

Where did anti-matter go?

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Contents

- What happened to the anti-matter?
- How to measure CP violation?
- The SuperKEKB / Belle II project
- Status and outlook



Open questions of particle physics (and cosmology)

- Why is the Universe predominantly made of matter, and of very little anti-matter?
 - Measure violation of the CP symmetry between particles and anti-particles
- What is the origin of mass?
 - Higgs boson search
- Why do particles have different masses, why are there several families of particles, what is dark matter?
 - Searches for new particles (e.g. supersymmetric partners of known particles) and their interactions

Difference between matter and anti-matter

Out of 10 billion particles and 10 billion anti-particles in the early Universe

only 1 particle survived!

10.000.000.000 particles

10.000.000.000 anti-particles

1 particle

0 anti-particle

CP symmetry and its violation

CP symmetry operation: turns a **particle** into its **anti-particle**

If particles and anti-particles behave differently – e.g. if there are differences in their decays → violation of CP symmetry.

Since the early Universe contained the same numbers of particles and anti-particles, while it is today composed only of **matter** (=particles), and no **anti-matter**, this symmetry is obviously **broken!**



Very important to understand why and how this symmetry is broken.

CP symmetry and its violation

1964: Fitch, Cronin and collaborators discover CP symmetry violation for neutral kaons

1973: Kobayashi and Maskawa: formulate a theory on how this symmetry is broken; the theory requires the existence of six quark types. A very daring hypothesis since it was formulated when only three quark types were known!

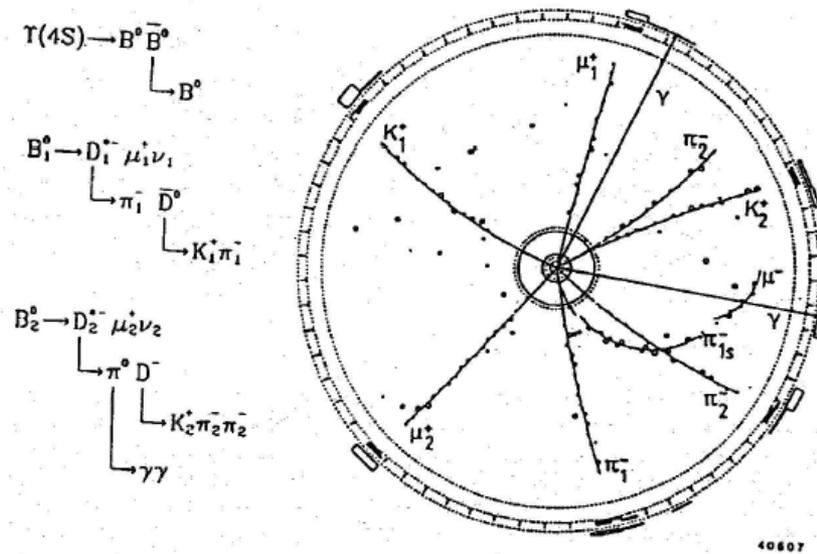
Their theory predicted that there are tight links between CP violation for various particle types, and also tight links to transitions between quark types.

1974, 1977, 1994: 21 years after their theory was published, all missing quarks were found.

However, the decisive proof of CP symmetry violation for these heavier particles only came in the last decade when we measured CP violation in B meson decays.

1987: First important step, discovery of the particle \rightarrow anti-particle transitions for B^0 mesons

1987: ARGUS Collaboration discovers BB mixing: B^0 turns into anti- B^0



Reconstructed event with one $B \rightarrow$ anti- B

Integrated $\Upsilon(4S)$ luminosity 1983-87:
 $103 \text{ pb}^{-1} \sim 110,000 \text{ B pairs}$

(=1/7000 of the Belle data sample...)

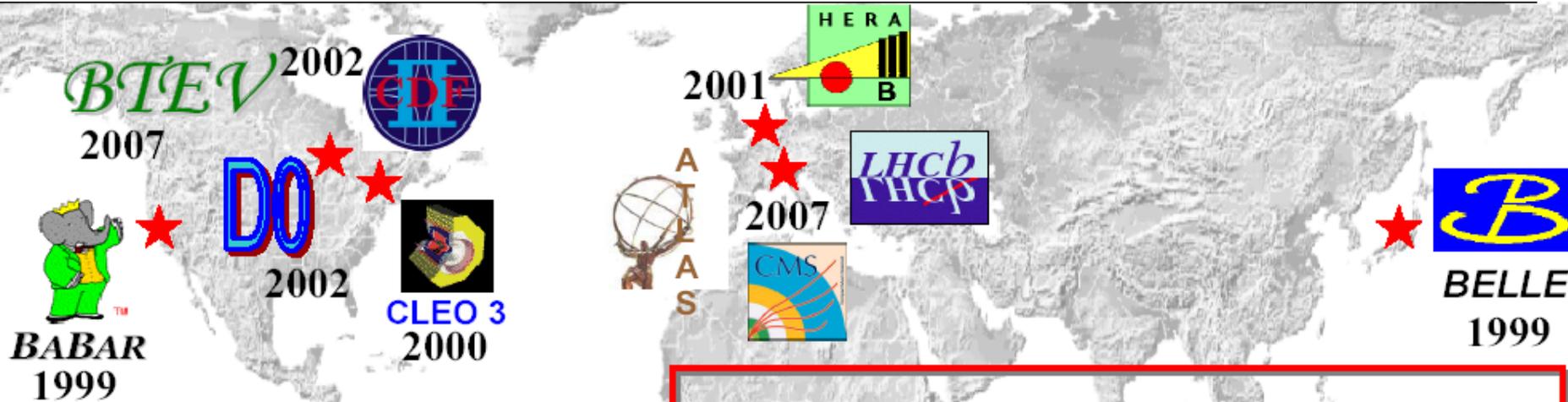
Large mixing in the B^0 system \rightarrow

\rightarrow Top quark is very heavy

\rightarrow CP violation effects could be large in B decays \rightarrow observable

Worldwide effort!

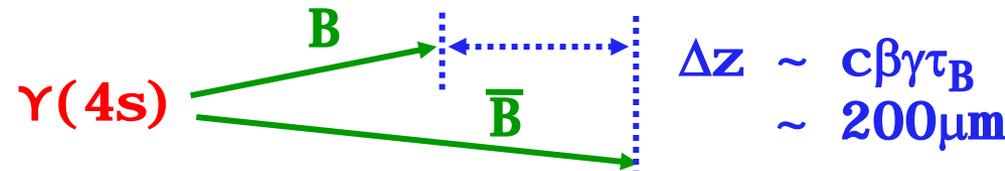
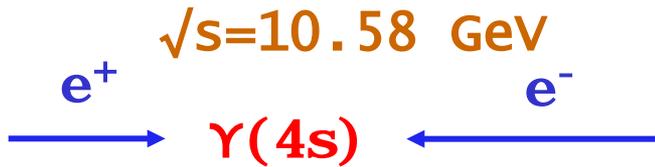
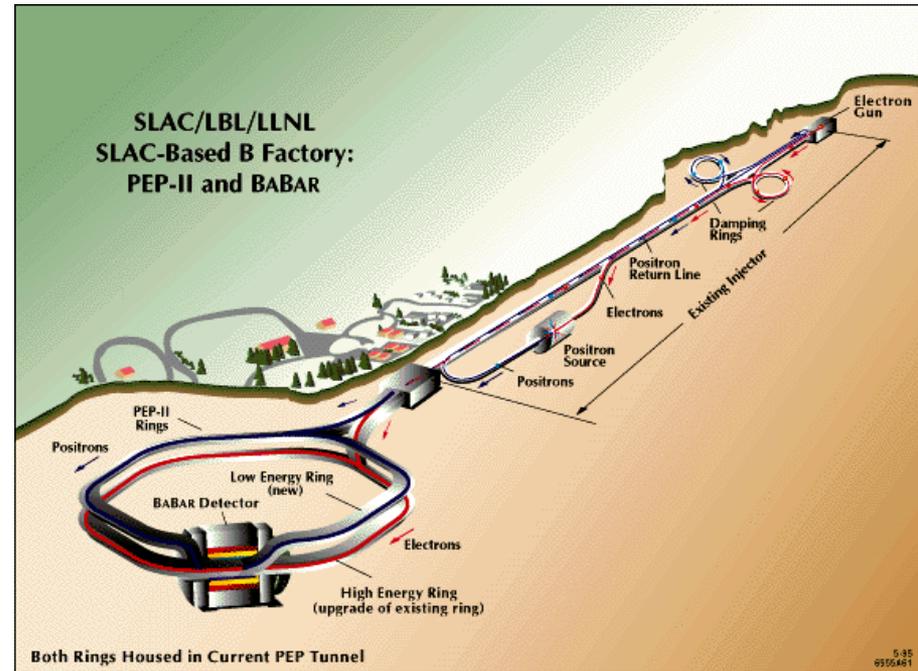
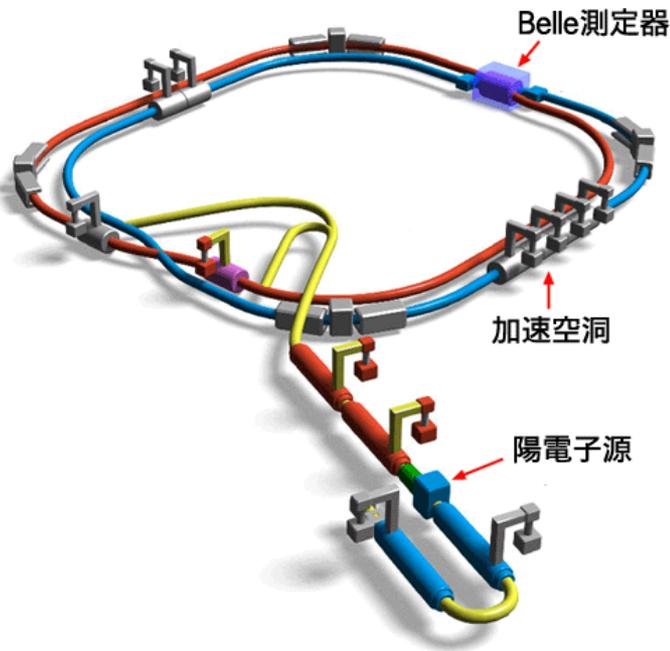
many experiments proposed around 1990, some approved, 2 succeeded...



Primary Goal

Precision measurements of **charged weak interactions** as a test of the **CKM** sector of the Standard Model and a probe of the origin of the **CP** violation

Final winners: asymmetric B factories



BaBar $p(e^-) = 9 \text{ GeV}$ $p(e^+) = 3.1 \text{ GeV}$

$\beta\gamma = 0.56$

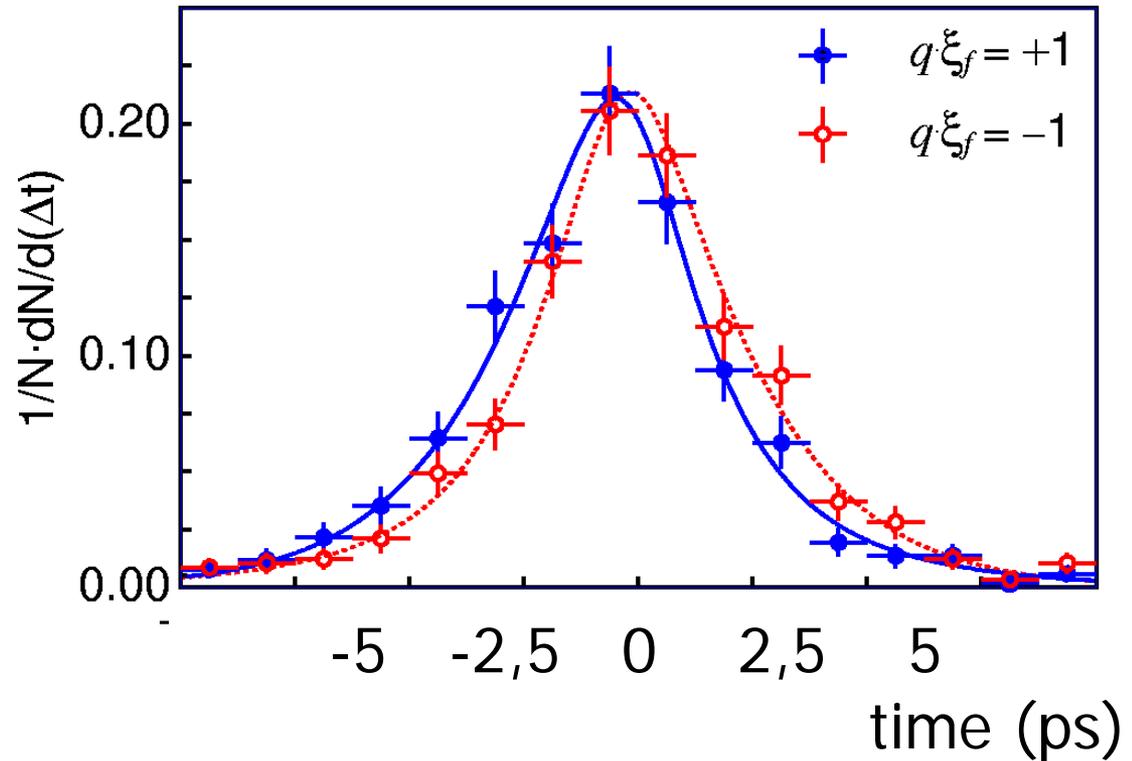
Belle $p(e^-) = 8 \text{ GeV}$ $p(e^+) = 3.5 \text{ GeV}$

$\beta\gamma = 0.42$

Results of our measurements: CP symmetry is violated in the B meson system!

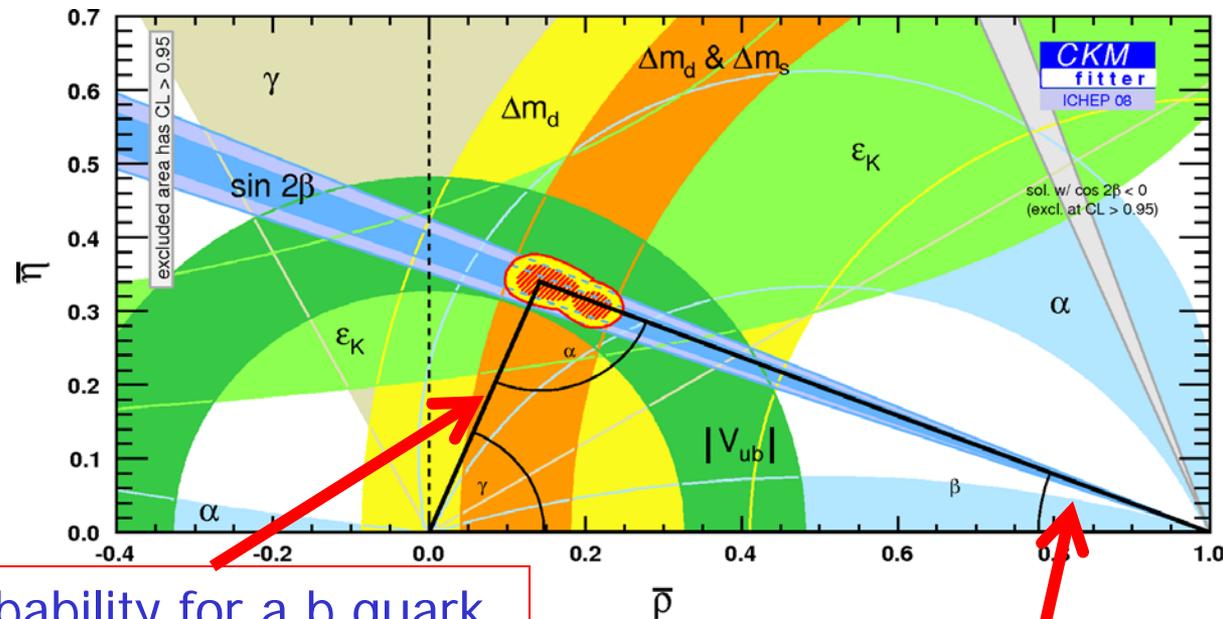
Blue: time dependence of the anti-B decays

Red: same for B decays



Obvious difference between **particles** in **anti-particles!**

All experimental studies combined...



Probability for a b quark to turn into a u quark \rightarrow determines the length of the side V_{ub}

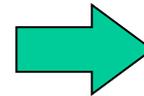
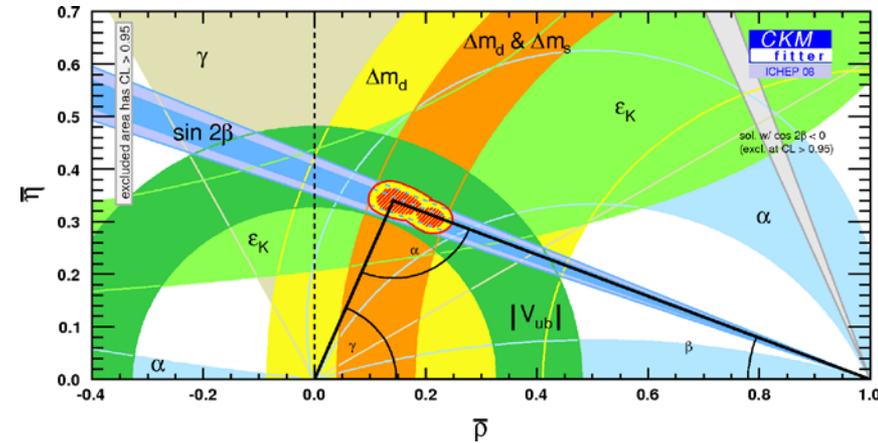
CP asymmetry oscillation amplitude \rightarrow angle $\phi_1 = \beta$

Constraints from measurements of angles and sides of the unitarity triangle

\rightarrow Remarkable agreement

Bold idea of Kobayashi and Maskawa verified by experiment

Relations between parameters as expected in the Standard model →

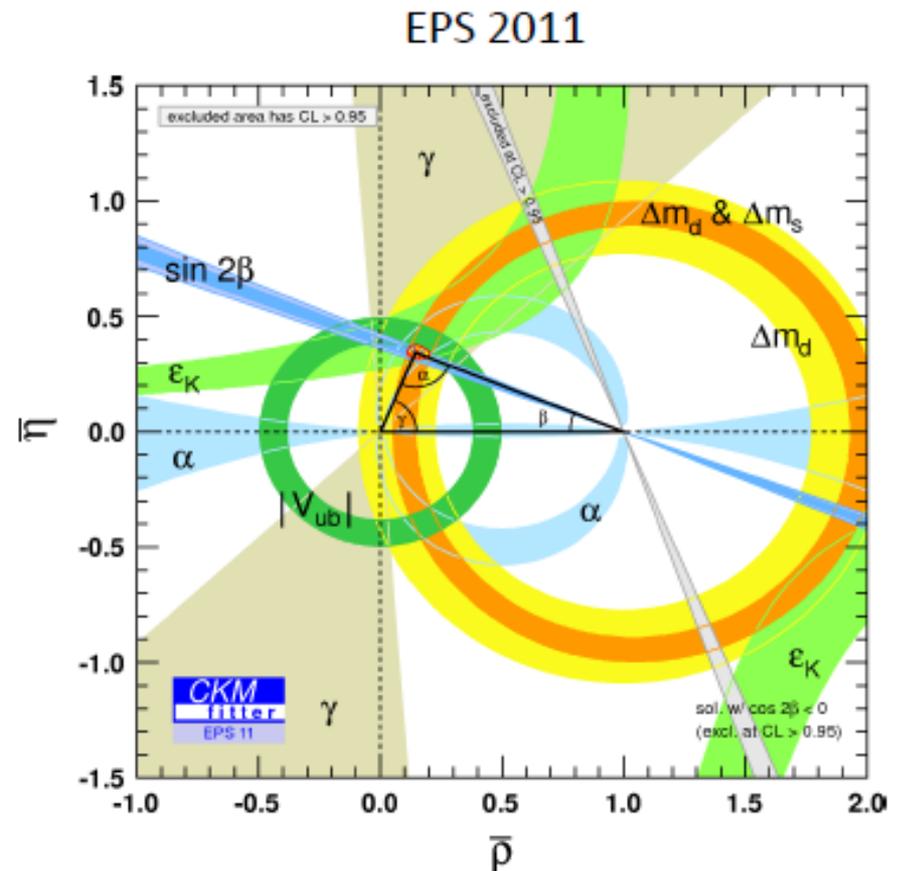
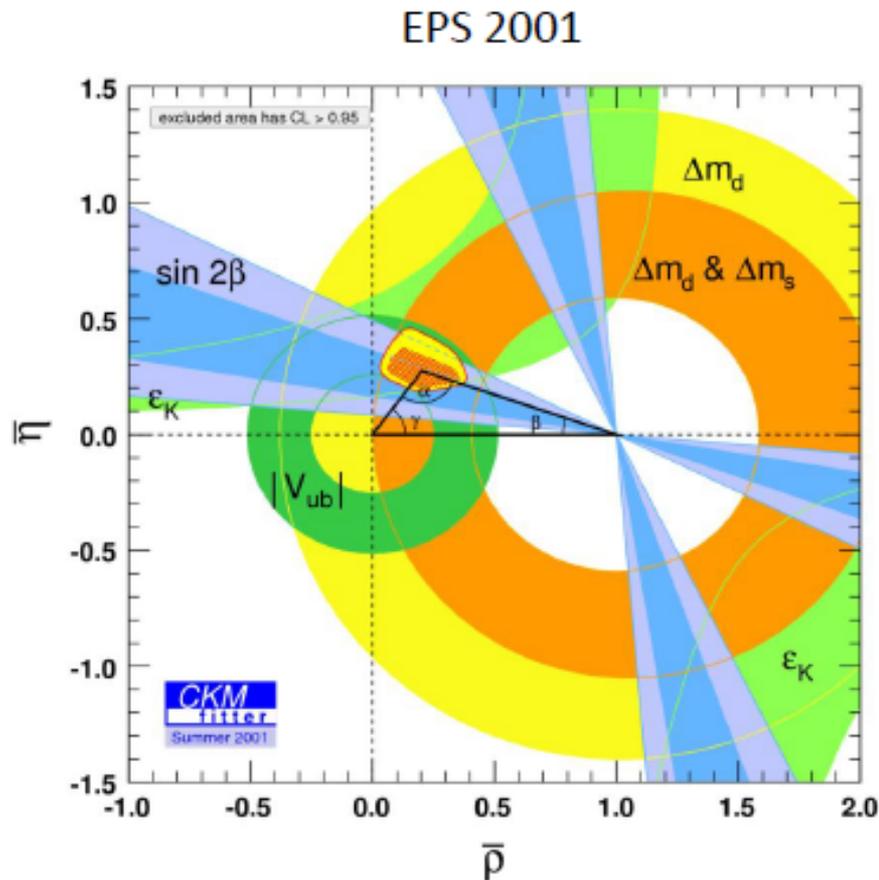


Nobel prize 2008!

→ With essential experimental confirmations by Belle and BaBar! (explicitly noted in the Nobel Prize citation)

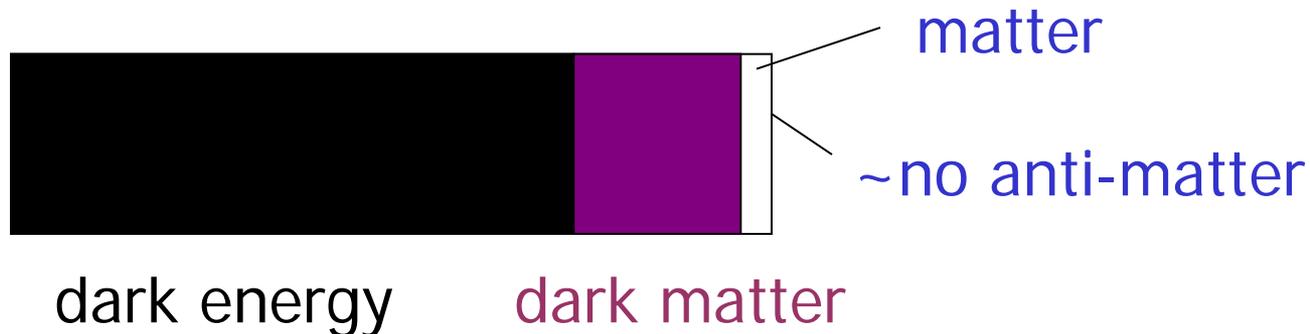
Unitarity triangle – 2011 vs 2001

CP violation in the B system: from the **discovery** (2001) to a **precision measurement** (2011).



The KM scheme is now part of the Standard Model of Particle Physics

- However, the CP violation of the KM mechanism is too small to account for the asymmetry between matter and anti-matter in the Universe (falls short by 10 orders of magnitude !)
- SM does not contain the fourth fundamental interaction, gravitation
- Most of the Universe is made of stuff we do not understand...



Are we done ? (Didn't the B factories accomplish their mission, recognized by the 2008 Nobel Prize in Physics ?)



Из эссе С. Окубо
при большой температуре
для Вселенной суща мучба
но ее кривой фигуре

НАРУШЕНИЕ CP-ИНВАРИАНТНОСТИ, C-АСИММЕТРИЯ
И БАРИОННАЯ АСИММЕТРИЯ ВСЕЛЕННОЙ

А.Д. Сахаров

Теория расширяющейся Вселенной, предполагающая сверхплотное начальное состояние вещества, по-видимому, исключает возможность макроскопического разделения вещества и антивещества; поэтому следует

Matter - anti-matter
asymmetry of the Universe:
KM (Kobayashi-Maskawa)
mechanism still short by 10
orders of magnitude !!!



Two complementary approaches to study shortcomings of the Standard Model and to search for the so far unobserved processes and particles (so called New Physics, NP). These are the **energy frontier** and the **intensity frontier** .

Energy frontier : direct search for production of unknown particles at the highest achievable energies.

Intensity frontier : search for rare processes, deviations between theory predictions and experiments with the ultimate precision.

→ for this kind of studies, one has to investigate a very large number of reactions ("events") → need accelerators with ultimate **intensity** ("luminosity")

Comparison of **energy** / **intensity** frontiers

To observe a large ship far away one can either use **strong binoculars** or observe **carefully the direction and the speed of waves** produced by the vessel.

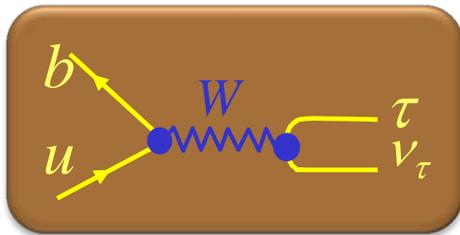
Energy frontier (LHC)



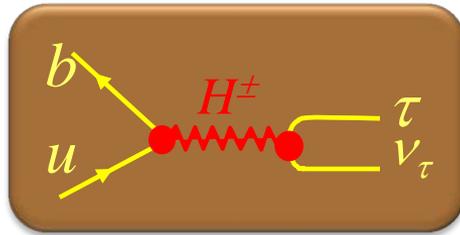
Luminosity frontier (SuperKEKB)

An example: Hunting the **charged Higgs** in the decay $B^- \rightarrow \tau^- \nu_\tau$

In addition to the Standard Model Higgs that was discovered at the LHC, in New Physics (e.g., in supersymmetric theories) there could be another 'God particle' – a **charged Higgs**.



The rare decay $B^- \rightarrow \tau^- \nu_\tau$ is in SM mediated by the **W boson**

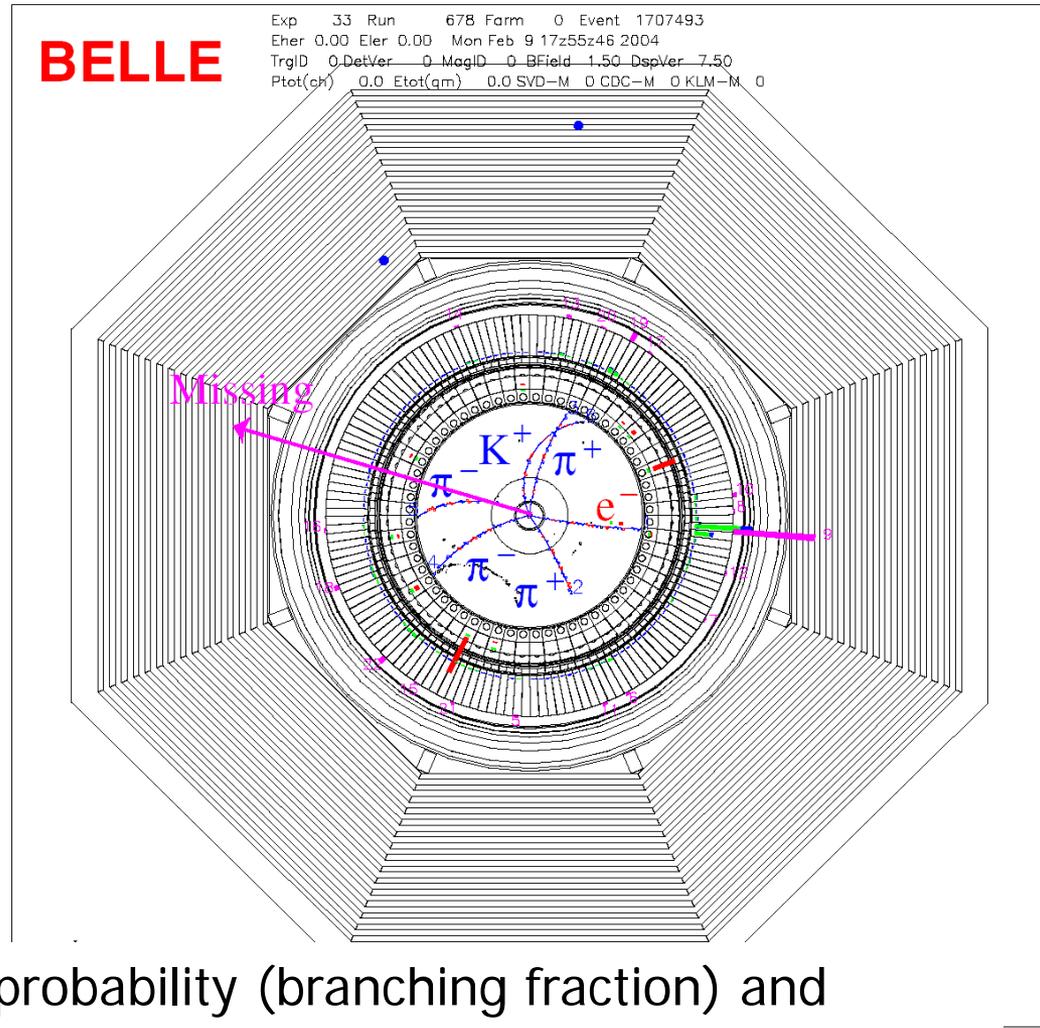


In some supersymmetric extension it can also proceed via a **charged Higgs**

The **charged Higgs** would influence the decay of a B meson to a tau lepton and its neutrino, and modify the probability for this decay.

Missing Energy Decays: $B^- \rightarrow \tau^- \nu_\tau$

$$B^+ \rightarrow D^0 \pi^+ \\ (\rightarrow K \pi^- \pi^+ \pi^-) \\ B^- \rightarrow \tau (\rightarrow e \nu \bar{\nu}) \nu$$

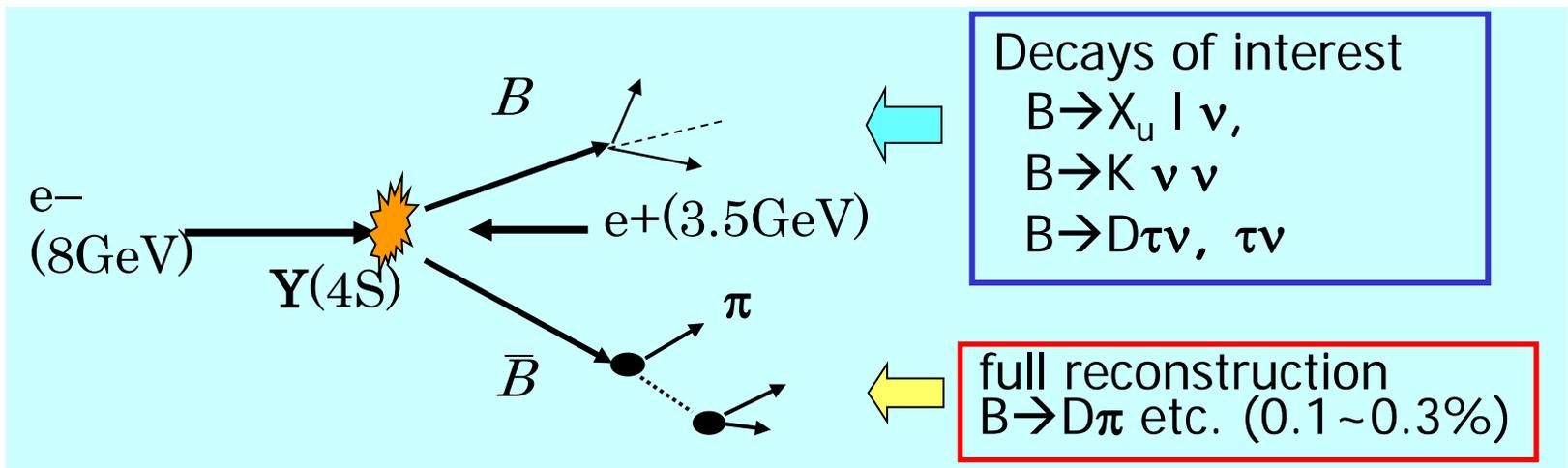


By measuring the decay probability (branching fraction) and comparing it to the SM expectation:

→ Properties of the charged Higgs (e.g. its mass)

Full Reconstruction Method

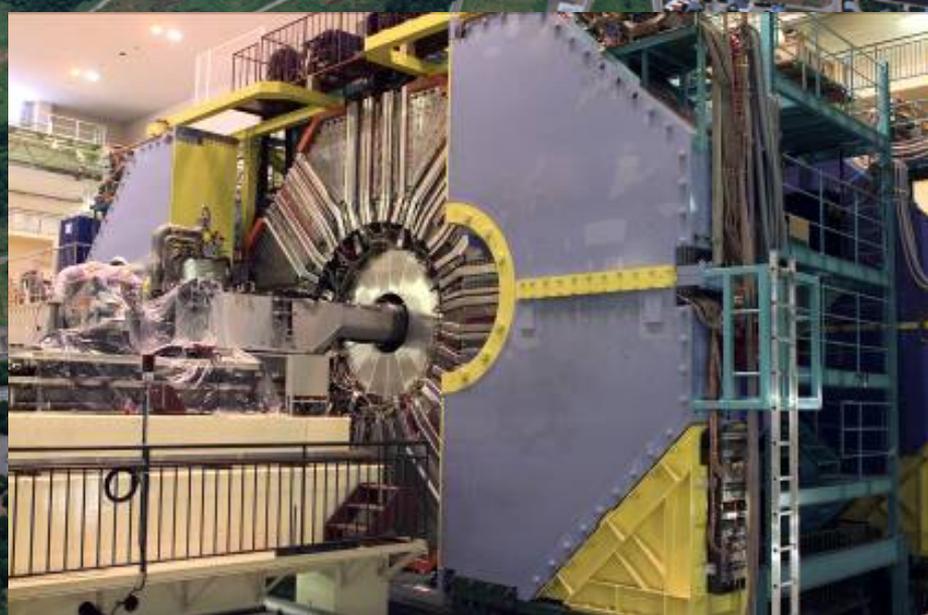
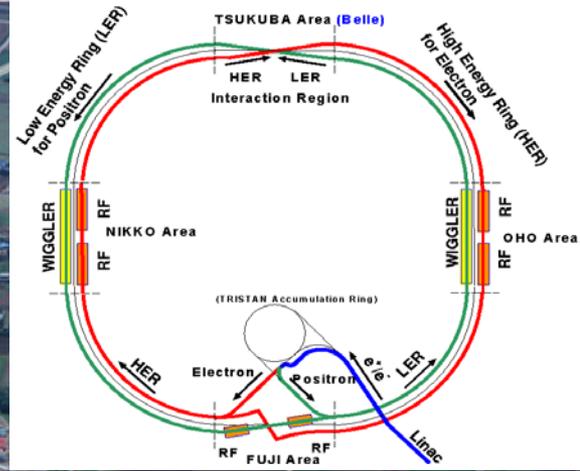
- Fully reconstruct one of the B's to
 - Tag B flavor/charge
 - Determine B momentum
 - Exclude decay products of one B from further analysis



→ Offline B meson beam!

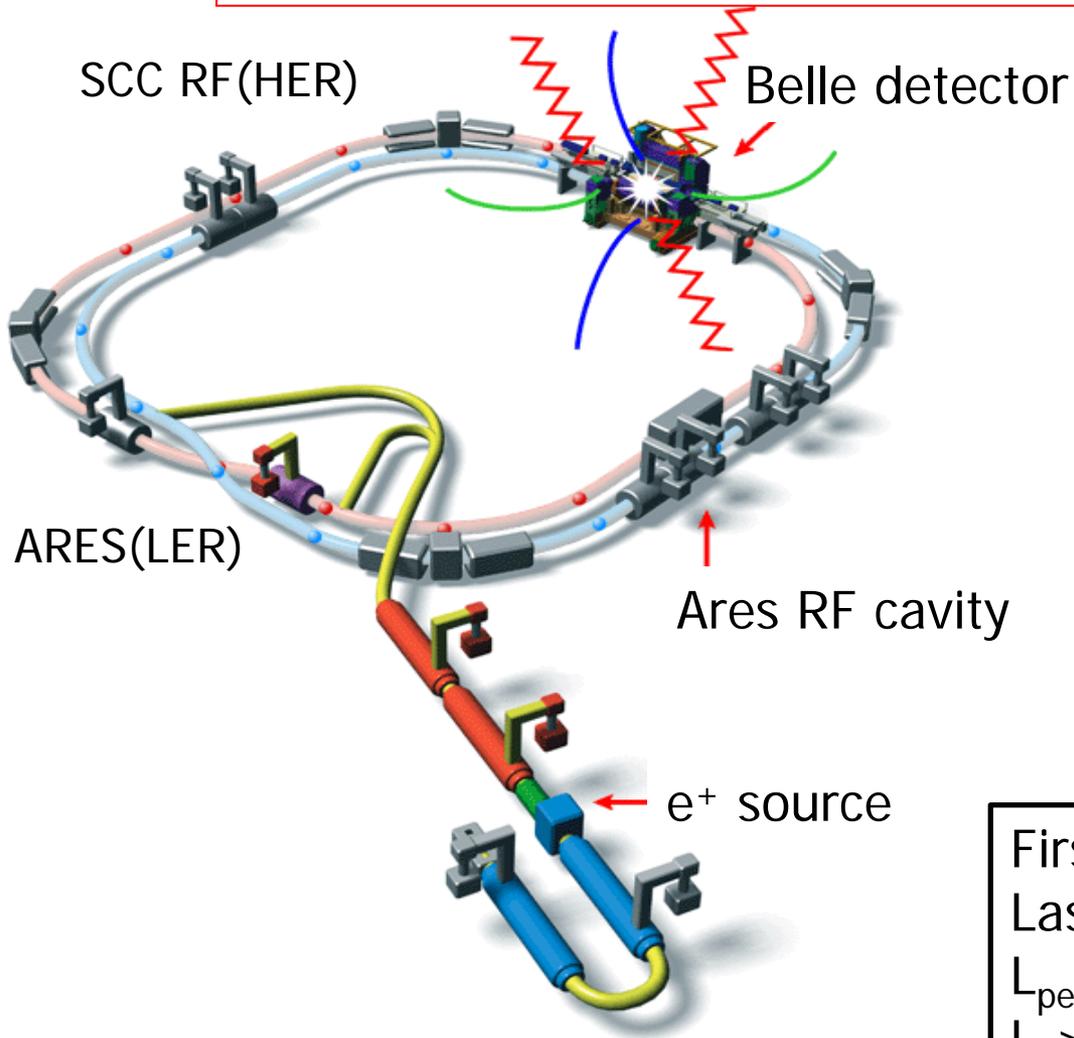
Powerful tool for B decays with neutrinos

How to do it?
→ upgrade KEKB and Belle



The KEKB Collider

Fantastic performance far beyond design values!



- e^- (8 GeV) on e^+ (3.5 GeV)
 - $\sqrt{s} \approx m_{\Upsilon(4S)}$
 - Lorentz boost: $\beta\gamma=0.425$
- 22 mrad crossing angle

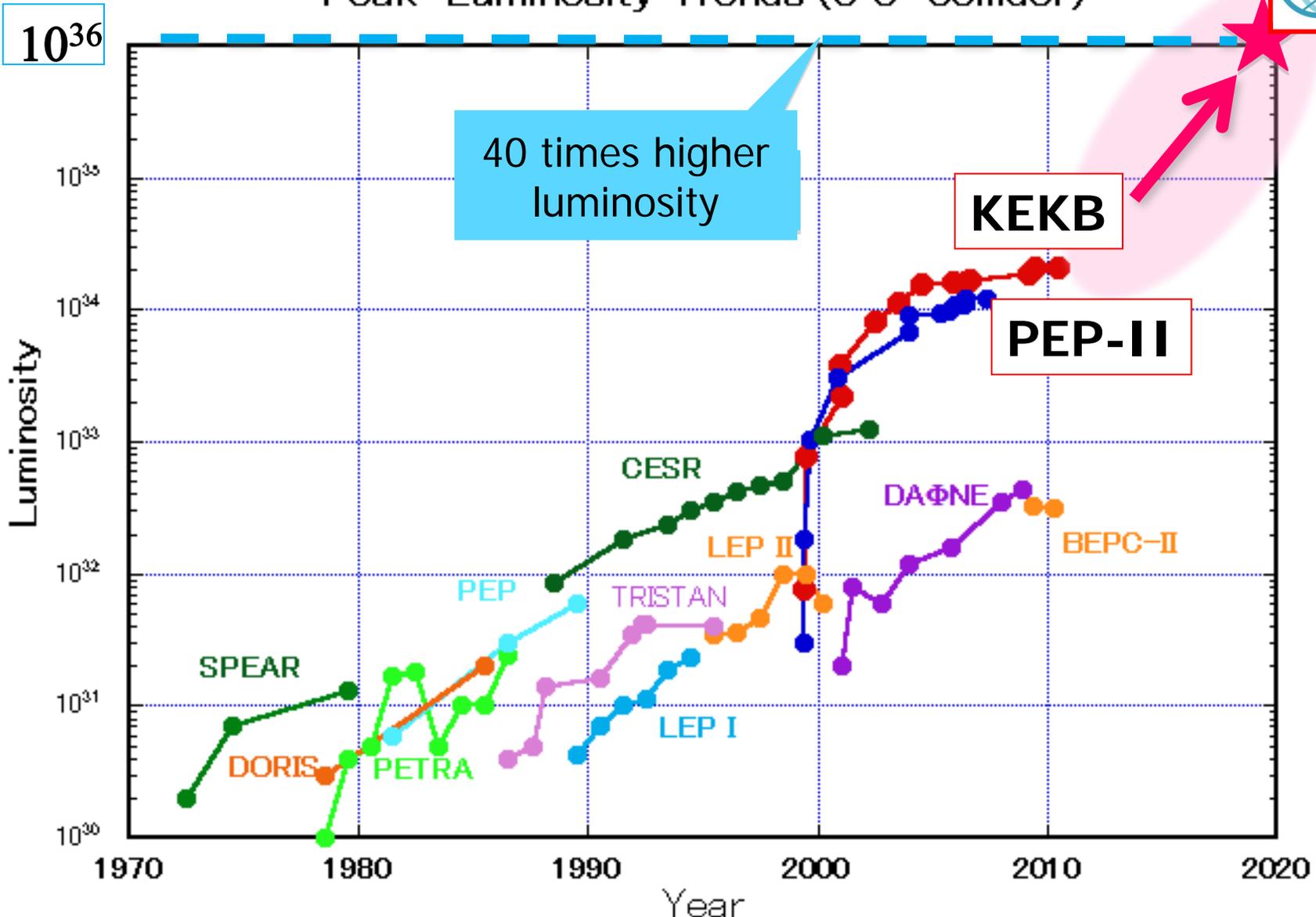
Peak luminosity (WR!) :
 $2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
=2x design value

First physics run on June 2, 1999
Last physics run on June 30, 2010
 $L_{\text{peak}} = 2.1 \times 10^{34} / \text{cm}^2 / \text{s}$
 $L > 1 \text{ ab}^{-1}$

SuperKEKB is the intensity frontier



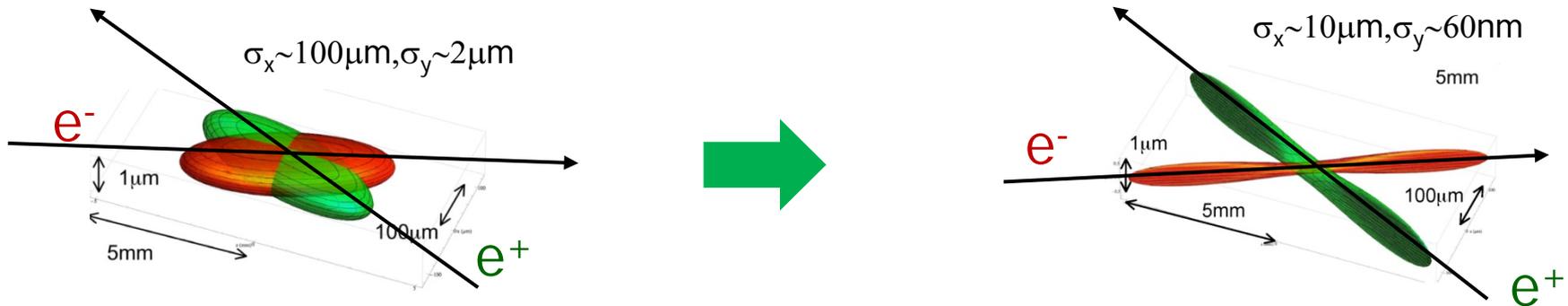
Peak Luminosity Trends (e^+e^- collider)



How big is a nano-beam ?

How to go from an excellent accelerator with world record performance – KEKB – to a 40x times better, more intense facility?

In KEKB, colliding electron and positron beams are **much thinner than the human hair...**

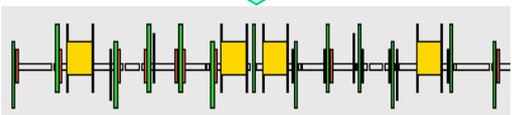


... For a 40x increase in intensity you have to make the beam as thin as **100 atomic layers!**

KEKB to SuperKEKB

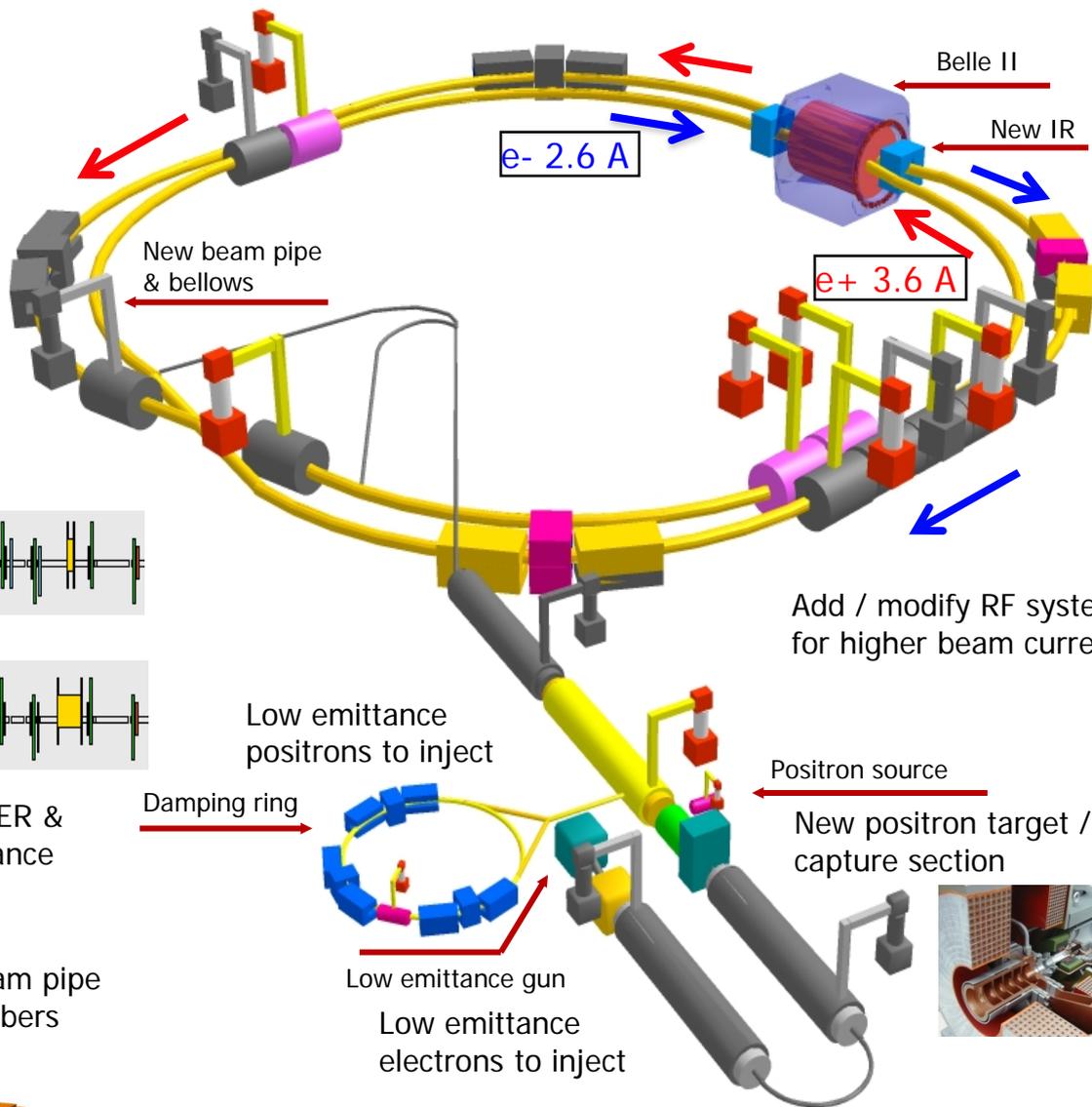
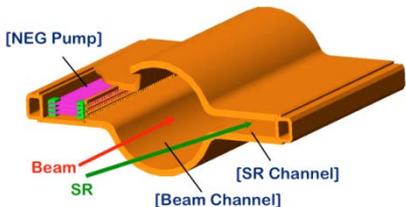


Replace short dipoles with longer ones (LER)



Redesign the lattices of HER & LER to squeeze the emittance

TiN-coated beam pipe with antechambers



Add / modify RF systems for higher beam current

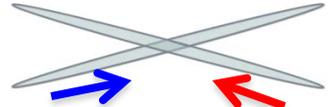
Low emittance positrons to inject

Positron source

New positron target / capture section

Low emittance gun
Low emittance electrons to inject

Colliding bunches



New superconducting / permanent final focusing quads near the IP



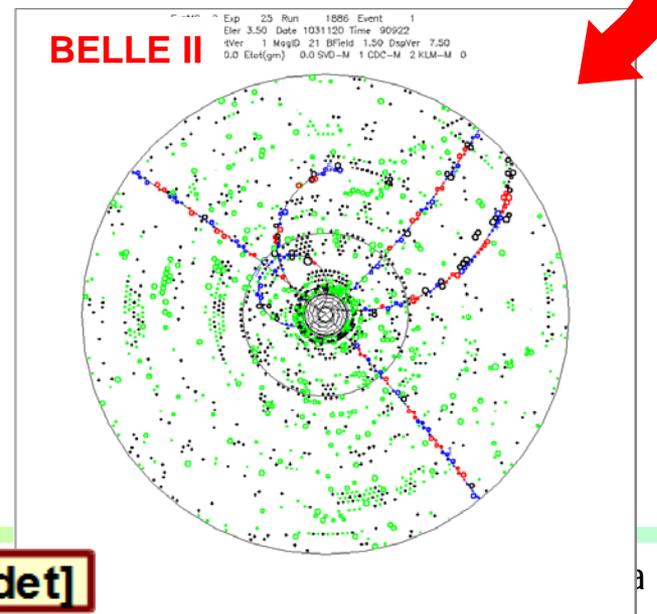
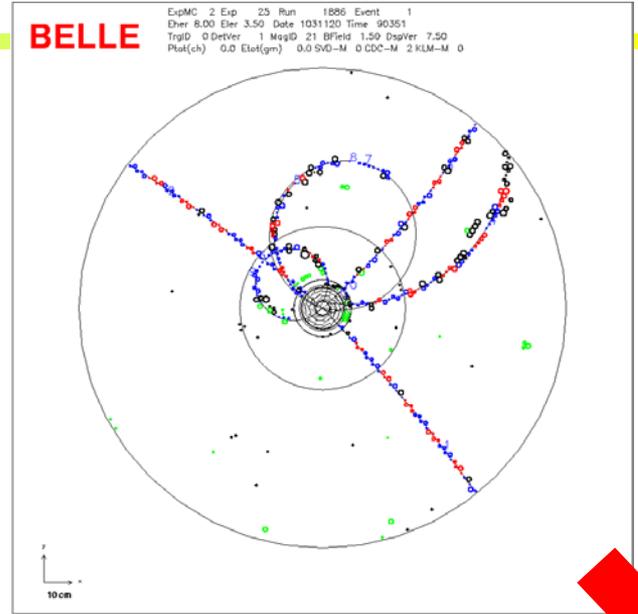
To get x40 higher interaction rate

Need to build a new detector to handle higher backgrounds

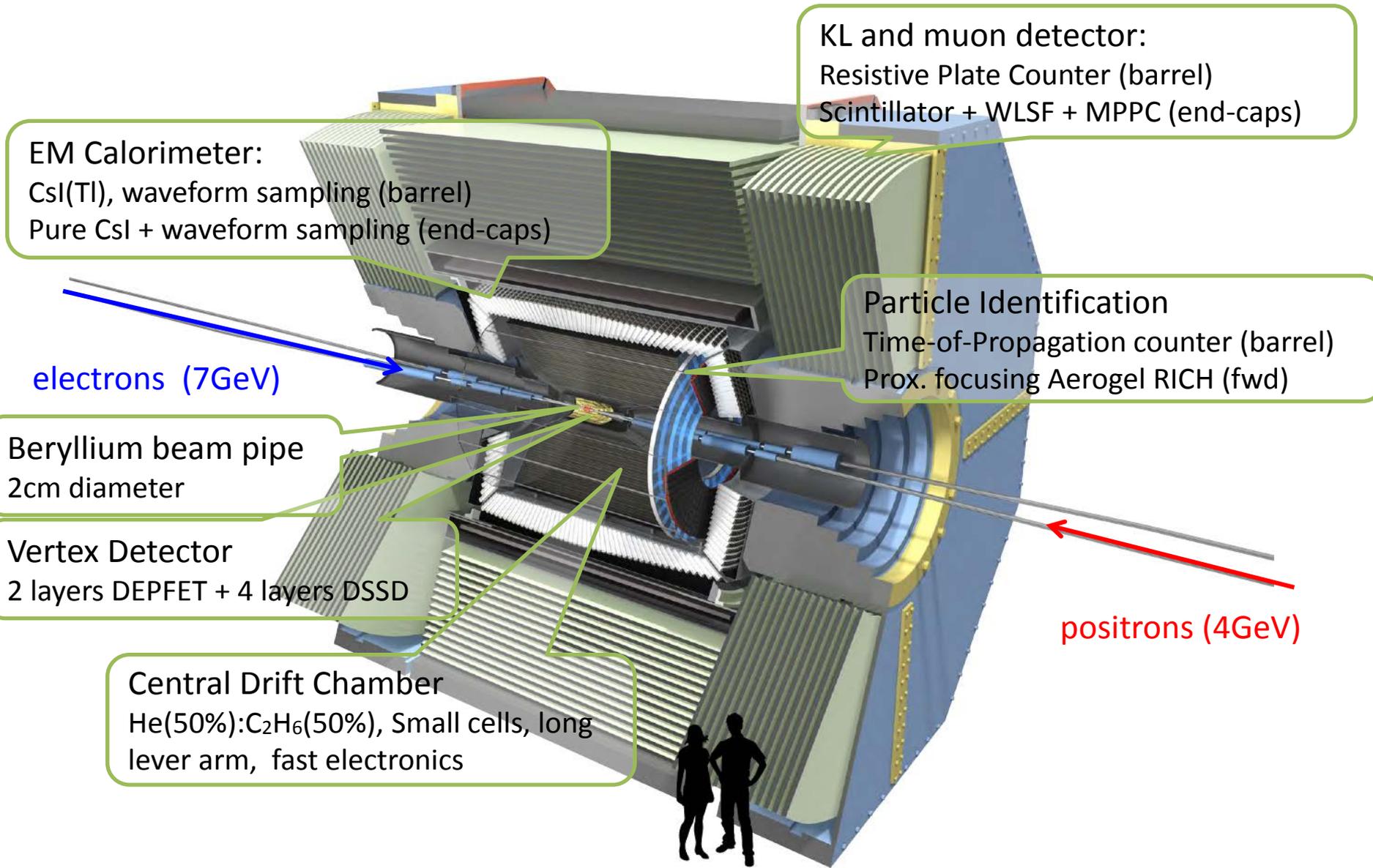
Critical issues at $L = 8 \times 10^{35}/\text{cm}^2/\text{sec}$

- ▶ **Higher background ($\times 10\text{-}20$)**
 - radiation damage and occupancy
 - fake hits and pile-up noise in the EM
- ▶ **Higher event rate ($\times 10$)**
 - higher rate trigger, DAQ and computing
- ▶ **Require special features**
 - low $p \mu$ identification $\leftarrow s\mu\mu$ recon. eff.
 - hermeticity $\leftarrow \nu$ "reconstruction"

Have to employ and develop very advanced technologies to build such an apparatus!



Belle II Detector



KL and muon detector:
Resistive Plate Counter (barrel)
Scintillator + WLSF + MPPC (end-caps)

EM Calorimeter:
CsI(Tl), waveform sampling (barrel)
Pure CsI + waveform sampling (end-caps)

electrons (7GeV)

Beryllium beam pipe
2cm diameter

Vertex Detector
2 layers DEPFET + 4 layers DSSD

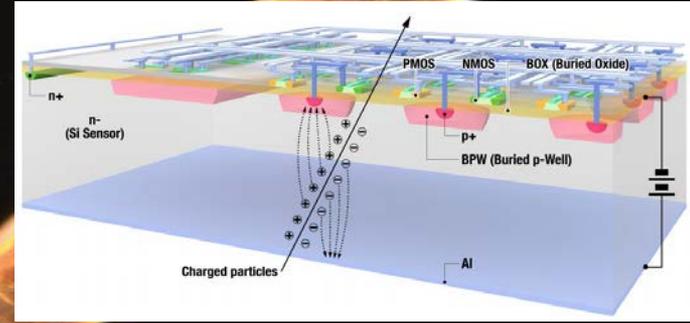
Central Drift Chamber
He(50%):C₂H₆(50%), Small cells, long
lever arm, fast electronics

Particle Identification
Time-of-Propagation counter (barrel)
Prox. focusing Aerogel RICH (fwd)

positrons (4GeV)

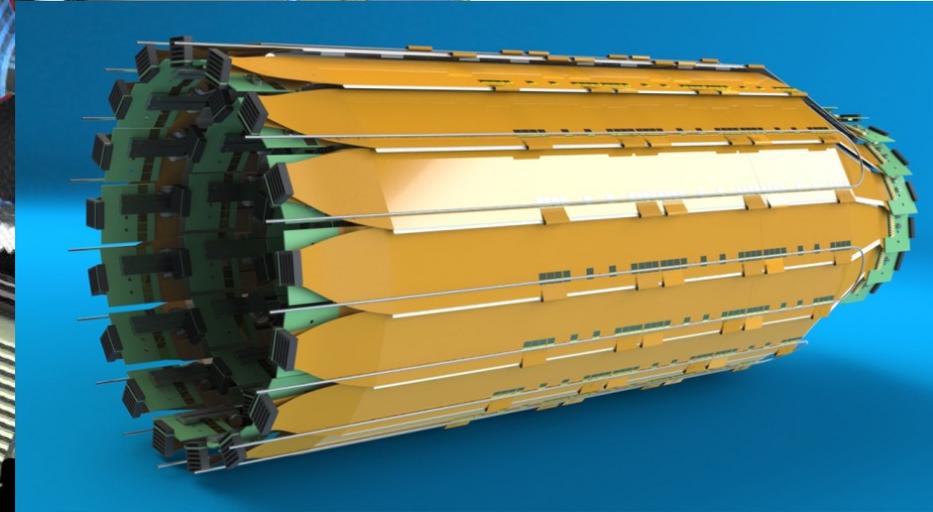
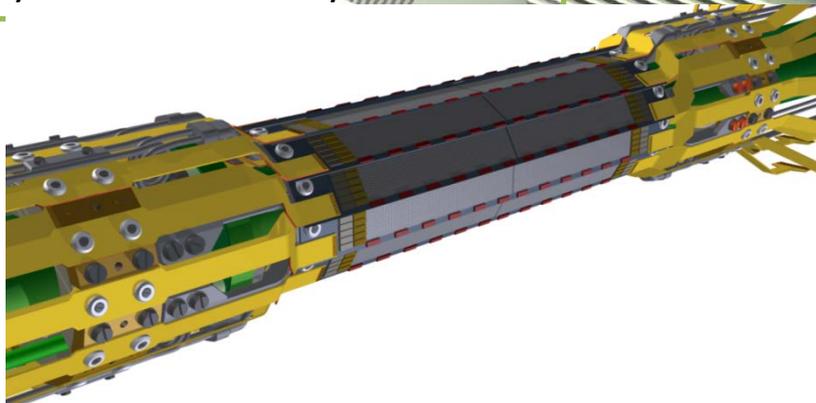
Determine the **reaction point** position with a **fantastic precision** - extremely delicate elements

Hair – 100 microns thick

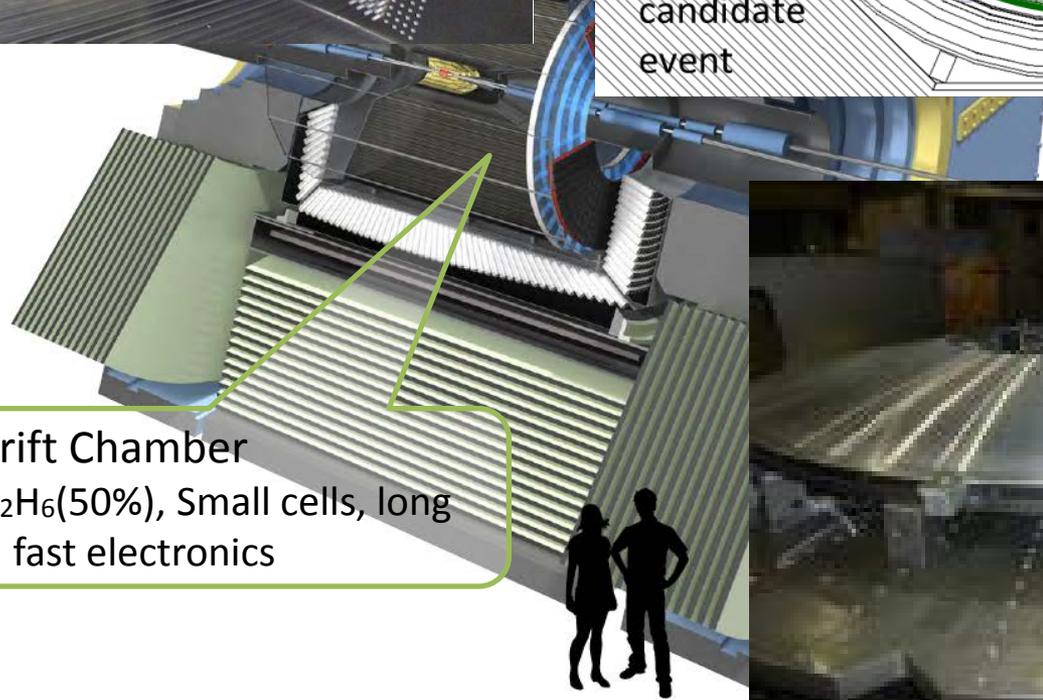
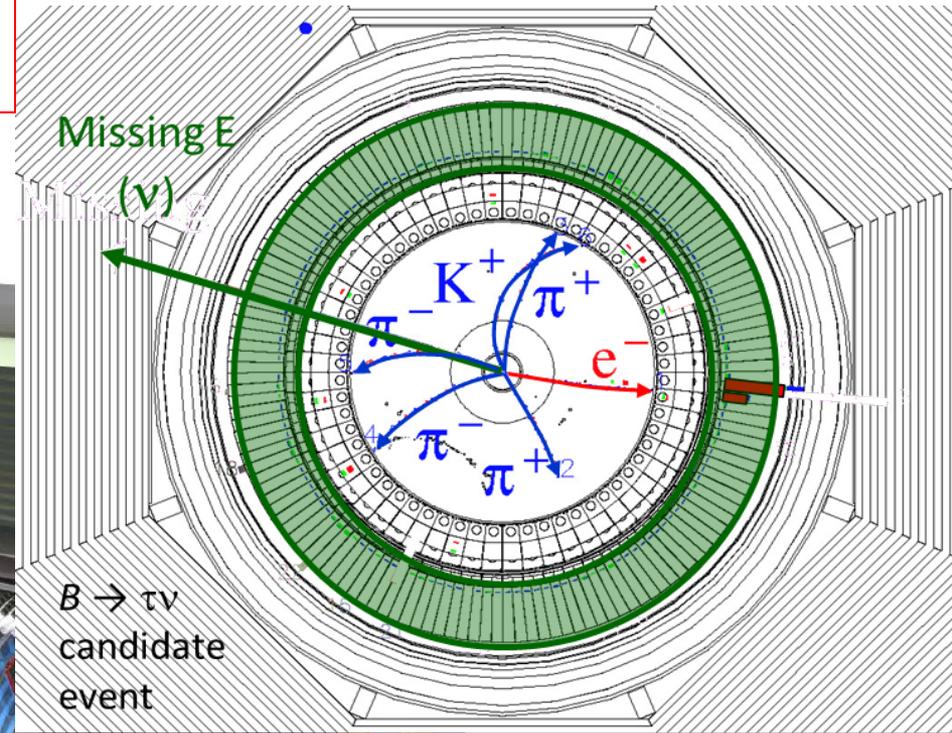
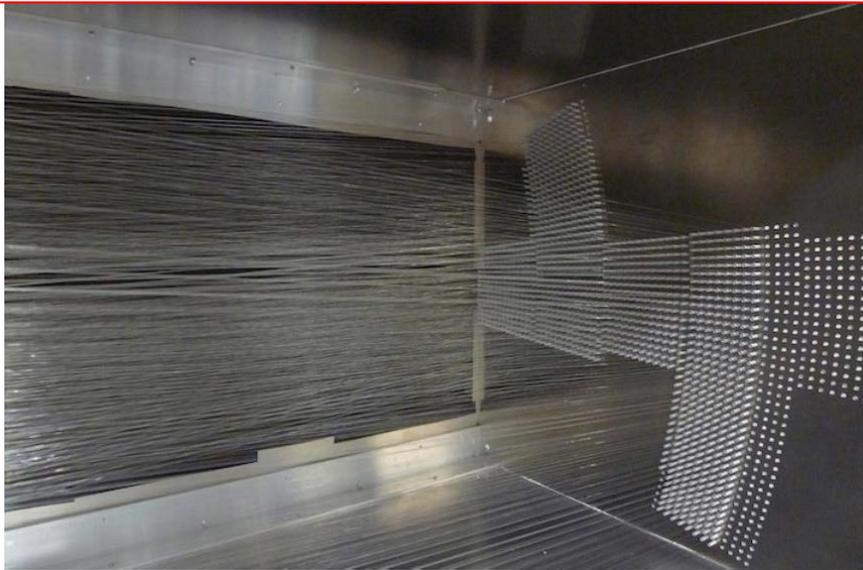


Beryllium beam pipe
2cm diameter

Vertex Detector
2 layers DEPFET + 4 layers DSSD



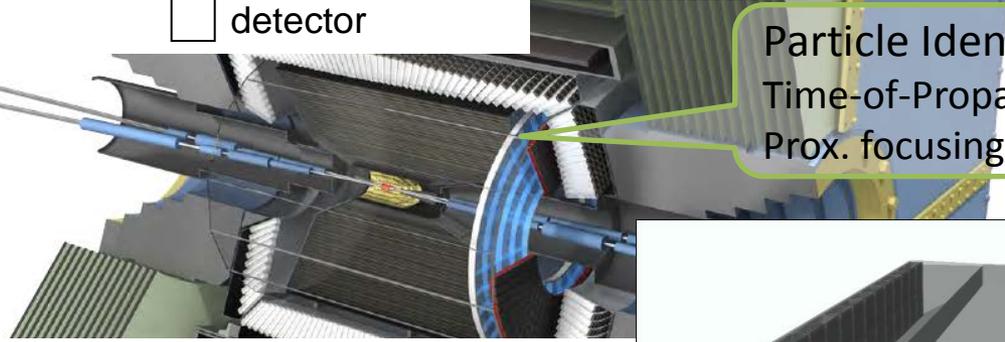
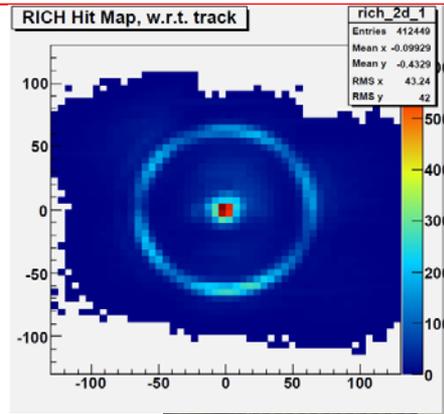
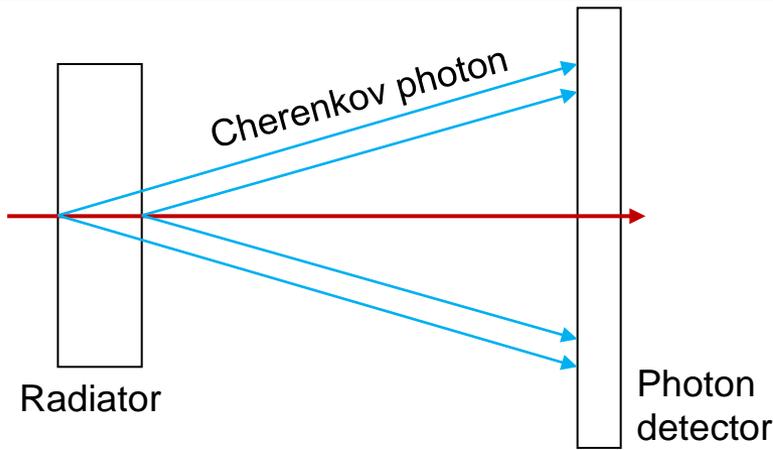
Tracking charged particles in magnetic field – measure their momenta



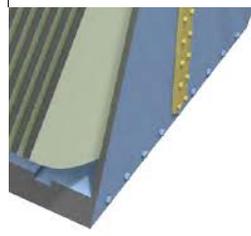
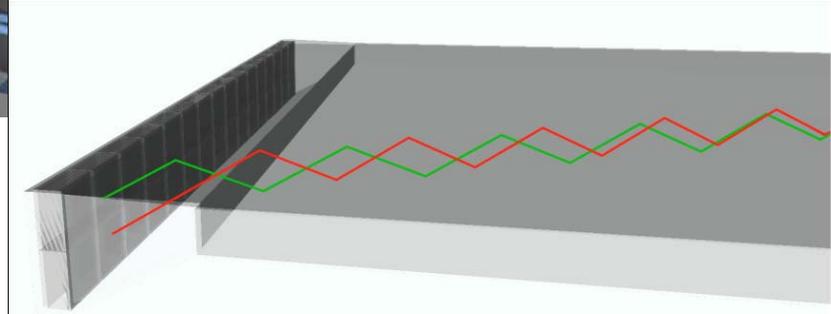
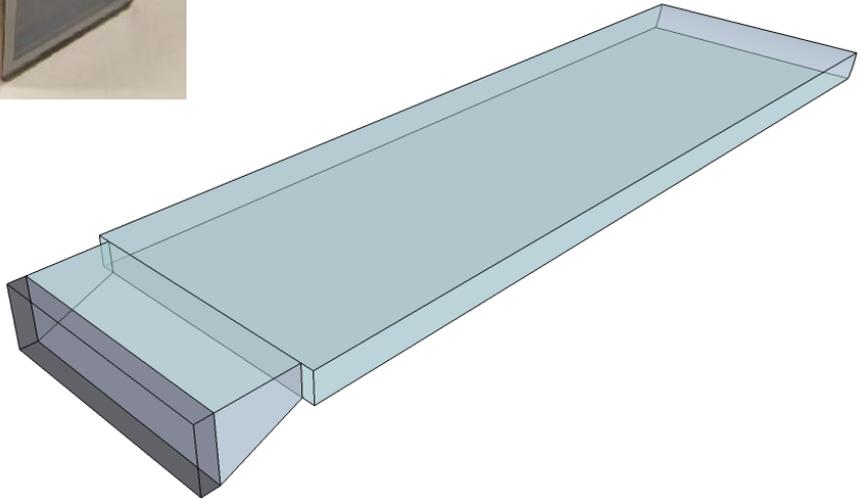
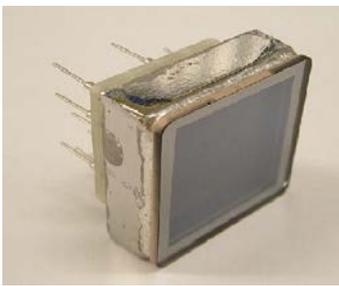
Central Drift Chamber
He(50%):C₂H₆(50%), Small cells, long lever arm, fast electronics



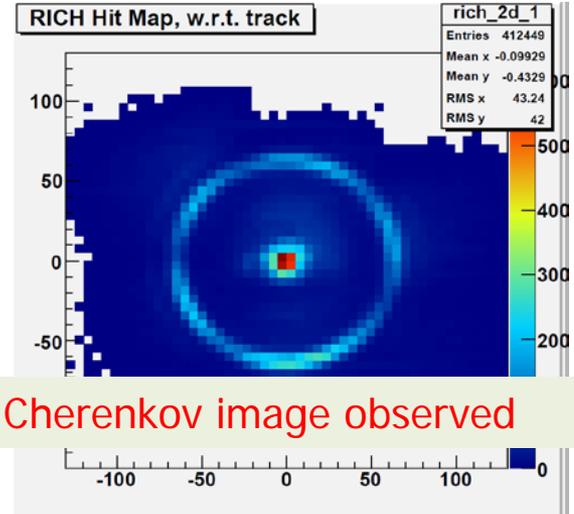
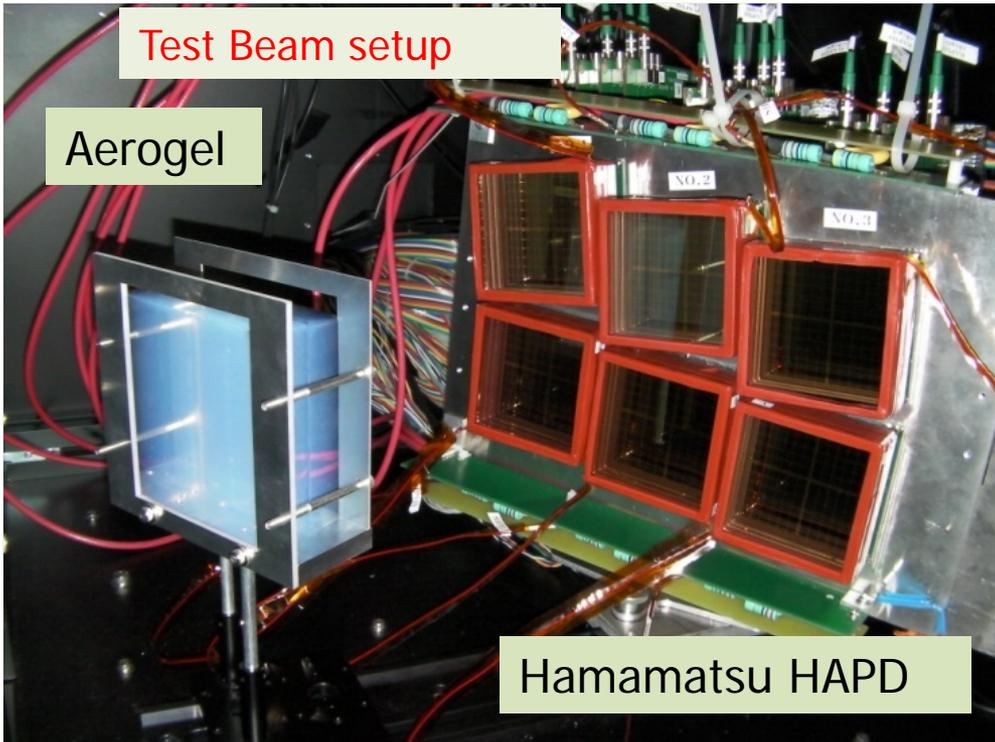
Use **Cherenkov effect**: light emitted by a particle **faster than velocity of light** in a medium - like a **shock wave** from a **supersonic airplane**!



Particle Identification
Time-of-Propagation counter (barrel)
Prox. focusing Aerogel RICH (fwd)

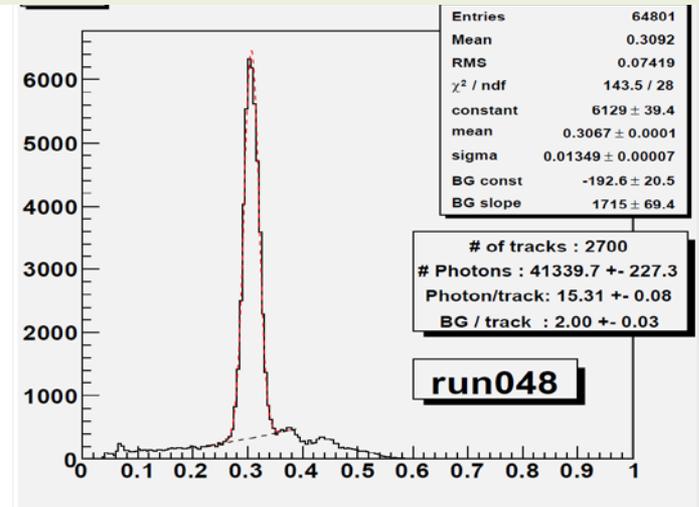


Aerogel RICH (endcap PID)



Clear Cherenkov image observed

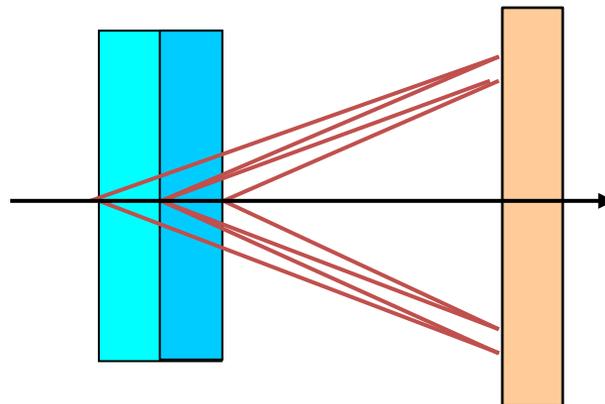
Cherenkov angle distribution



6.6 σ π/K at 4GeV/c !

RICH with a novel "focusing" radiator – a two layer radiator

Employ multiple layers with different refractive indices \rightarrow Cherenkov images from individual layers overlap on the photon detector.



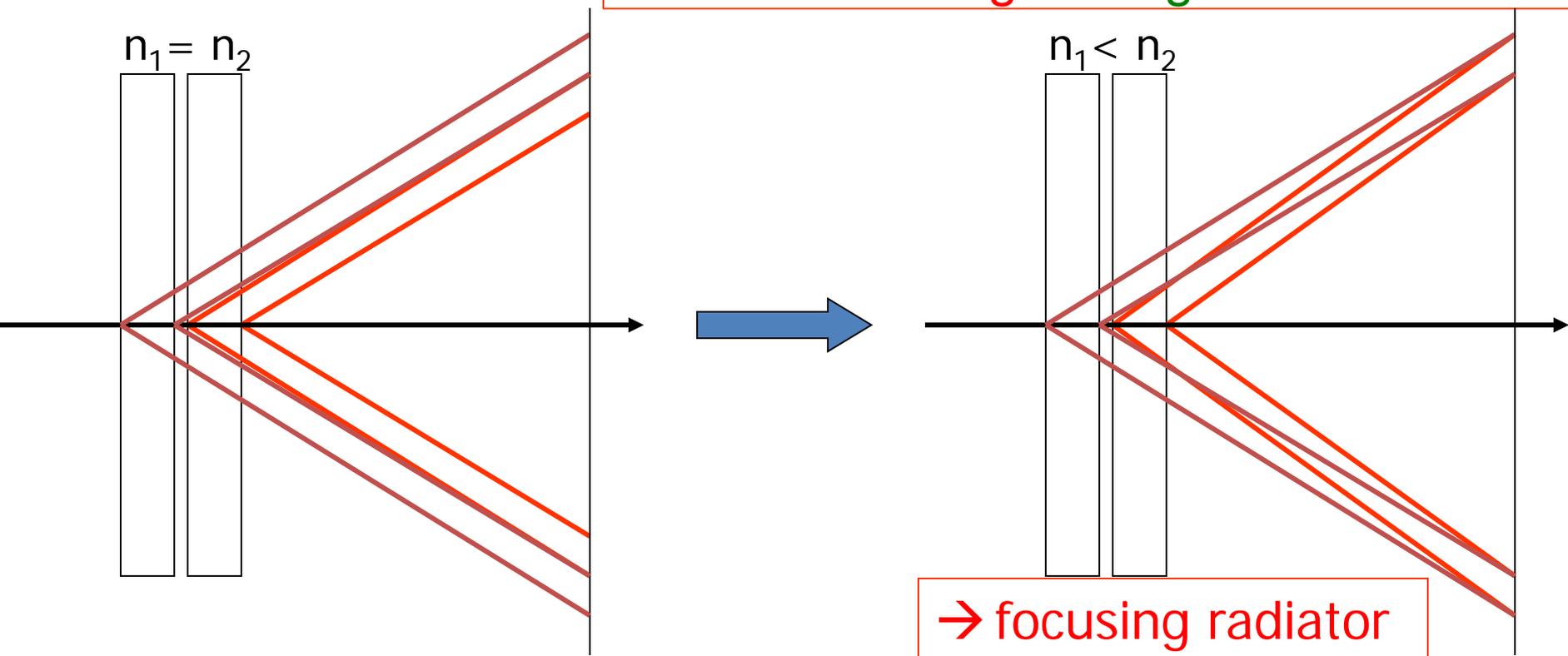


Radiator with multiple refractive indices

How to increase the number of photons without degrading the resolution?

normal

→ stack two tiles with different refractive indices: “focusing” configuration

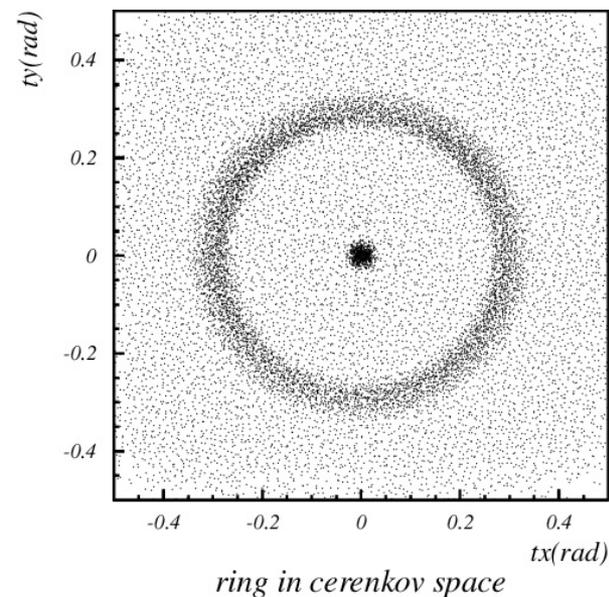
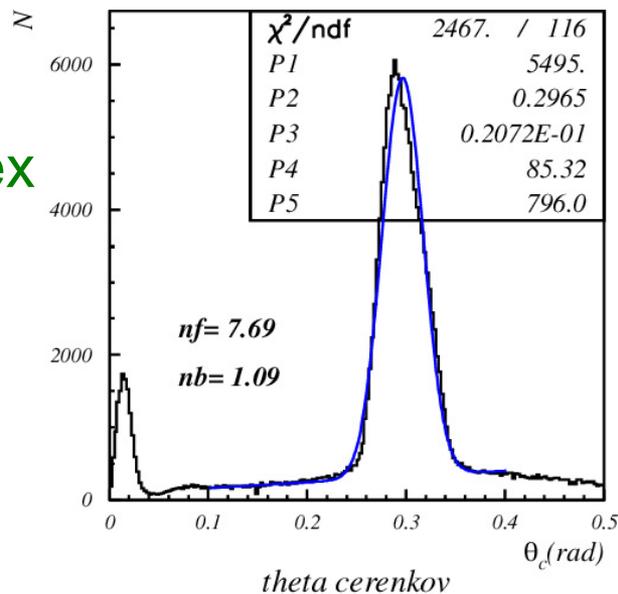
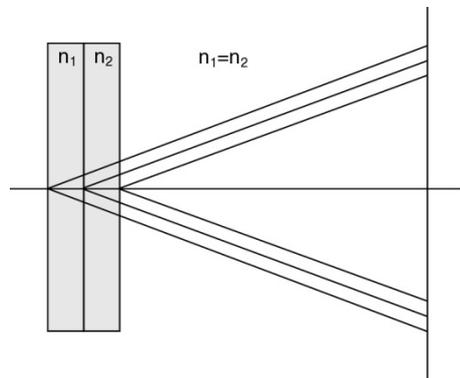


→ focusing radiator

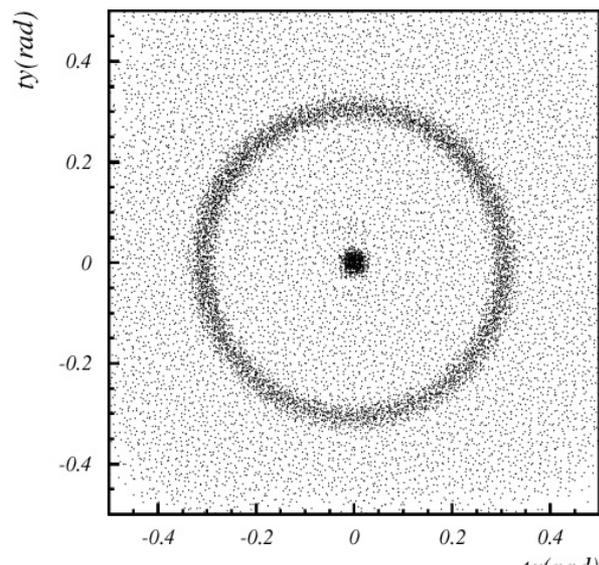
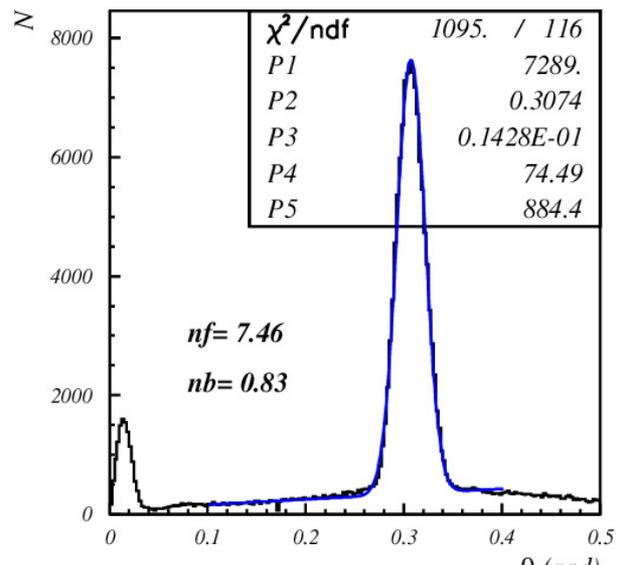
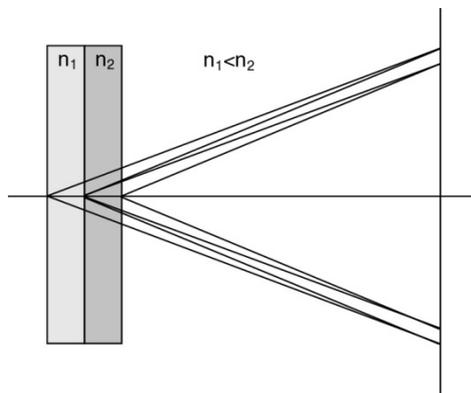
Such a configuration is only possible with aerogel (a form of Si_xO_y) – material with a tunable refractive index between 1.01 and 1.13.

Focusing configuration – data

4cm aerogel single index

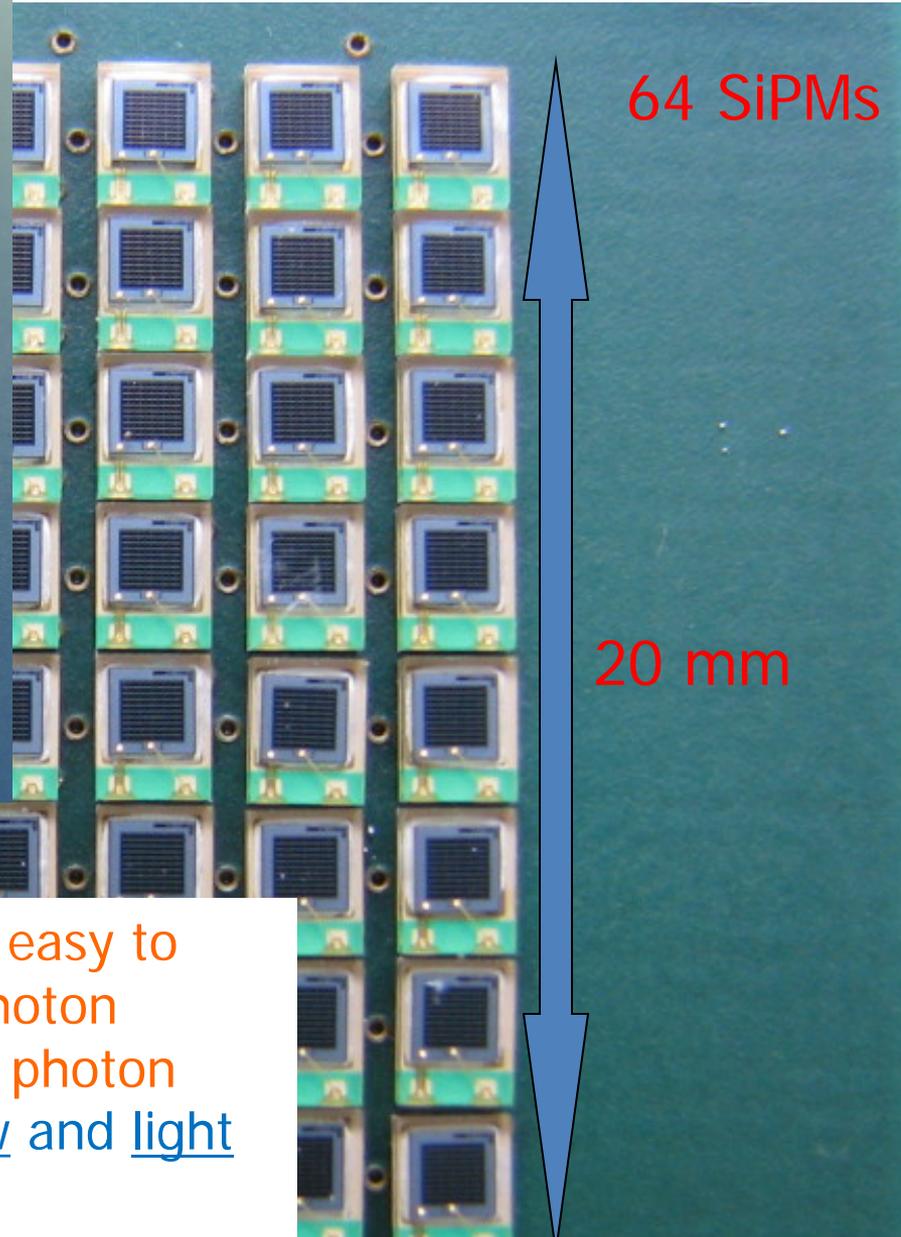
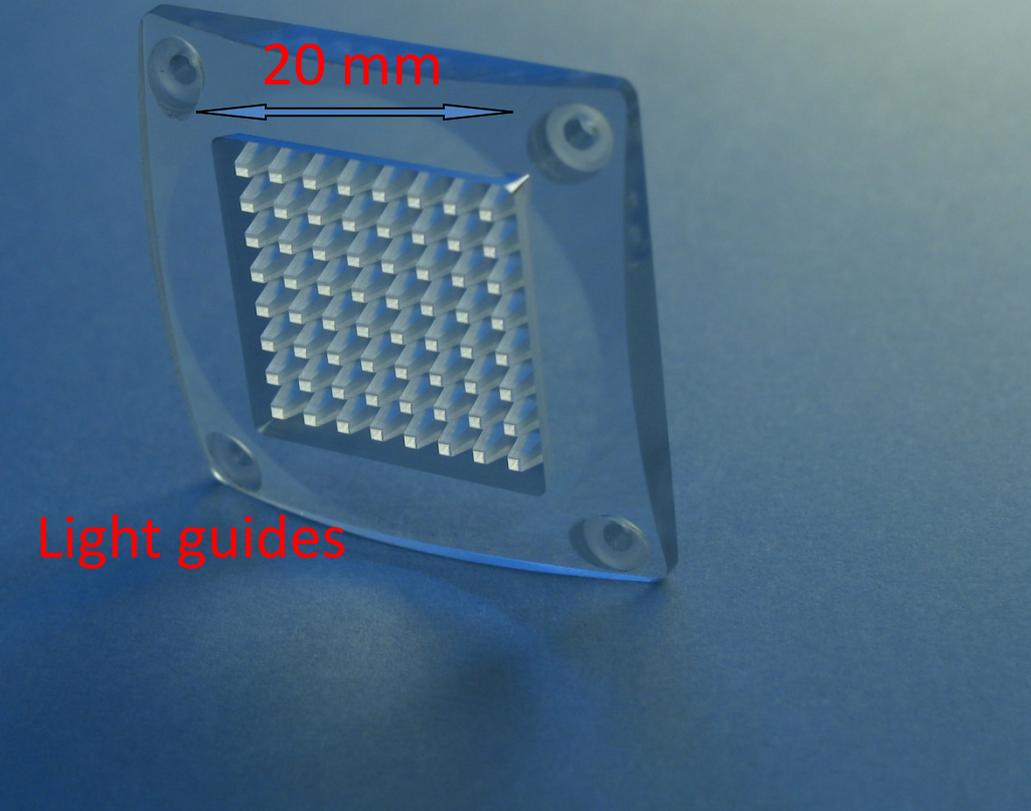


2+2cm aerogel



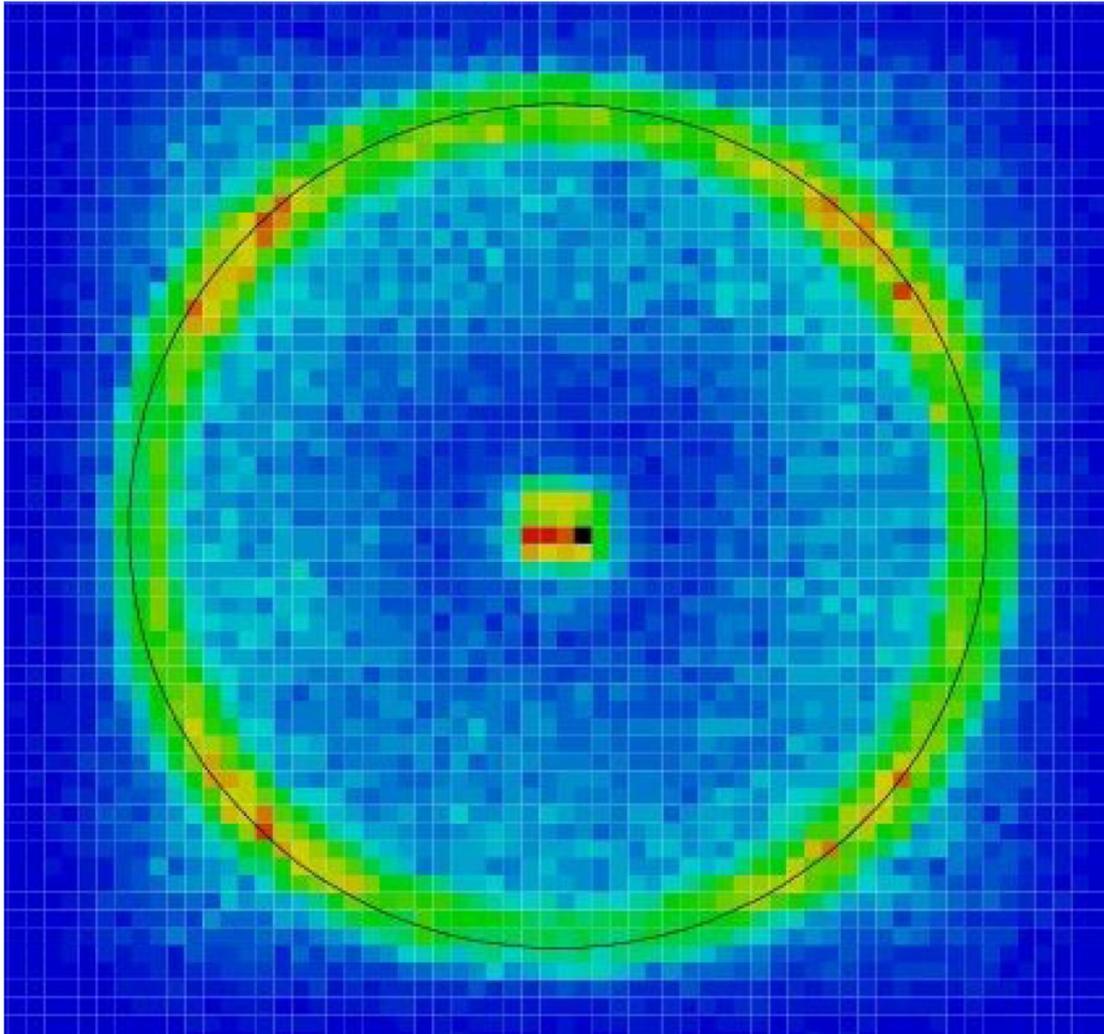
→ NIM A548 (2005) 383

Another candidate: SiPM



Another sensor candidate: SiPMs (G-PAD), easy to handle, but never before used for single photon detection (high dark count rate with single photon pulse height) → use a narrow time window and light concentrators

Cherenkov ring with SiPMs



First successful use of SiPMs
as single photon detectors in a
RICH counter!

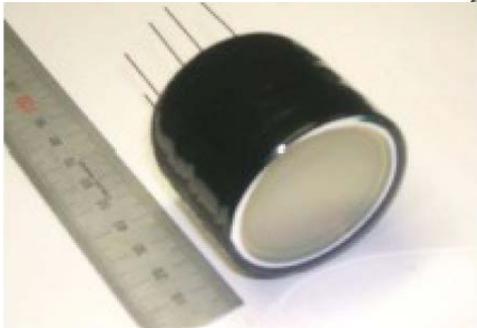
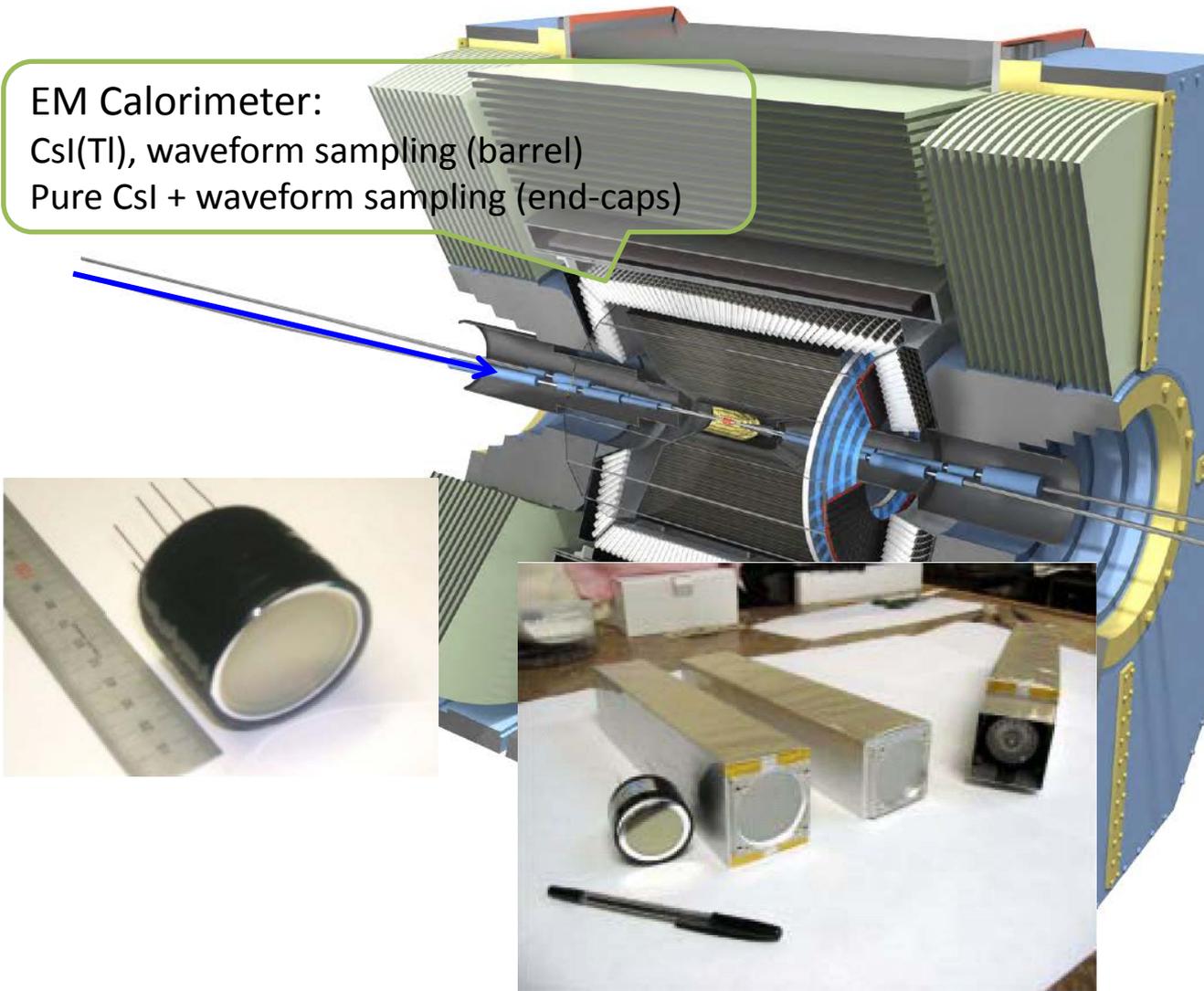
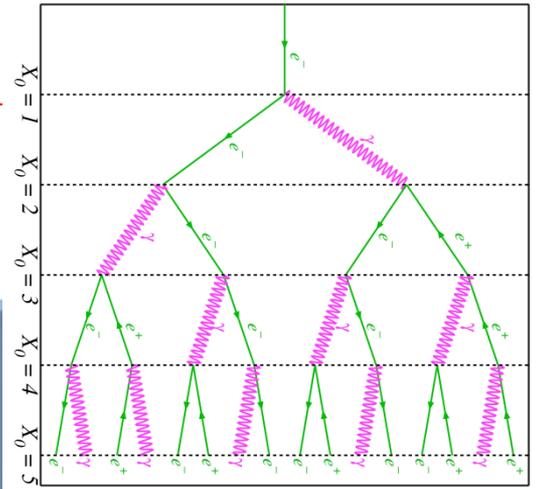
NIM A594 (2008) 13

Detect **electrons** and high energy **gamma rays** by letting them produce a **shower** in a **heavy crystal**

EM Calorimeter:

CsI(Tl), waveform sampling (barrel)

Pure CsI + waveform sampling (end-caps)

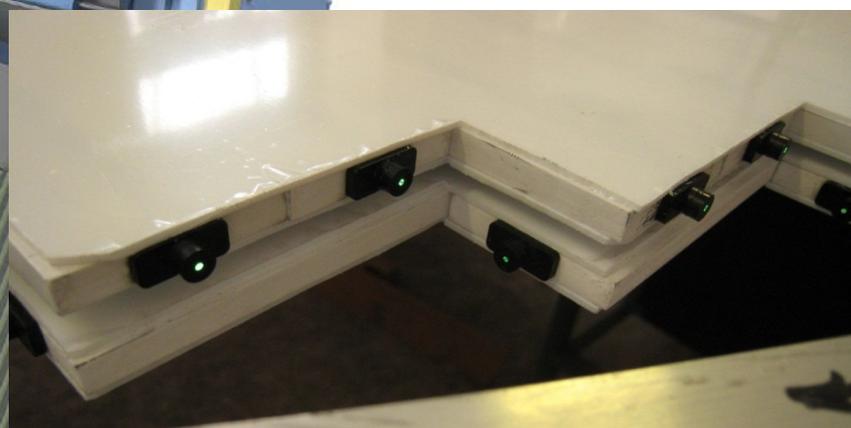
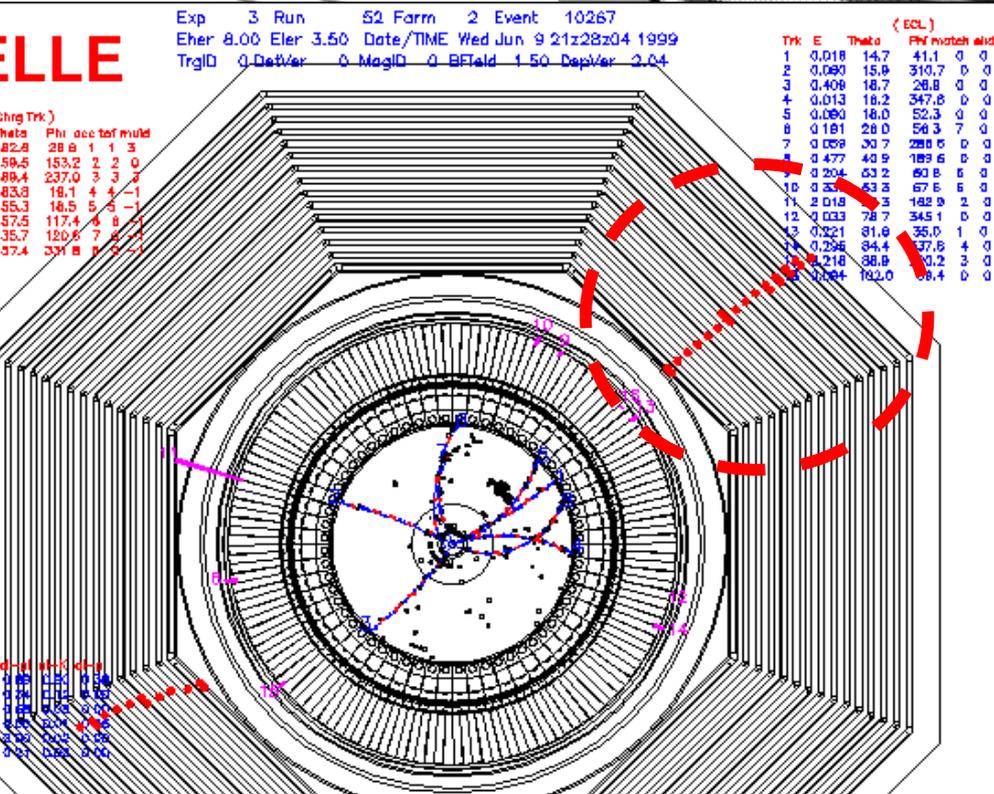
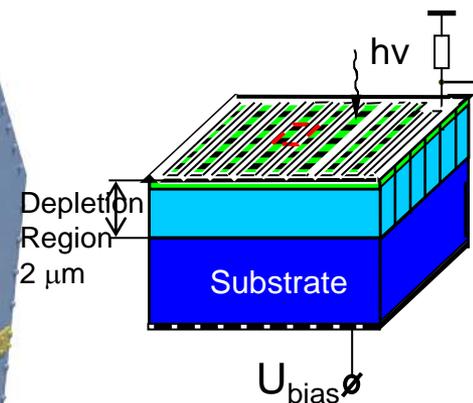
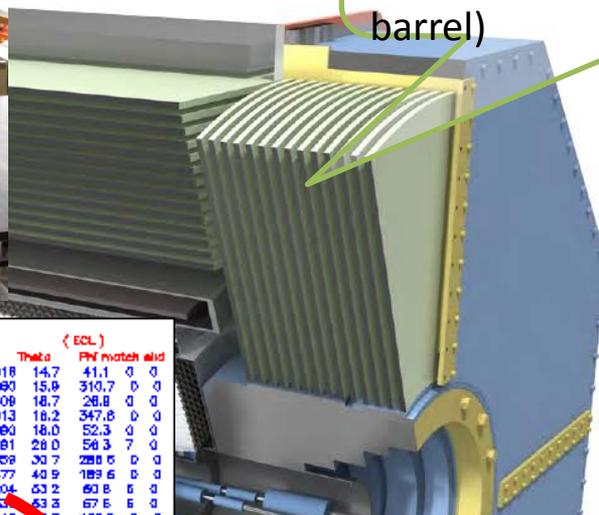
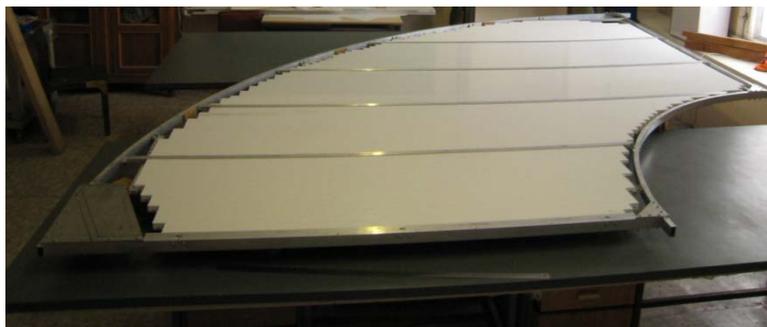


Detect muons: particles that penetrate 1m of iron

KL and muon detector:

Resistive Plate Counter (barrel)

Scintillator + WLSF + MPPC (end-caps + barrel)

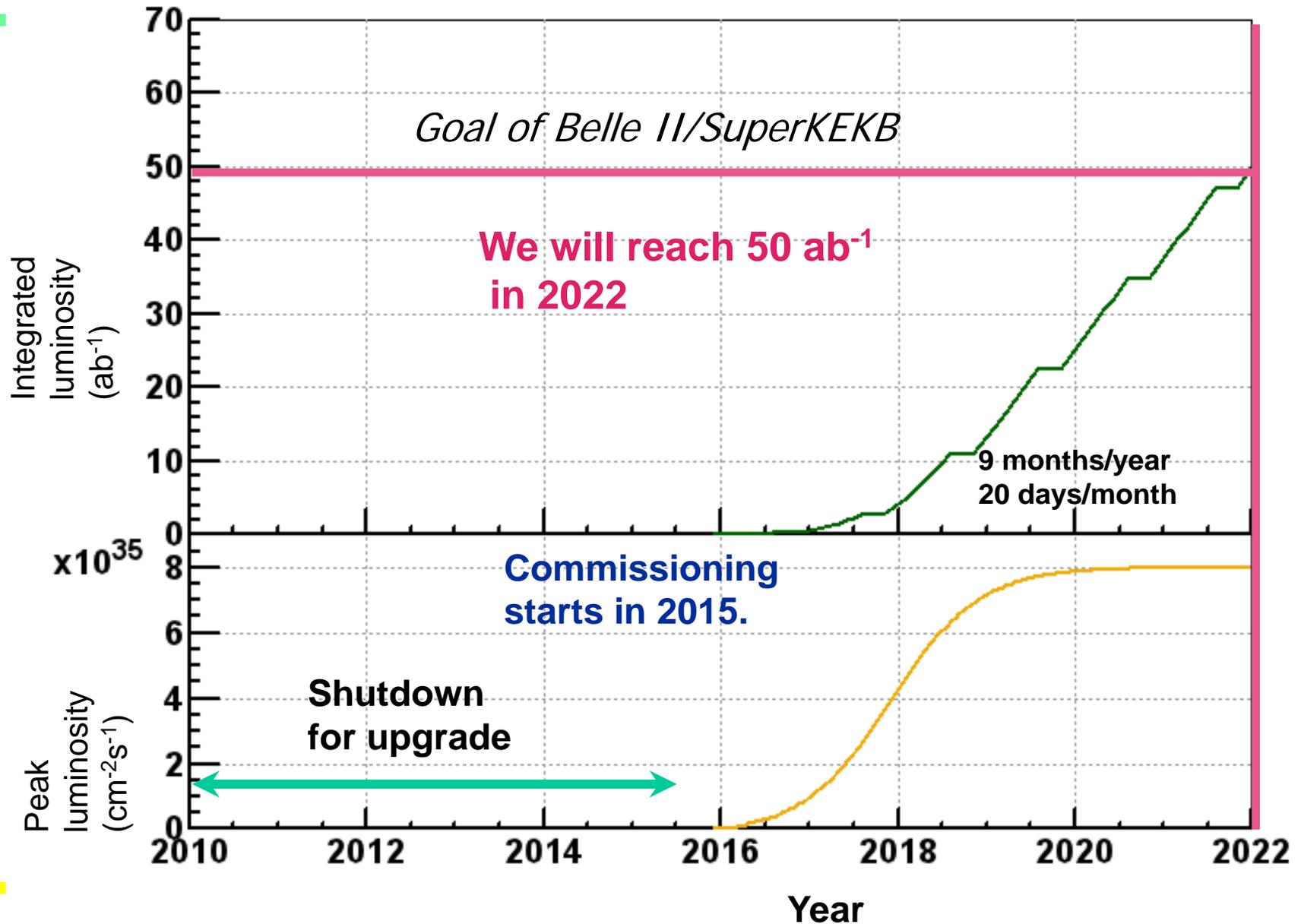


The Belle II Collaboration



A very strong group of ~400 highly motivated scientists!

Schedule (Beam starts end of 2014)





Conclusion



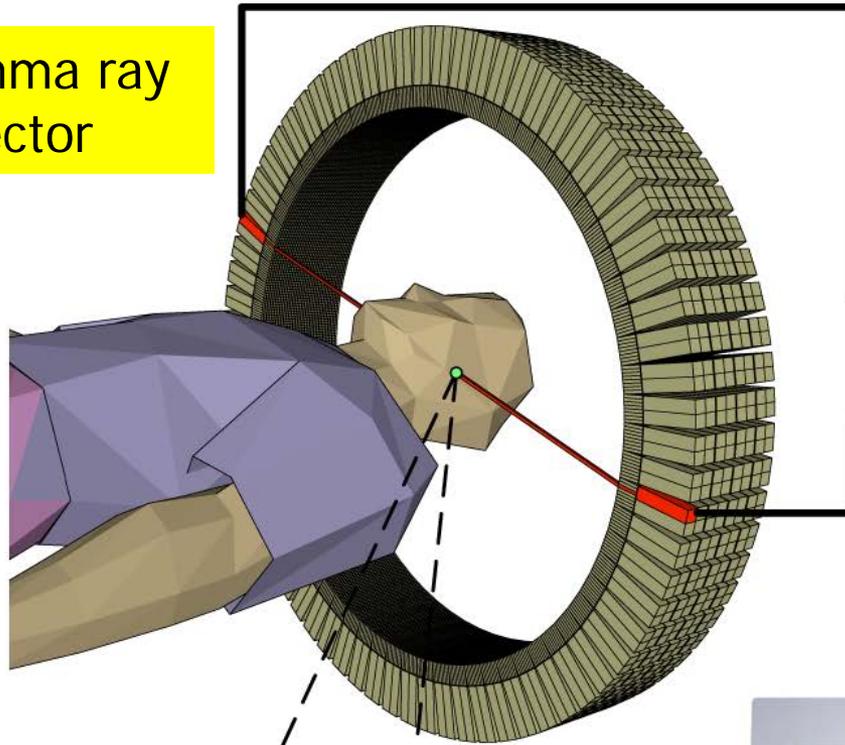
- Understanding of CP violation has helped to shape our understanding of Nature at small scales and in the early Universe
- A big step since its discovery in 1964, however there are many open questions left. One way how to proceed is to make very precise measurements → intensity frontier of particle physics
- Major upgrade of the KEKB accelerator and Belle detector at KEK in 2010-15 → SuperKEKB+Belle II, with **40x larger** event rates, **construction started**
- Expect a new, exciting **era of discoveries**, complementary to the LHC

Slovenian physics have been playing an important role in flavour physics, and it all started when Elko Kernel brought us young physics into the ARGUS collaboration.

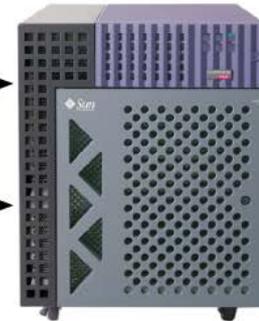
Elko also had the bright idea that we should get involved in RICH detectors, and we indeed became one of the leading labs in this challenging detection method.

PET: positron emission tomography

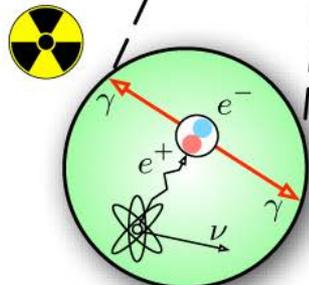
Gamma ray detector



Read-out electronics



Data transfer



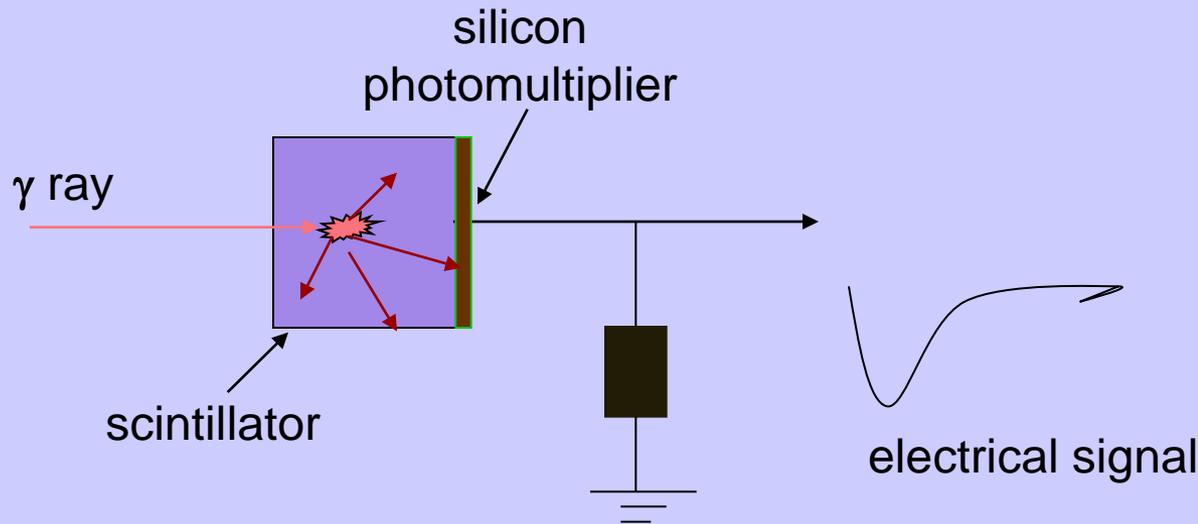
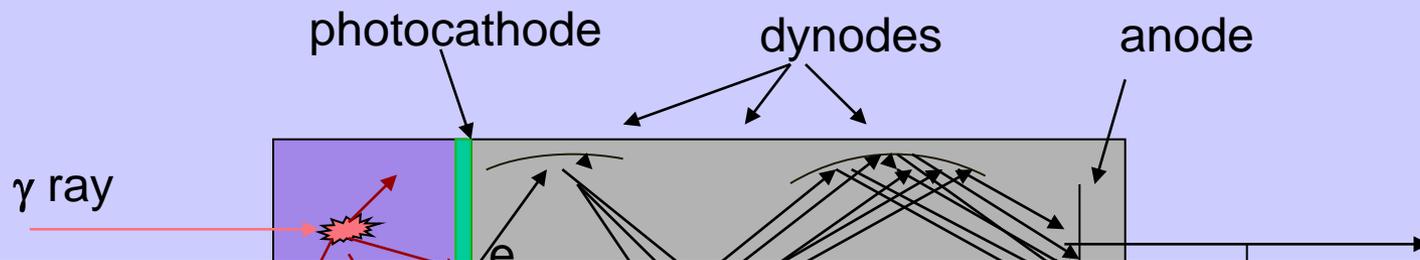
Annihilation of e^+e^-

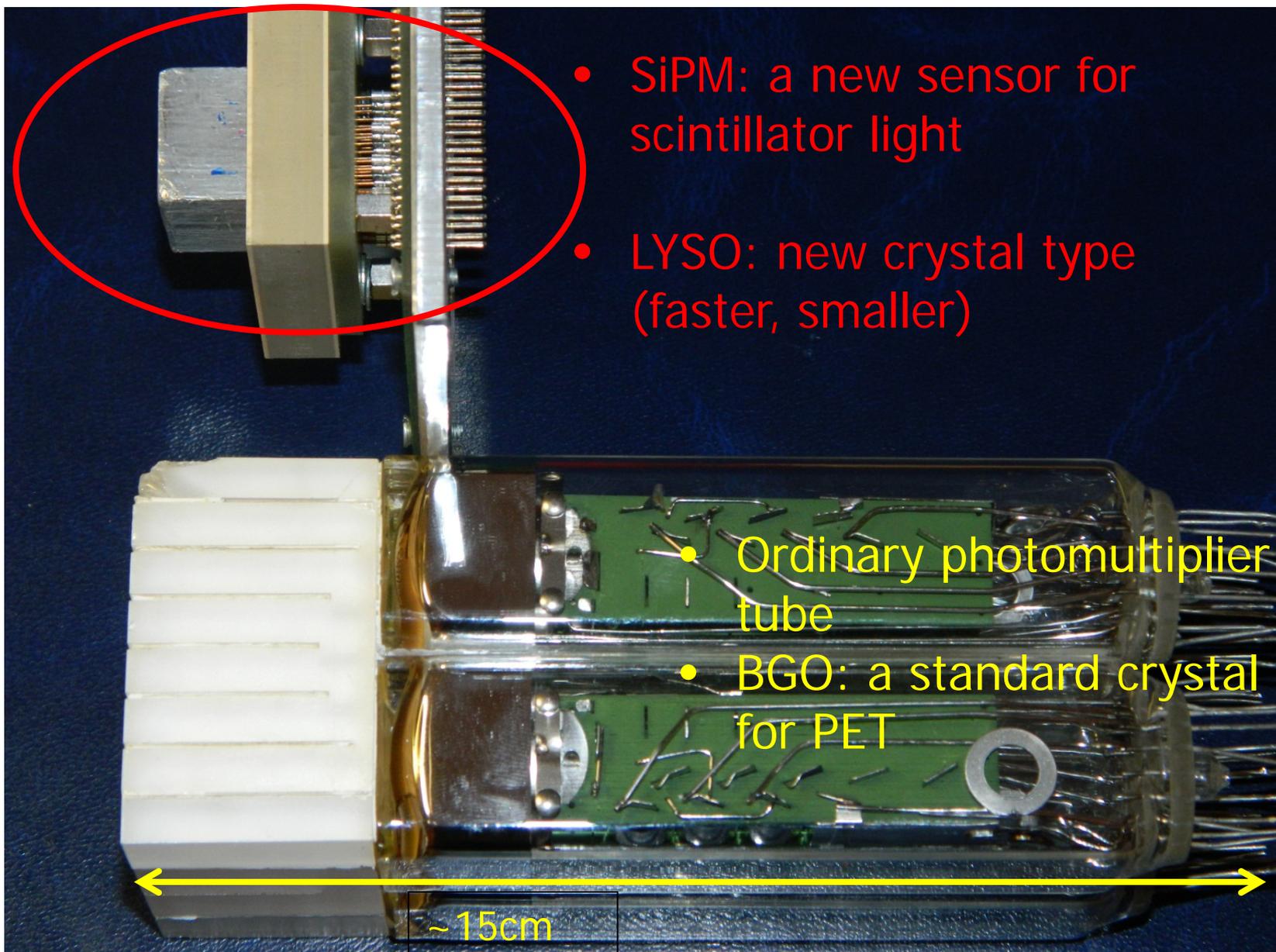


Image reconstruction

PET with a new sensor type

Silicon photomultiplier (SiPM): a new light sensor type
→ considerably smaller than the existing light sensors, does not need a high voltage supply, works well magnetic fields (several T).



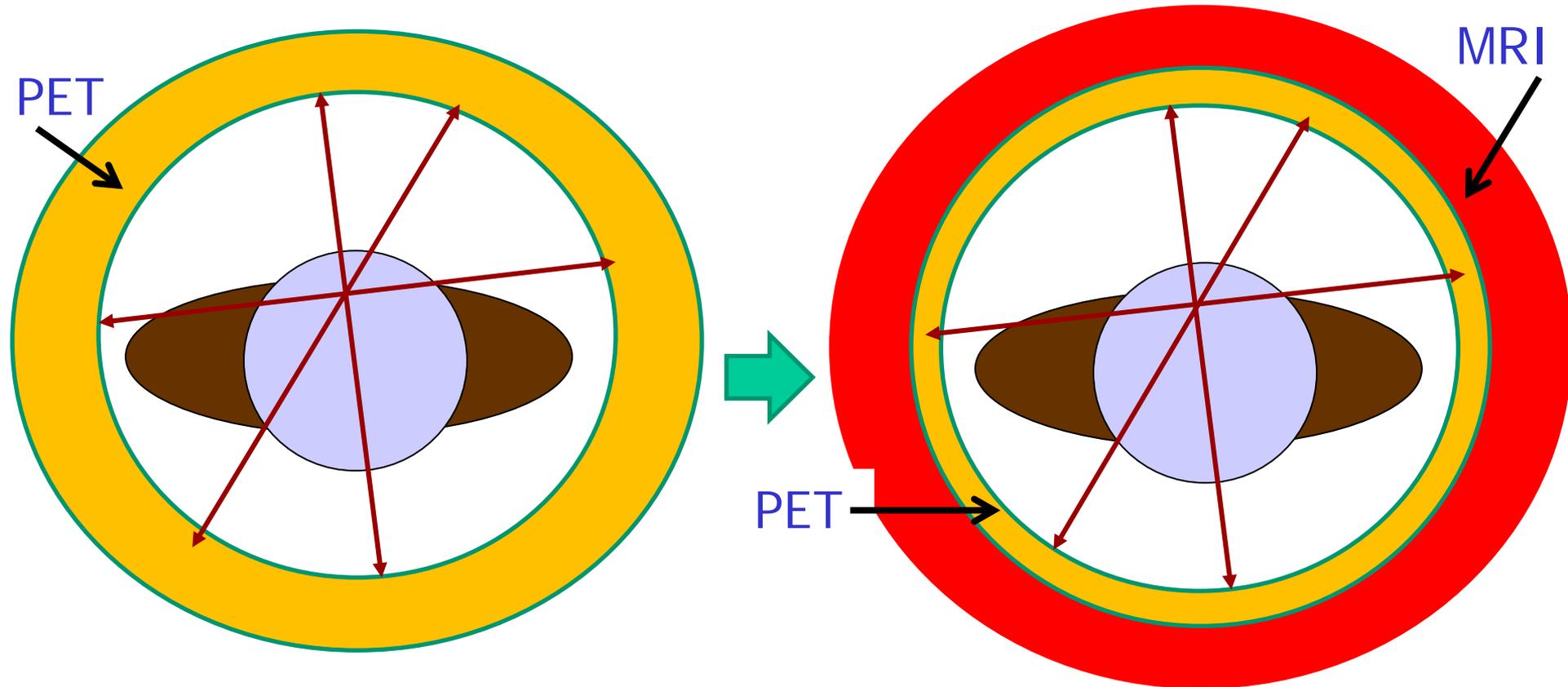


- SiPM: a new sensor for scintillator light
- LYSO: new crystal type (faster, smaller)

- Ordinary photomultiplier tube
- BGO: a standard crystal for PET

~15cm

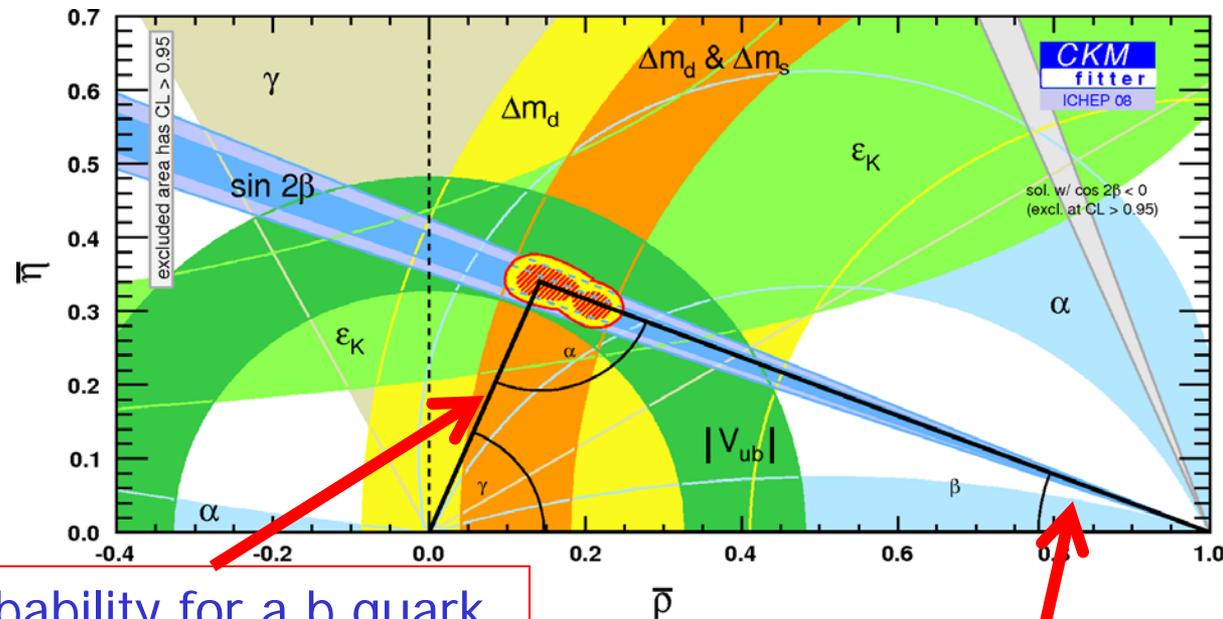
New sensor type → considerably smaller than existing detectors, operates well in high magnetic field



Allows a simultaneous imaging with magnetic resonance and PET – an important improvement in diagnostics!

More slides....

All experimental studies combined...



Probability for a b quark to turn into a u quark \rightarrow determines the length of the side V_{ub}

CP asymmetry oscillation amplitude \rightarrow angle $\phi_1 = \beta$

Constraints from measurements of angles and sides of the unitarity triangle

\rightarrow Remarkable agreement

B Physics @ Y(4S)

Observable	B Factories (2 ab ⁻¹)	SuperB (75 ab ⁻¹)
sin(2β) (J/ψ K ⁰)	0.018	0.005 (†)
cos(2β) (J/ψ K ^{*0})	0.30	0.05
sin(2β) (Dh ⁰)	0.10	0.02
cos(2β) (Dh ⁰)	0.20	0.04
S(J/ψ π ⁰)	0.10	0.02
S(D ⁺ D ⁻)	0.20	0.03
S(φK ⁰)	0.13	0.02 (*)
S(η'K ⁰)	0.05	0.01 (*)
S(K _s ⁰ K _s ⁰ K _s ⁰)	0.15	0.02 (*)
S(K _s ⁰ π ⁰)	0.15	0.02 (*)
S(ωK _s ⁰)	0.17	0.03 (*)
S(f ₀ K _s ⁰)	0.12	0.02 (*)
γ (B → DK, D → CP eigenstates)	~ 15°	2.5°
γ (B → DK, D → suppressed states)	~ 12°	2.0°
γ (B → DK, D → multibody states)	~ 9°	1.5°
γ (B → DK, combined)	~ 6°	1-2°
α (B → ππ)	~ 16°	3°
α (B → ρρ)	~ 7°	1-2° (*)
α (B → ρπ)	~ 12°	2°
α (combined)	~ 6°	1-2° (*)
2β + γ (D ^{(*)±} π [∓] , D [±] K _s ⁰ π [∓])	20°	5°

Observable	B Factories (2 ab ⁻¹)	SuperB (75 ab ⁻¹)
V _{cb} (exclusive)	4% (*)	1.0% (*)
V _{cb} (inclusive)	1% (*)	0.5% (*)
V _{ub} (exclusive)	8% (*)	3.0% (*)
V _{ub} (inclusive)	8% (*)	2.0% (*)
$\mathcal{B}(B \rightarrow \tau\nu)$	20%	4% (†)
$\mathcal{B}(B \rightarrow \mu\nu)$	visible	5%
$\mathcal{B}(B \rightarrow D\tau\nu)$	10%	2%
$\mathcal{B}(B \rightarrow \rho\gamma)$	15%	3% (†)
$\mathcal{B}(B \rightarrow \omega\gamma)$	30%	5%
$A_{CP}(B \rightarrow K^*\gamma)$	0.007 (†)	0.004 († *)
$A_{CP}(B \rightarrow \rho\gamma)$	~ 0.20	0.05
$A_{CP}(b \rightarrow s\gamma)$	0.012 (†)	0.004 (†)
$A_{CP}(b \rightarrow (s+d)\gamma)$	0.03	0.006 (†)
S(K _s ⁰ π ⁰ γ)	0.15	0.02 (*)
S(ρ ⁰ γ)	possible	0.10
$A_{CP}(B \rightarrow K^*\ell\ell)$	7%	1%
$A^{FB}(B \rightarrow K^*\ell\ell)_{s_0}$	25%	9%
$A^{FB}(B \rightarrow X_s\ell\ell)_{s_0}$	35%	5%
$\mathcal{B}(B \rightarrow K\nu\bar{\nu})$	visible	20%
$\mathcal{B}(B \rightarrow \pi\nu\bar{\nu})$	-	possible

Charm mixing and CP

Mode	Observable	Υ(4S) (75 ab ⁻¹)	ψ(3770) (300 fb ⁻¹)
D ⁰ → K ⁺ π ⁻	x' ²	3 × 10 ⁻⁵	
	y'	7 × 10 ⁻⁴	
	y _{CP}	5 × 10 ⁻⁴	
D ⁰ → K ⁺ K ⁻	x	4.9 × 10 ⁻⁴	
	y	3.5 × 10 ⁻⁴	
D ⁰ → K _S ⁰ π ⁺ π ⁻	q/p	3 × 10 ⁻²	
	φ	2°	
	x ²		(1-2) × 10 ⁻⁵
ψ(3770) → D ⁰ D ⁰	y		(1-2) × 10 ⁻³
	cos δ		(0.01-0.02)

Charm FCNC

	Sensitivity
D ⁰ → e ⁺ e ⁻ , D ⁰ → μ ⁺ μ ⁻	1 × 10 ⁻⁸
D ⁰ → π ⁰ e ⁺ e ⁻ , D ⁰ → π ⁰ μ ⁺ μ ⁻	2 × 10 ⁻⁸
D ⁰ → ηe ⁺ e ⁻ , D ⁰ → ημ ⁺ μ ⁻	3 × 10 ⁻⁸
D ⁰ → K _s ⁰ e ⁺ e ⁻ , D ⁰ → K _s ⁰ μ ⁺ μ ⁻	3 × 10 ⁻⁸
D ⁺ → π ⁺ e ⁺ e ⁻ , D ⁺ → π ⁺ μ ⁺ μ ⁻	1 × 10 ⁻⁸

D ⁰ → e [±] μ [∓]	1 × 10 ⁻⁸
D ⁺ → π ⁺ e [±] μ [∓]	1 × 10 ⁻⁸
D ⁰ → π ⁰ e [±] μ [∓]	2 × 10 ⁻⁸
D ⁰ → ηe [±] μ [∓]	3 × 10 ⁻⁸
D ⁰ → K _s ⁰ e [±] μ [∓]	3 × 10 ⁻⁸
D ⁺ → π ⁻ e ⁺ e ⁺ , D ⁺ → K ⁻ e ⁺ e ⁺	1 × 10 ⁻⁸
D ⁺ → π ⁻ μ ⁺ μ ⁺ , D ⁺ → K ⁻ μ ⁺ μ ⁺	1 × 10 ⁻⁸
D ⁺ → π ⁻ e [±] μ [∓] , D ⁺ → K ⁻ e [±] μ [∓]	1 × 10 ⁻⁸

τ Physics

Sensitivity

$\mathcal{B}(\tau \rightarrow \mu\gamma)$	2 × 10 ⁻⁹
$\mathcal{B}(\tau \rightarrow e\gamma)$	2 × 10 ⁻⁹
$\mathcal{B}(\tau \rightarrow \mu\mu\mu)$	2 × 10 ⁻¹⁰
$\mathcal{B}(\tau \rightarrow eee)$	2 × 10 ⁻¹⁰
$\mathcal{B}(\tau \rightarrow \mu\eta)$	4 × 10 ⁻¹⁰
$\mathcal{B}(\tau \rightarrow e\eta)$	6 × 10 ⁻¹⁰
$\mathcal{B}(\tau \rightarrow \ell K_s^0)$	2 × 10 ⁻¹⁰

B_s Physics @ Y(5S)

Observable	Error with 1 ab ⁻¹	Error with 30 ab ⁻¹
ΔΓ	0.16 ps ⁻¹	0.03 ps ⁻¹
Γ	0.07 ps ⁻¹	0.01 ps ⁻¹
β _s from angular analysis	20°	8°
A _{SL} [*]	0.006	0.004
A _{CH}	0.004	0.004
$\mathcal{B}(B_s \rightarrow \mu^+\mu^-)$	-	< 8 × 10 ⁻⁹
V _{td} /V _{ts}	0.08	0.017
$\mathcal{B}(B_s \rightarrow \gamma\gamma)$	38%	7%
β _s from J/ψφ	10°	3°
β _s from B _s → K ⁰ K ⁰	24°	11°

Relation between the Super B Factory and the LHC

- **Physics motivation is independent of LHC.**
 - If LHC finds NP, precision flavour physics is compulsory.
 - If LHC finds no NP, high statistics B/ τ decays would be a unique way to search for the $>$ TeV scale physics (=TeV scale in case of MFV).

How big is a nano-beam ?

$$L = \frac{\gamma_{e\pm}}{2er_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left(\frac{I_{e\pm} \xi_{\zeta y}^{e\pm}}{\beta_y^*} \right) \left(\frac{R_L}{R_{\xi_y}} \right)$$

Lorentz factor $\gamma_{e\pm}$
 Beam current $I_{e\pm}$
 Beam-beam parameter $\xi_{\zeta y}^{e\pm}$
 Classical electron radius er_e
 Beam size ratio@IP $\frac{\sigma_y^*}{\sigma_x^*}$ 1 - 2 % (flat beam)
 Vertical beta function@IP β_y^*
 Lumi. reduction factor (crossing angle) & Tune shift reduction factor (hour glass effect) $\frac{R_L}{R_{\xi_y}}$ 0.8 - 1 (short bunch)

- (1) Smaller β_y^*
- (2) Increase beam currents
- (3) Increase $\xi_{\zeta y}$

"Nano-Beam" scheme

Collision with very small spot-size beams

Invented by Pantaleo Raimondi for SuperB

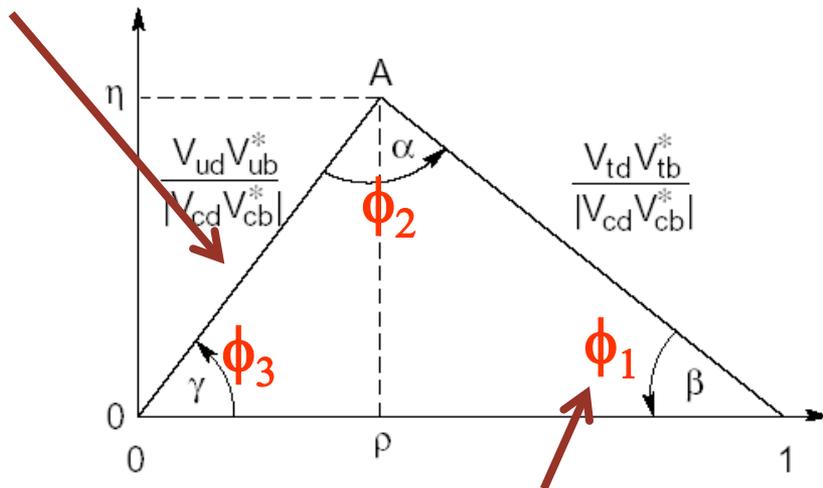
CKM matrix: determines charged weak interaction of quarks

Wolfenstein parametrisation: expand the CKM matrix in the parameter λ ($=\sin\theta_c=0.22$)

A , ρ and η : all of order one

$$V = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

from probability of $b \rightarrow u$ transitions



7-92

from CP violation in $B \rightarrow J/\psi K_S$ decays

Unitarity condition:

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



Goal: measure sides and angles in several different ways, check consistency →