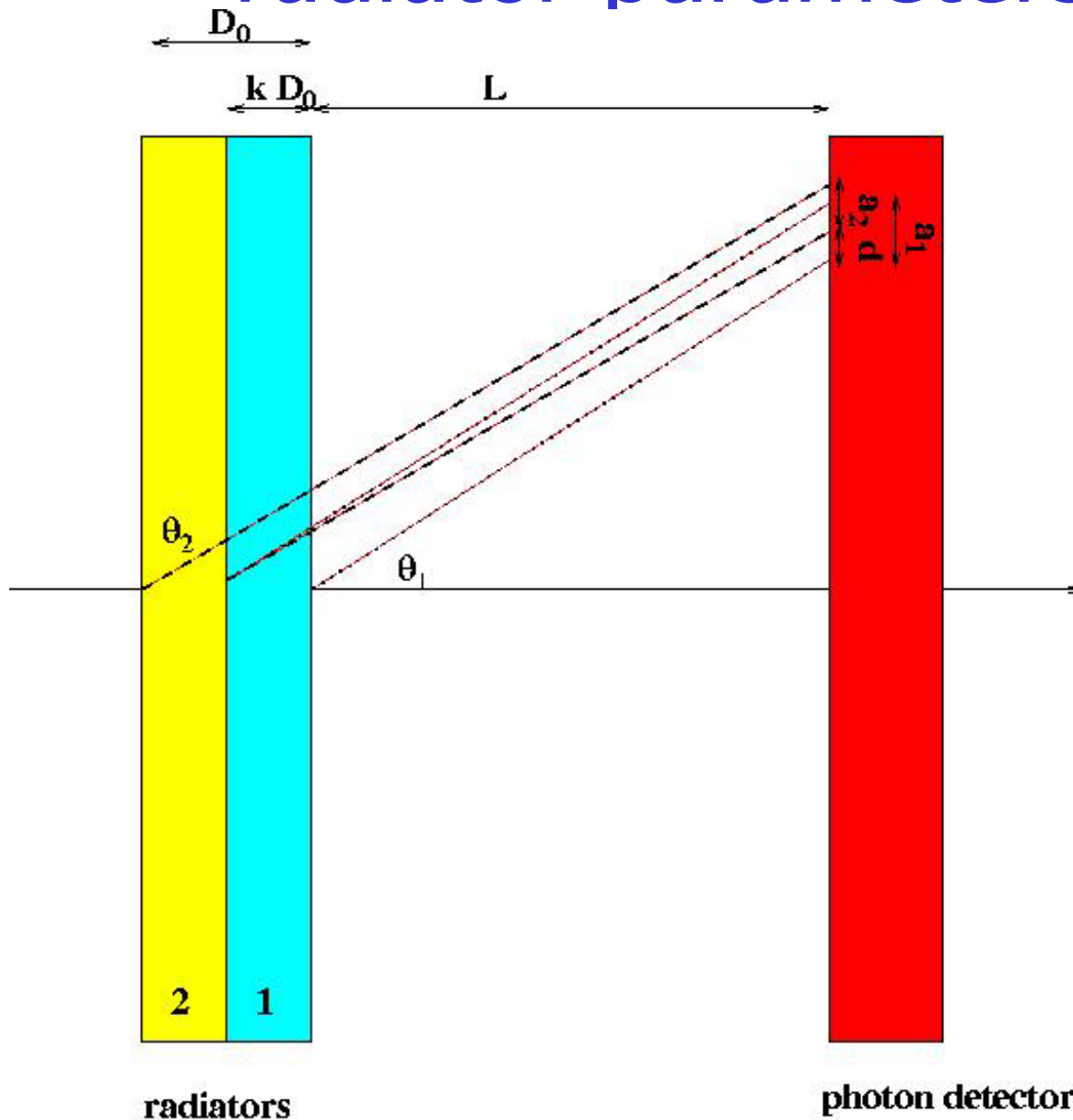


Multiple radiator: Optimisation of radiator parameters - revisited



Dual radiator: three parameters (if fixed space available)

- Difference in n
- Ratio of radiator thicknesses
- Total radiator thickness

Minimized: error per track

$$\sigma_{track} = \frac{1}{\sqrt{N_{det}}} \sqrt{\sigma_{emp}^2 + \sigma_{det}^2 + \sigma_{rest}^2}$$

Distance to photon detector

$$\frac{1}{(L + D0 / 2)}$$

Number of photons

$$\sqrt{\left(\frac{1}{(N1 + N2)} \right)}$$

Emission point error

$$\left(\frac{1}{12 (N1 + N2)^2} \right)$$

$$(-3 (a1 N1 + (a2 + 2 d) N2))^2 +$$

$$4 (N1 + N2) (a1^2 N1 + (a2^2 + 3 a2 d + 3 d^2) N2) +$$

$$\text{pad}^2 / 12 \Big) \Big)$$

Pad size contribution

Now assume $\sigma_{rest} = 0.006$

Minimize track error vs.

Relative radiator thickness k and refractive index difference dn
and total thickness D_0

Transm. length 3cm

$dn=0.0046$

$k=0.43$

$D_0 = 2.7 \text{ cm}$

σ at minimum 0.0047

Transm. length 4.5cm

$dn=0.0053$

$k=0.44$

$D_0 = 3.0 \text{ cm}$

σ at minimum 0.0044

Available space in front of photon detector: 20cm

$\sigma_{\text{rest}}=6\text{mrad}$

Triple radiator

Transm. length 3cm, $\sigma_{\text{rest}}=6\text{mrad}$

dn1=0.0033

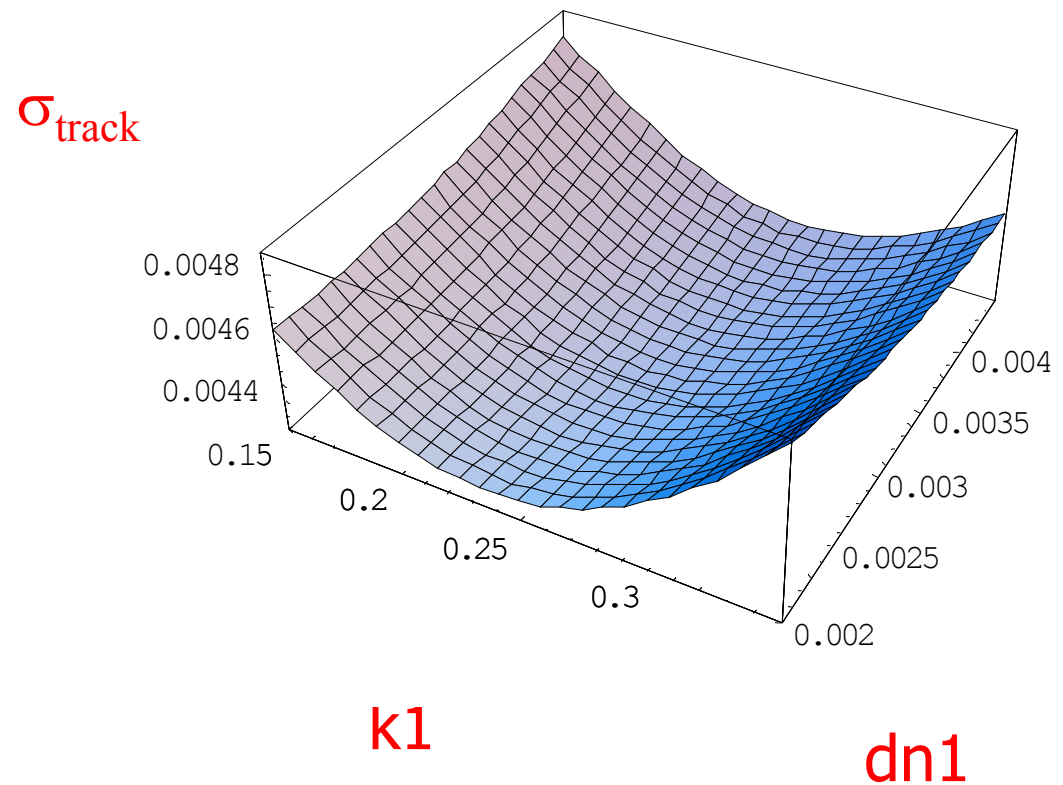
dn2=0.0081

k1=0.25

k2=0.34

$D_0 = 3.4 \text{ cm}$

σ at minimum 0.0043



Quadruple radiator

Transm. length 3cm, $\sigma_{\text{rest}}=6\text{mrad}$

$$\mathbf{dn1=0.0020}$$

$$\mathbf{dn2=0.0062}$$

$$\mathbf{dn3=0.0105}$$

$$\mathbf{k1=0.16}$$

$$\mathbf{k2=0.24}$$

$$\mathbf{k3=0.28}$$

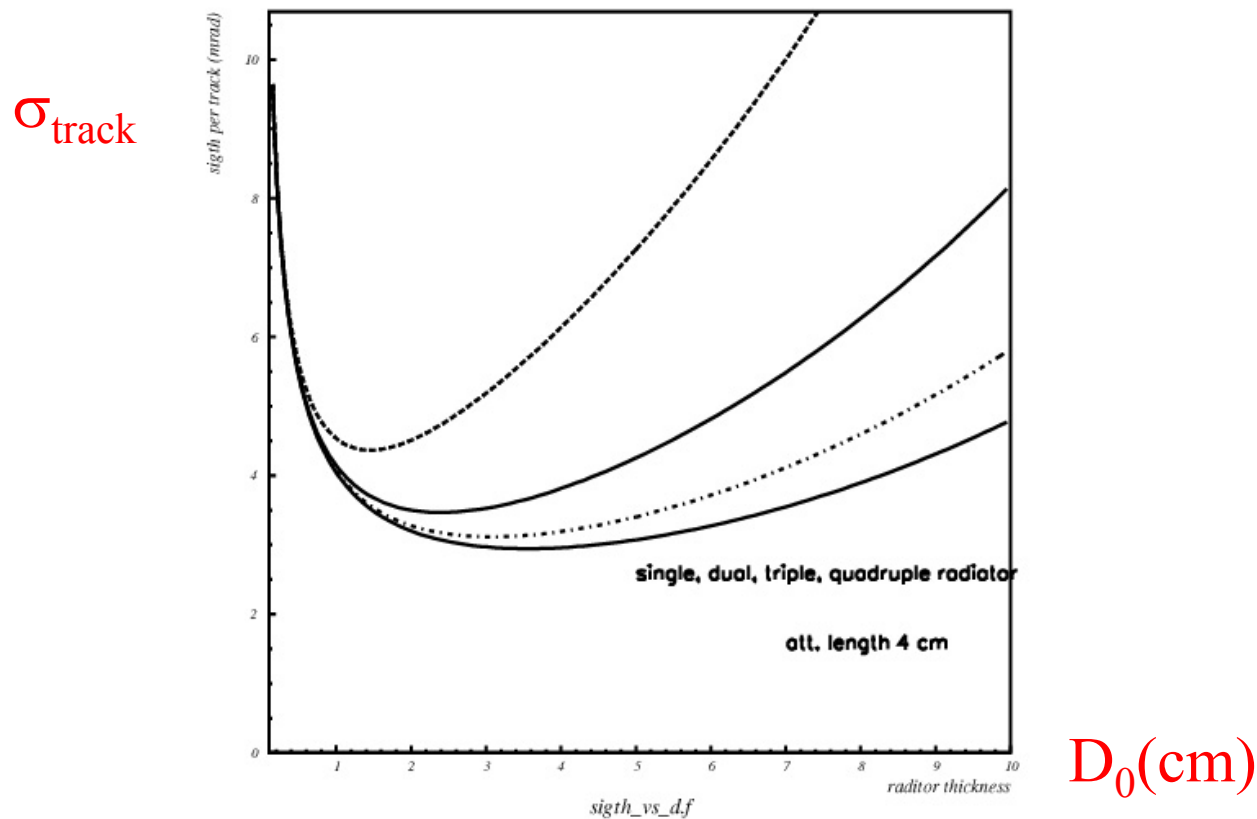
$$\mathbf{D_0 = 3.9 \text{ cm}}$$

σ at minimum 0.0041

Lower ref. index -> smaller emission point error at same thickness-> optimal if upstream radiators thicker

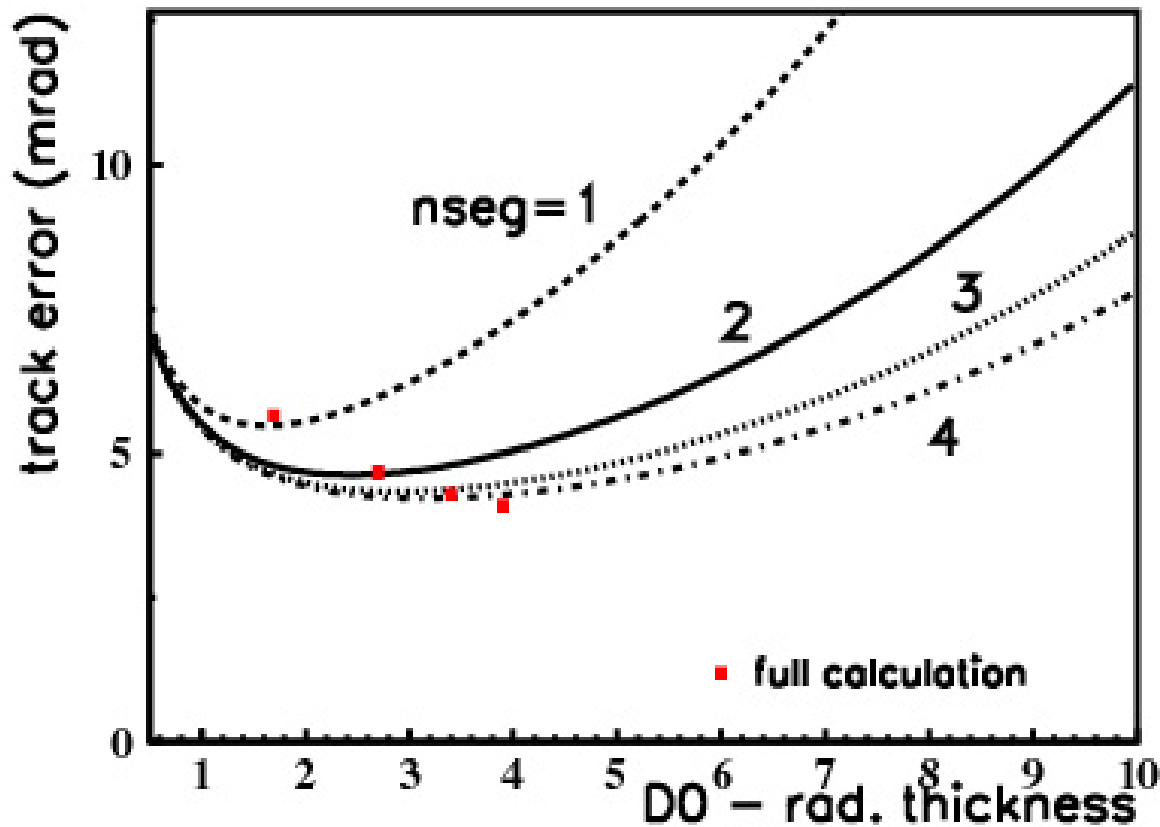
A simple model of what happens when we go from the single layer to focusing multilayer arrangement:

If the indices are well adjusted, the error in emission point goes down by a factor of two in the dual radiator case etc



Simple model

How good is this simple model? Contrast it with the full calculation

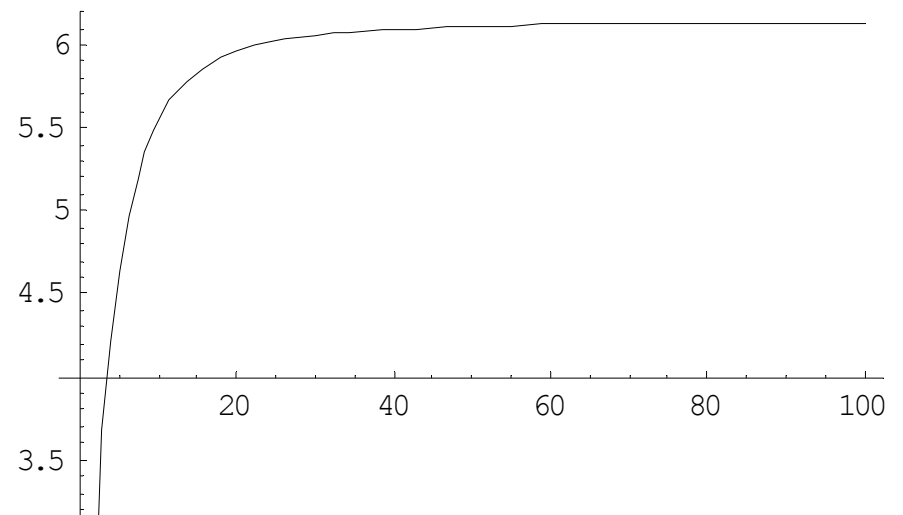
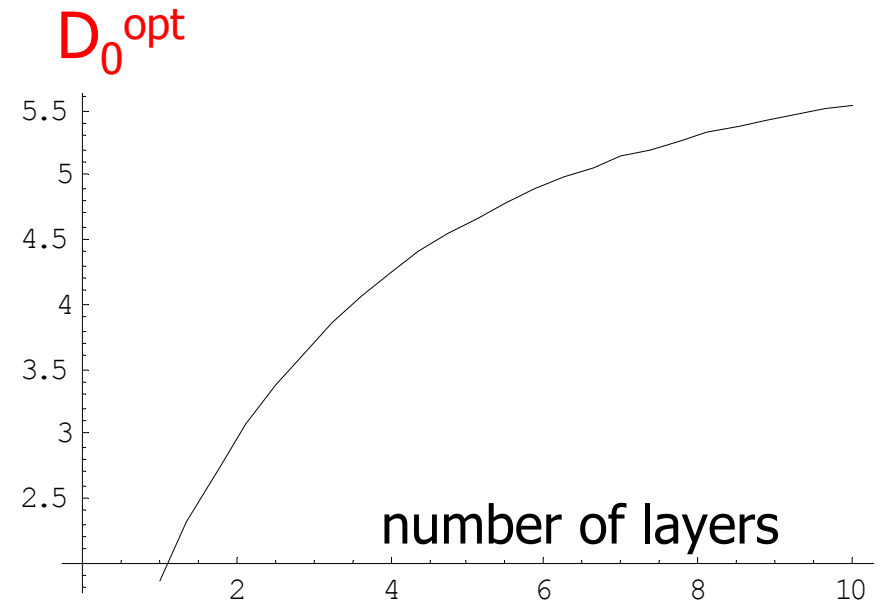


Curves: simple model
Points: full calculation

Half a year later, results revisited.

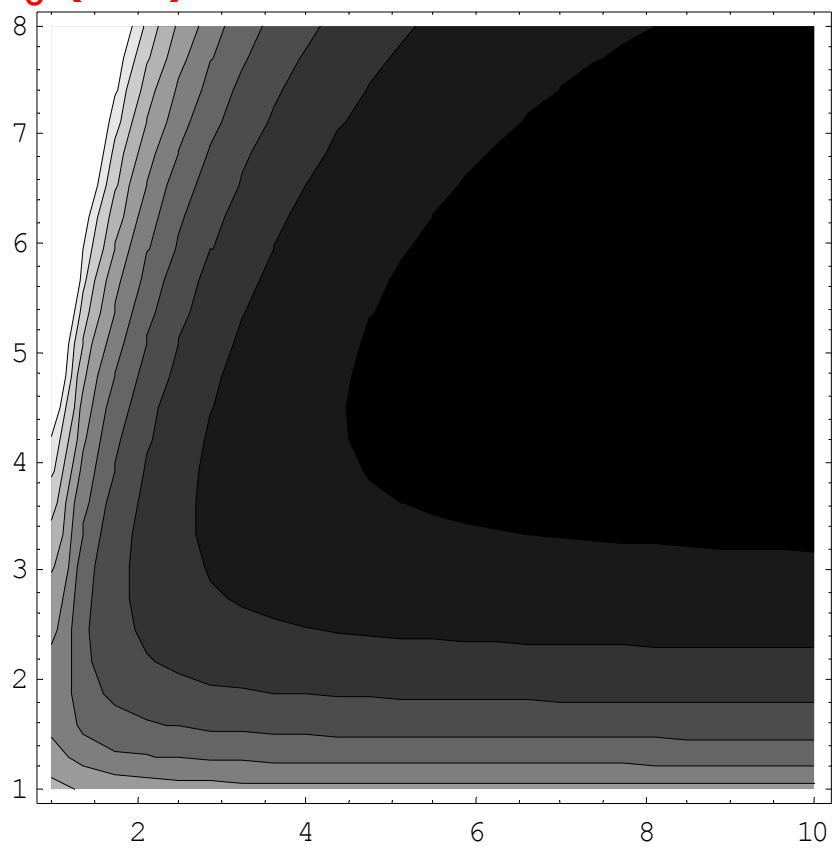
Minimize the expression (sigma per track) vs. to total radiator thickness D , x =number of layers

Plot as a function of the number of layers for standard values:
 $L=4\text{cm}$, $\sigma=7\text{mrad}$,
 $L=20\text{cm}$, $a=0.6\text{cm}$, $\theta=0.3$



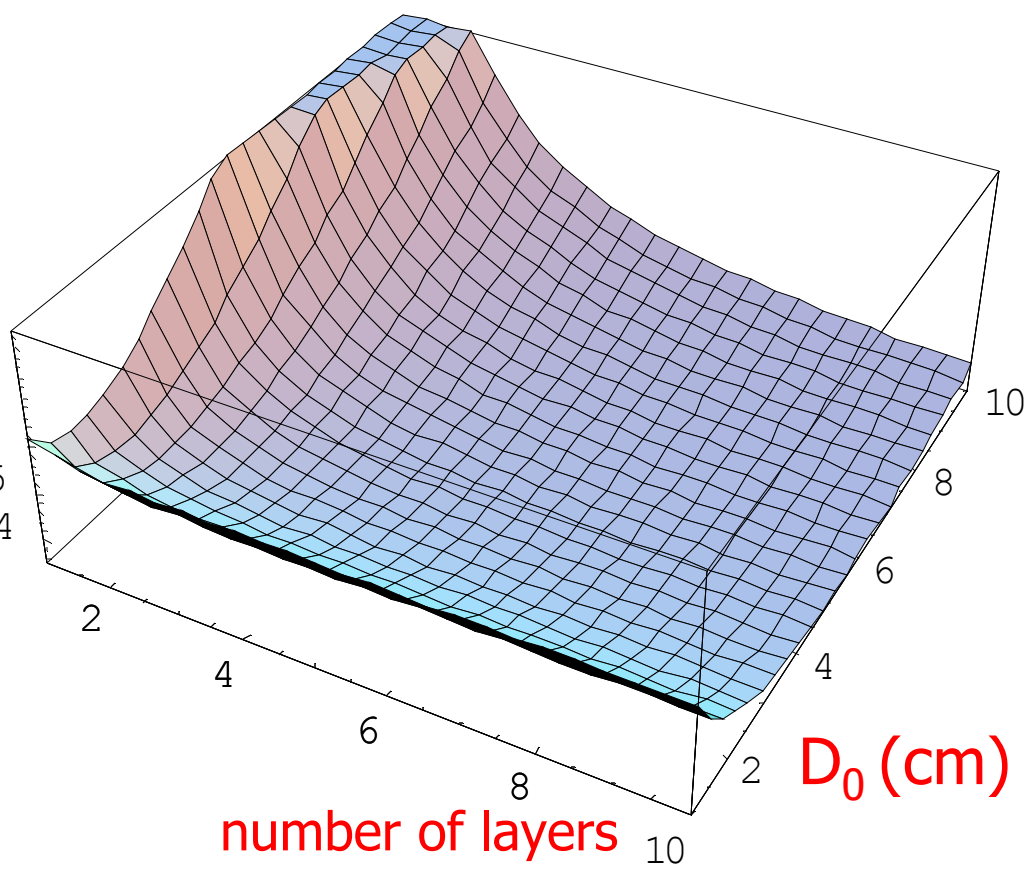
σ_{track} VS
number of
layers and D_0

D_0 (cm)



σ_{track}

0.008
0.007
0.006
0.005
0.004

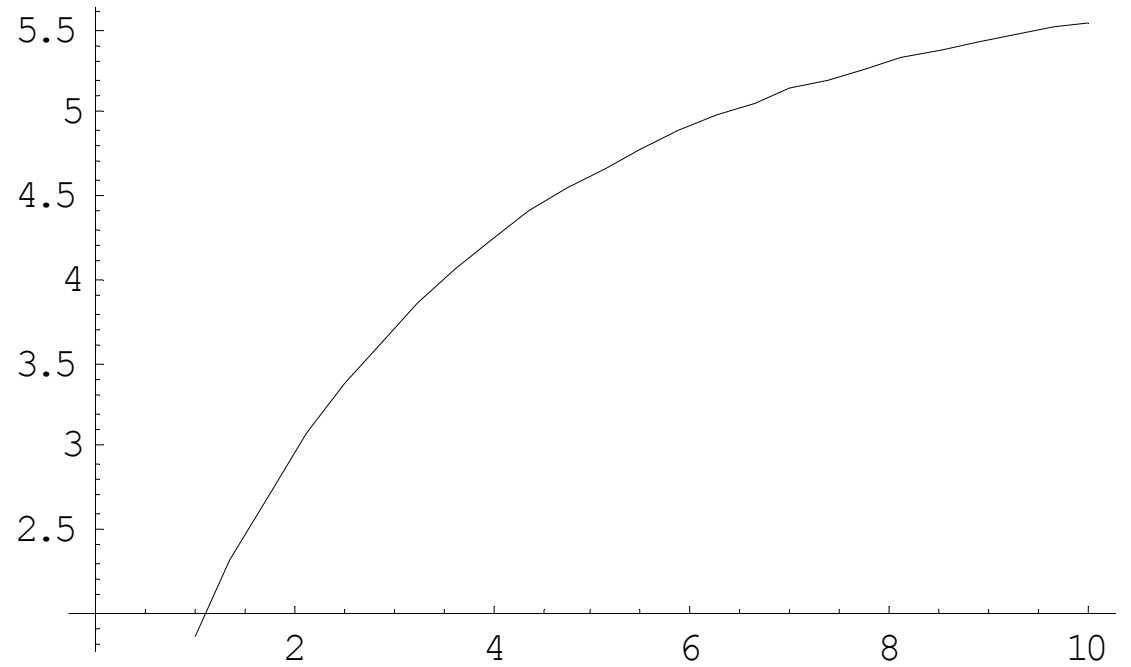
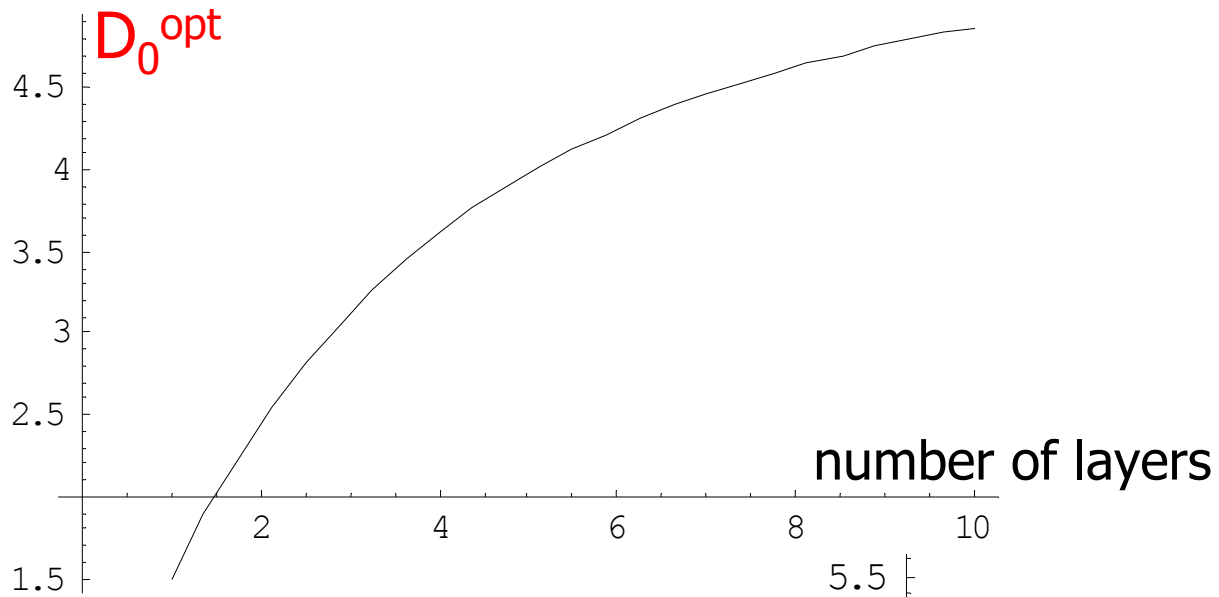


number of layers

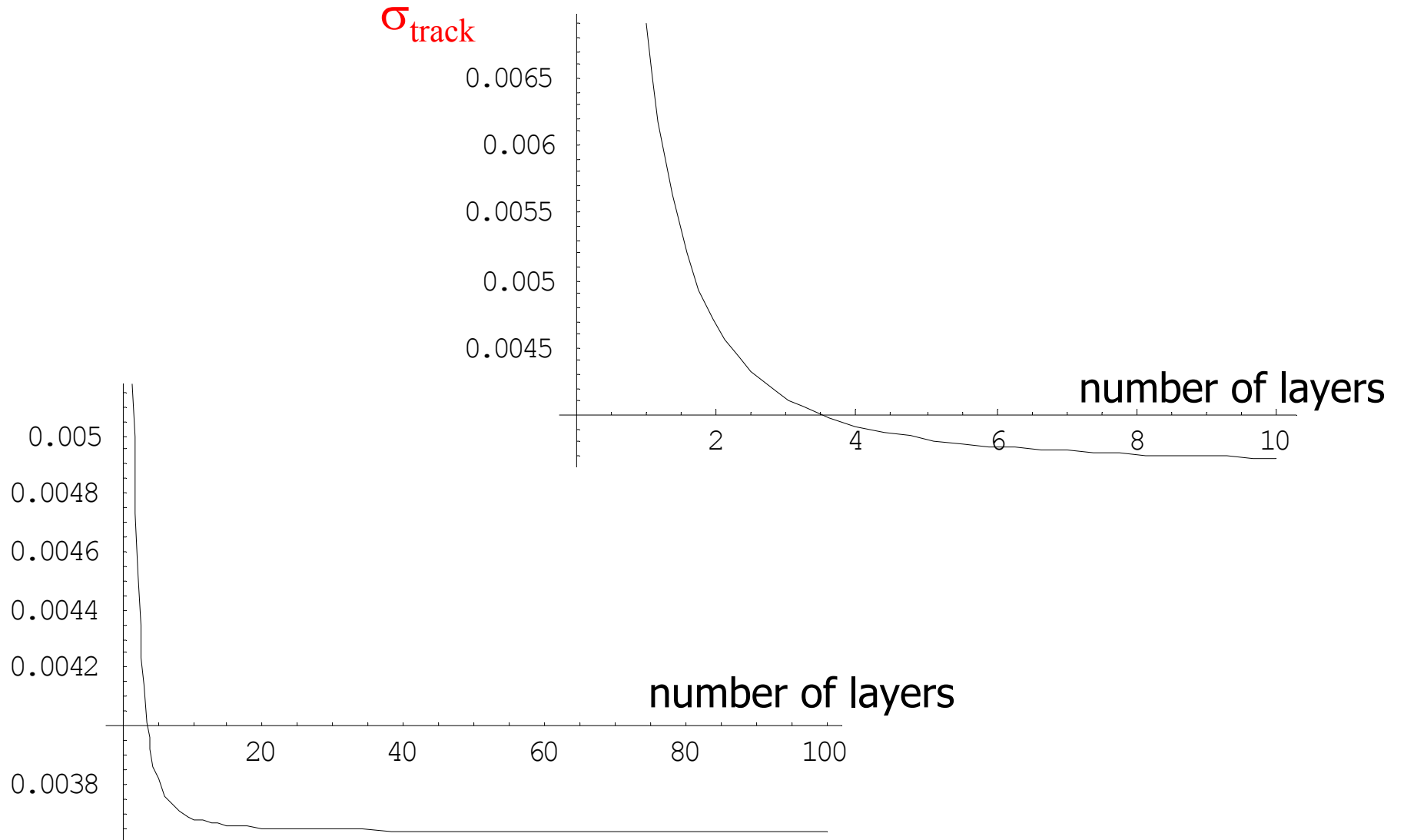
D_0 (cm)

number of layers

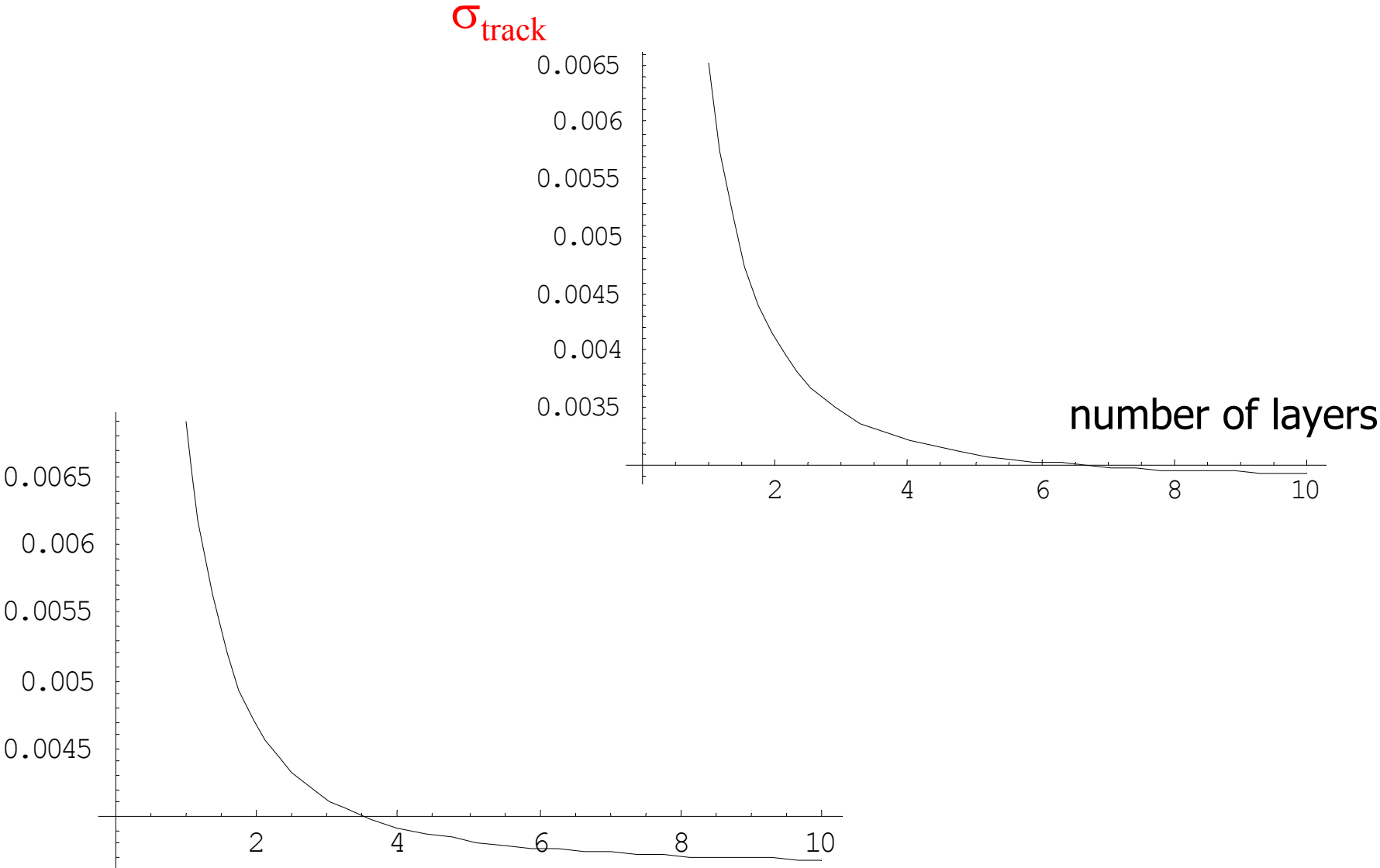
D_0^{opt} for $\text{sigre}=0$ compared to $\text{sigre}=7\text{mrad}$ (bottom right)



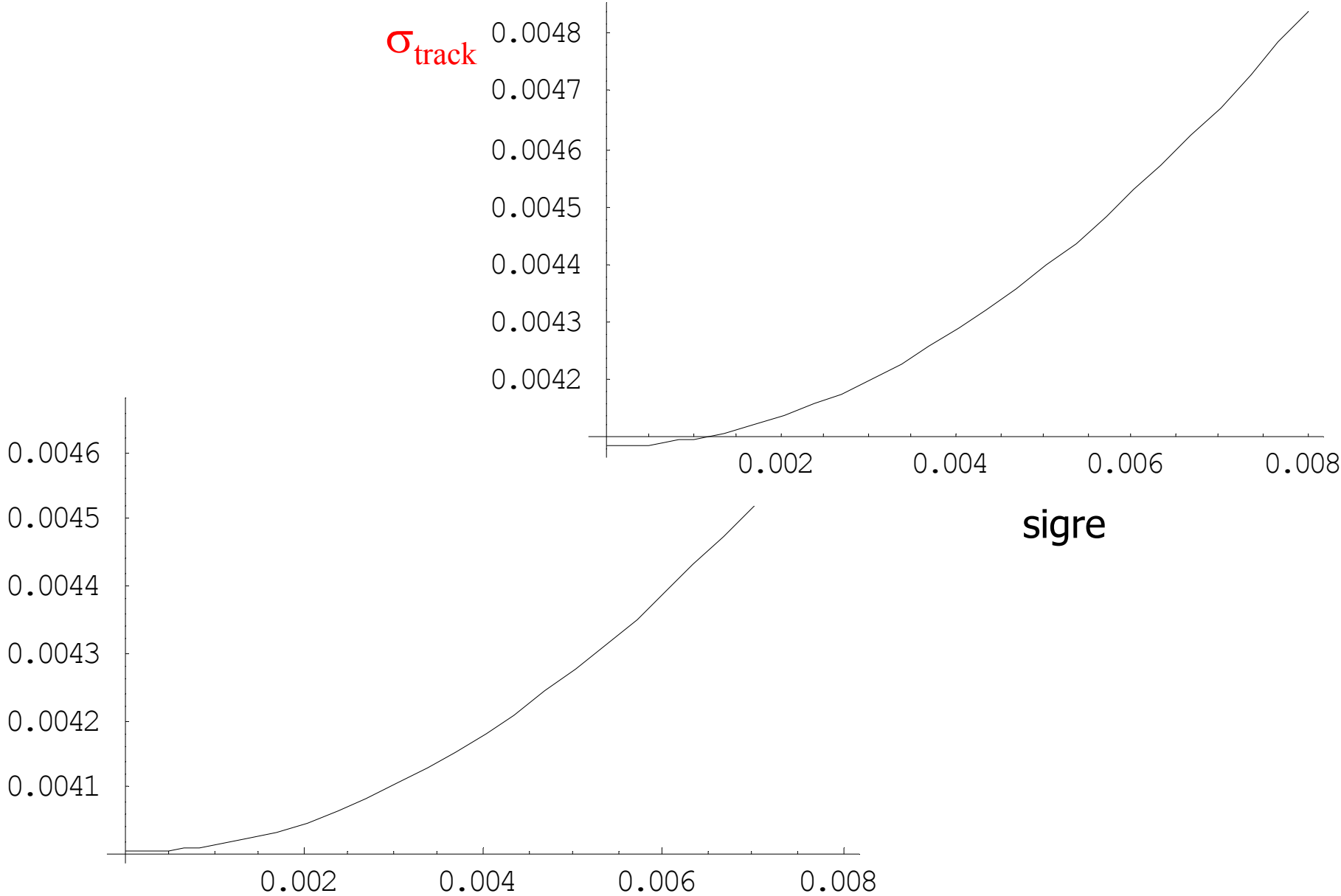
Now fix $D=4\text{cm}$, vary number of layers x



Same, for $\sigma_{\text{sig}}=0$ compared to $\sigma_{\text{sig}}=7\text{mrad}$ (bottom left)



Variation with sigre for 4cm, 2 layers and 6cm, 3 layers (bottom)



Impact of σ_{rest}

At 4cm:

σ_{track} from 4.1mrad \rightarrow 4.8mrad
 $\sigma_{\text{rest}}=0$ $\sigma_{\text{rest}}=8\text{mrad}$

σ_{track} from 4.7mrad \rightarrow 4.1mrad
2 layers 3 layers

\rightarrow Have to understand the origin of σ_{rest} !