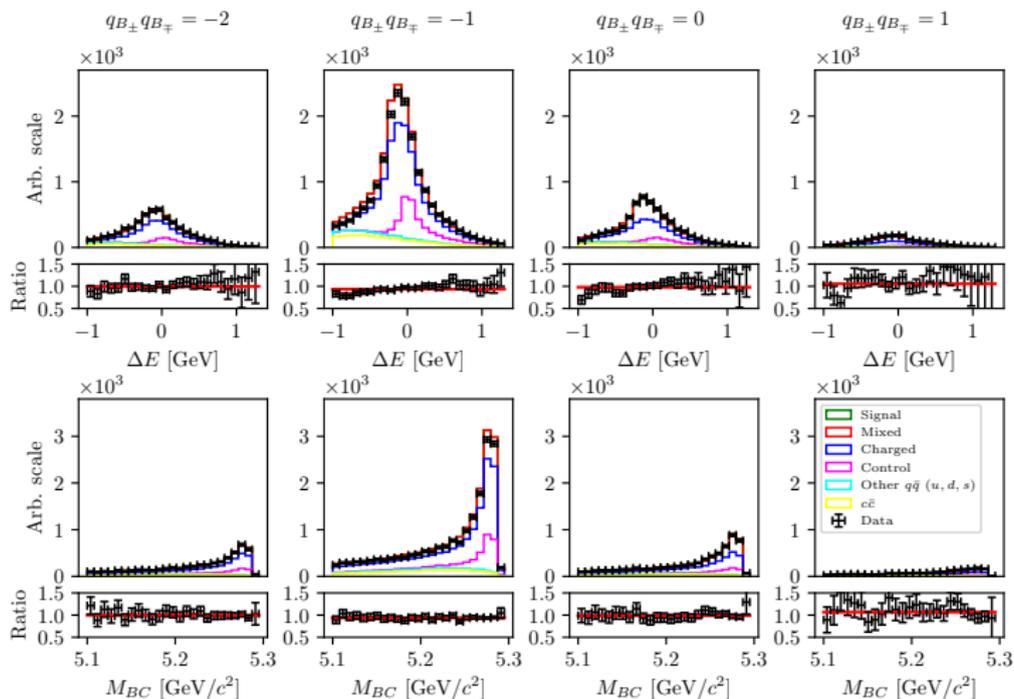


Figure: Distributions of ΔE (top) and M_{BC} (bottom) split in bins of the charge product of the two B mesons.

Backup – BDT for $B\bar{B}$ Suppression

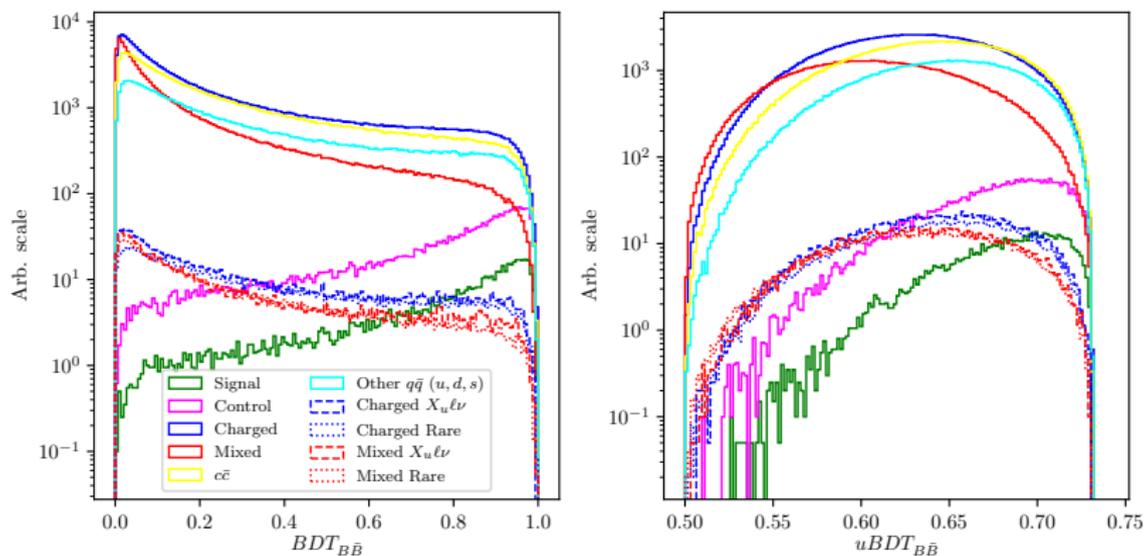


Figure: $B\bar{B}$ suppression classifier output for signal and various types of background for the standard BDT classifier (left) and the $uBDT$ classifier (right). B candidates from $B\bar{B}$ background events dominate the lower region, while signal and control candidates dominate in the upper region of the classifier output.

Backup – $B\bar{B}$ BKG Composition

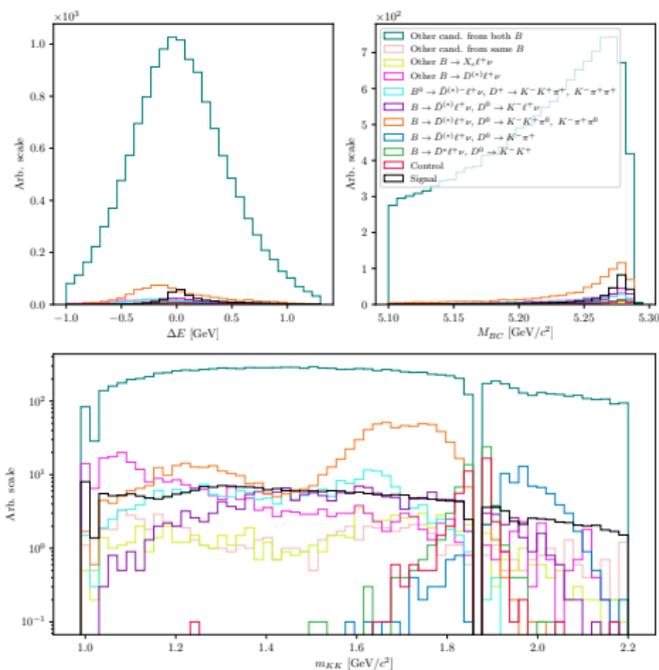


Figure: ΔE (left), M_{BC} (right) and m_{KK} (bottom) for major contributions to the $B\bar{B}$ background in the signal region after the lepton veto. The double semileptonic background component is suppressed by a factor of 4 – 5.

Backup – Off Resonance Agreement

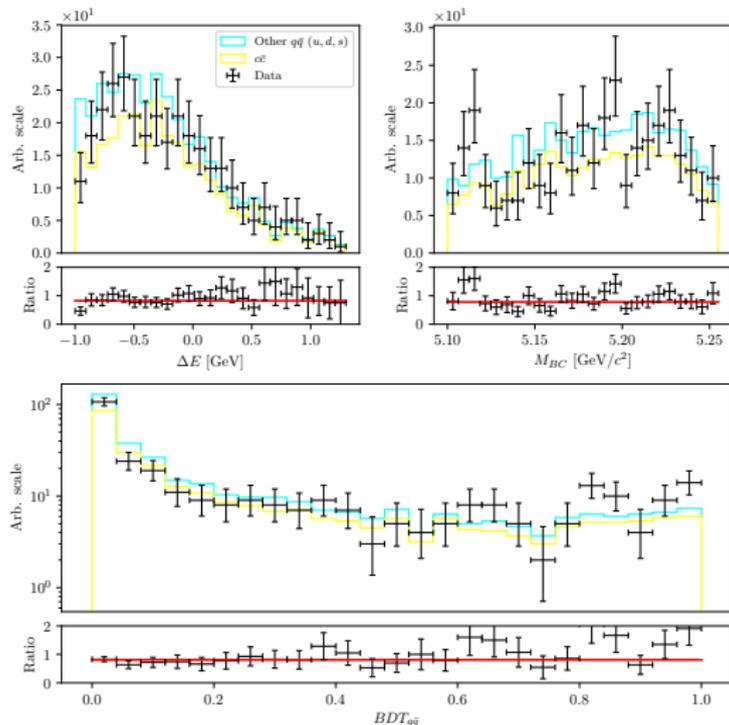


Figure: ΔE (left), M_{BC} (right), and the $q\bar{q}$ classifier output (bottom) for off-resonance data and MC in the control region prior to any MVA selection.

Backup – Binning Algorithm

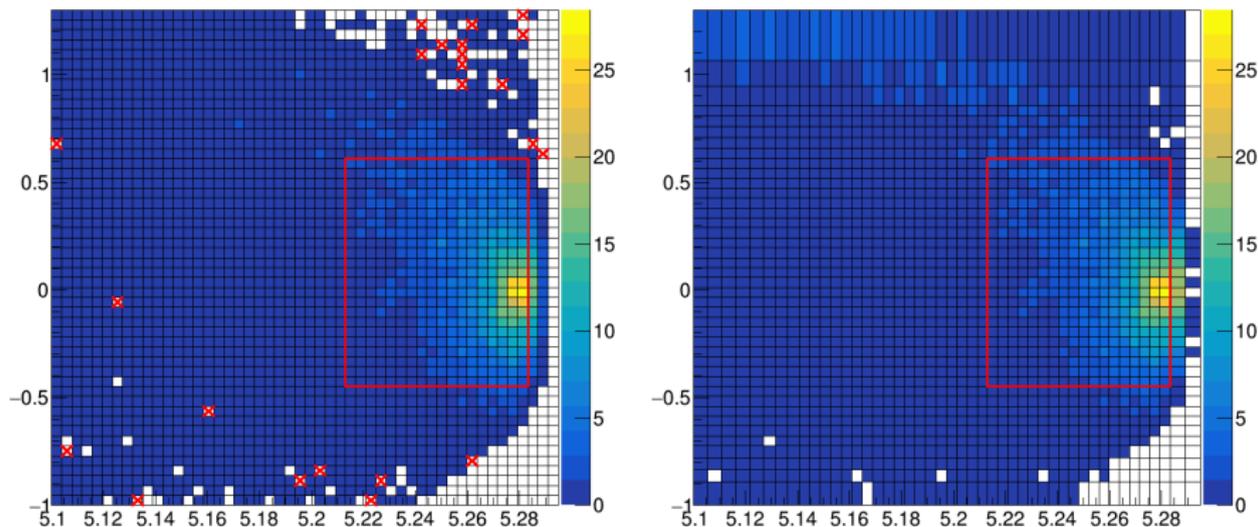


Figure: Steps taken in the adaptive binning algorithm. Left image shows the initial 2D histogram with the defined optimal region and the problematic bins, the right image shows the final binning with the unchanged optimal region, while the problematic bins are gone due to the new binning choice.

Backup – Linearity Test

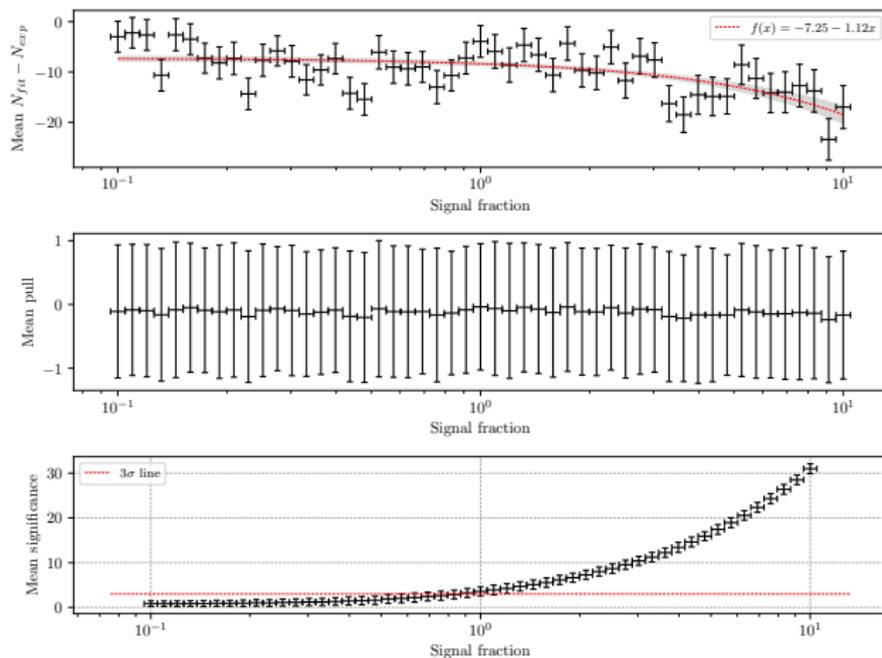
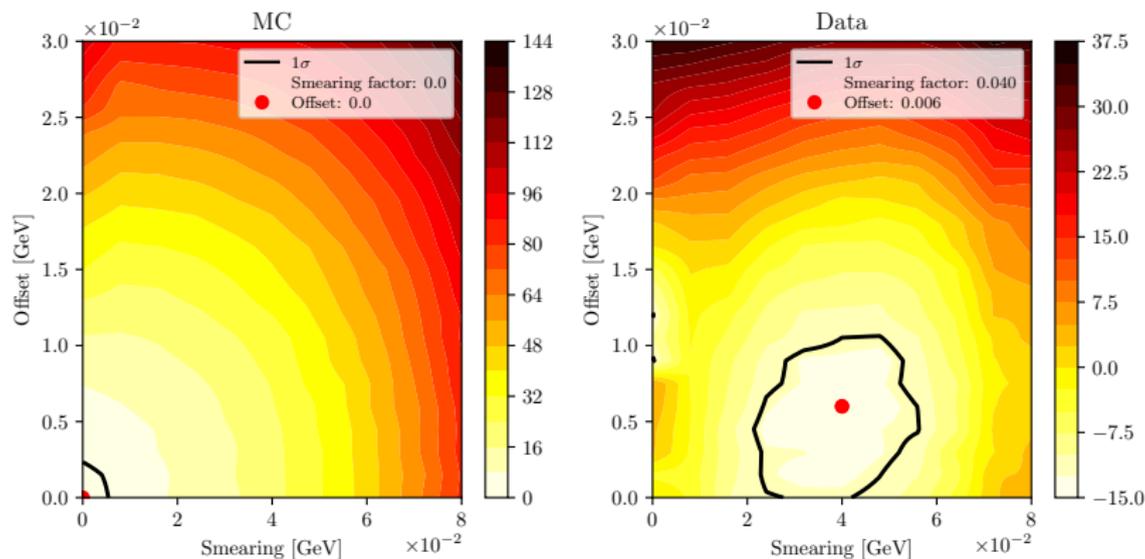


Figure: The mean fit yield and expected yield difference (top), the mean pull (center) and the mean significance (bottom) as a function of the signal fraction.

Backup – Smearing and Offset

We introduced 2 additional parameters to the ΔE variable:

$$f_{\text{offset}} : x \mapsto x + a, \quad f_{\text{smearing}} : x \mapsto \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}},$$



Consistency check on MC, data fit better with introduced parameters:
Smearing: 40_{-17}^{+15} MeV, Offset: $6_{-6}^{+4.6}$ MeV.



D. M. Asner, K. W. Edwards, and others. “Study of exclusive charmless semileptonic B decays and extraction of $|V_{ub}|$ at CLEO”. In: *Phys. Rev. D* 76 (1 July 2007), p. 012007. DOI: [10.1103/PhysRevD.76.012007](https://doi.org/10.1103/PhysRevD.76.012007). URL: <https://link.aps.org/doi/10.1103/PhysRevD.76.012007>.



H. Ha et al. “Measurement of the decay $B^0 \rightarrow \pi^- \ell^+ \nu$ and determination of $|V_{ub}|$ ”. In: *Phys. Rev. D* 83 (2011), p. 071101. DOI: [10.1103/PhysRevD.83.071101](https://doi.org/10.1103/PhysRevD.83.071101). arXiv: 1012.0090 [hep-ex].