

# Prehod nabitih delcev in fotonov skozi snov

## I. Prehod nabitih delcev

- Interakcija delec - snov
- Energijske izgube težkih nabitih delcev
- Energijske izgube elektronov in pozitronov
- Večkratno sipanje
- Energijsko stresanje
- Energijske izgube visokoenergijskih mionov

## II. Prehod fotonov

- Fotoefekt
- Comptonsko sipanje
- Turba parov

## III. EM plaz

### Literatura:

- W. Lee: Techniques for Nuclear and Particle .....
- K. Kleinknecht: Detectors for Particle Radiation
- T. Ferbel: Experimental Techniques in HEP
- W. Heitler: The Quantum Theory of Radiation
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1.1.2018

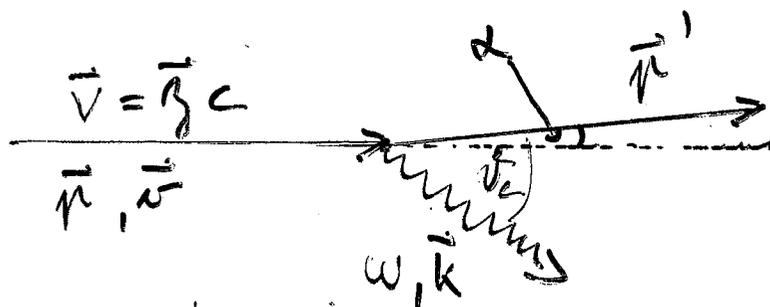
# I Prehod na bitični delec

## a) interakcija delec - snov

delec :  $M$  (masa),  $p$  (gibalna količina),  $v = \frac{p}{m}$  (hitrost)

snov :  $\epsilon(\omega) = \epsilon_1(\omega) + i \epsilon_2(\omega)$  (vitalni deli, viktualni deli, ohmitiv energije)

$$\omega^2 = \frac{k^2 c^2}{\epsilon} \quad (1)$$



$$\vec{p} = \vec{p}' + \hbar \vec{k}$$

$$E = E' + \hbar \omega$$

$\hbar k \ll p$  (spremenjena energija)

$\hbar \omega \ll E$  :  $\hbar \omega = \Delta E = \hbar \frac{\Delta p}{E} = v \Delta p$

$$\vec{p} - \vec{p}' = \Delta \vec{p} = \hbar \vec{k} \quad | \cdot \vec{v} \Rightarrow (\vec{p} - \vec{p}') \cdot \vec{v} = p v - p' v \cos \alpha$$

$$\Rightarrow \hbar \vec{k} \cdot \vec{v} = \hbar \omega$$

$\approx \hbar v \Delta p$   
Za majhne kote

$$\omega = v \Delta p \cos \frac{\alpha}{2}$$

čerenkov radijacija

$$(2)$$

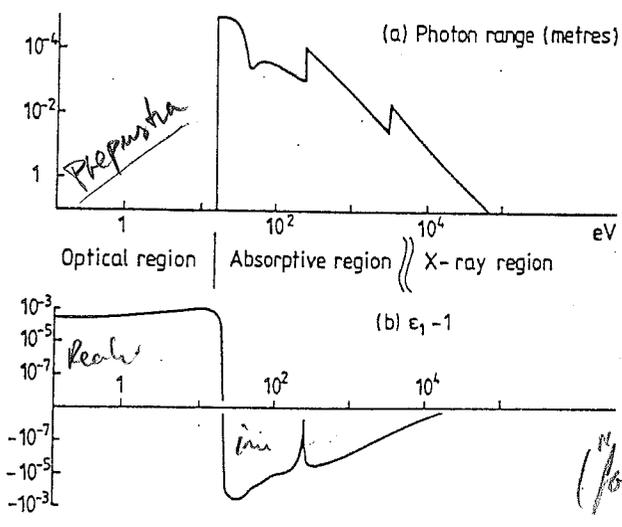
iz (1) in (2)

$$\frac{c^2}{\epsilon} = v^2 \cos^2 \frac{\alpha}{2}$$

$$\sqrt{\epsilon} \frac{v}{c} \cos \frac{\alpha}{2} = 1$$

2 parametri snov in delec (3)

# Odnosnost $\epsilon(\omega)$



$\epsilon_2$

iz dielektričnosti dobimo lomni količnik

$\epsilon_1 - 1$

( $\mu_0 \mu''$ )

Fig.3. The dependence of  $\epsilon$  for argon at normal density on photon energy.  
 a) imaginary part expressed as a range and  
 b) real part - 1 on a split log scale.

tri območja

a) optično  $\epsilon_2 = 0$   $\epsilon_1 > 1$   
 $h\nu < 2eV$

$n \geq \frac{c}{v} \Rightarrow v_c$  realen  $\Rightarrow$  sevanje Čerenkova

b) absorbtivno  $\epsilon_2 > 0$   $\epsilon_1 < 1$   
 $2eV < h\nu < 5 keV$

absorbira virtualnih fotonov  $\rightarrow$  ionizacija  
 vzbujanje

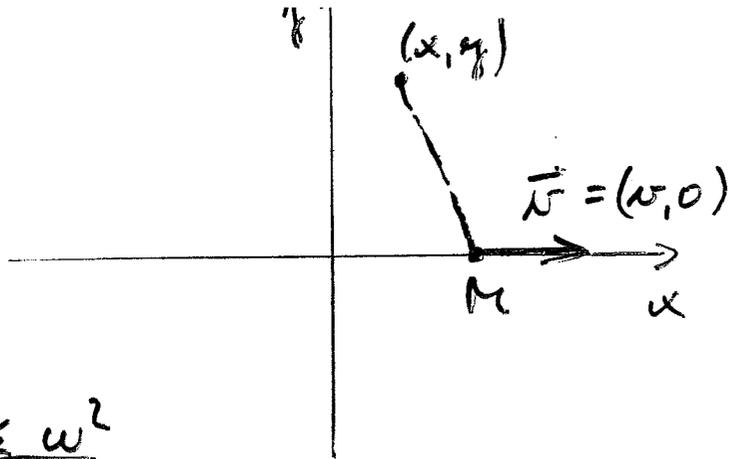
c) rentgensko  $\epsilon_2 \ll 1$   $\epsilon_1 \approx 1$   
 $h\nu > 5 keV$   $\times$  tvoj

malo ionizacije (s-elektroni)

sevanje na prehodih snovi  $\rightarrow$  prehodno sevanje

iz (2)

$$n k_x = \omega$$



iz (1)

$$k^2 = k_x^2 + k_y^2 = \frac{\omega^2}{c^2}$$

$$\Rightarrow k_y = \frac{\omega}{c} \sqrt{\frac{c^2 n^2}{\omega^2} - 1}$$

transverzalna komponenta  
izsevanega fotona

vpeljimo:  $c_m = \frac{c}{\sqrt{\epsilon}}$ ;  $\beta' = \frac{v}{c_m}$ ;  $\gamma' = \frac{1}{\sqrt{1-\beta'^2}}$

$$k_y = \frac{\omega}{c} \sqrt{\beta'^2 - 1} \tag{4}$$

območji  $\beta' > 1$   $k_x, k_y$  realna.

črtaor sramje  $\rightarrow$  sevanje.  $e^{i(\vec{k}\vec{r} - \omega t)}$   
(transverzali del je realen)

$\beta' < 1$   $k_y$  imaginaren, pelje.

transverzali dušeno v transverzalni smeri

del je imaginarna  $e^{i(\vec{k}\vec{r} - \omega t)} = e^{i\omega(\frac{x}{v} - t)} e^{-\frac{y}{\lambda_0}}$   
kar je dobljeno v transverzali smeri:

$$\lambda_0 = \frac{v}{\omega} \frac{1}{\sqrt{1-\beta'^2}} = \frac{\beta' \gamma'}{k} \tag{5}$$

doseg narašča  $\approx \beta' \gamma'$   $\rightarrow$  relativistični drog

$\approx \beta' \gamma'$

$$\lambda_0 = \frac{v}{k} \frac{1}{\sqrt{\frac{1}{\gamma'^2} + (1-\beta'^2) \beta'^2}} \tag{6}$$

optično :  $\epsilon > 1$   $\gamma' \rightarrow 1 \Rightarrow \gamma_0 \rightarrow \infty$  Čerenkov

svetlobna  
hitrost

$\epsilon < 1$

$\gamma_0$  naraste.  $\approx \gamma$

$\gamma_{0, \text{max}}$  doseg =  $\frac{1}{k \sqrt{1-\epsilon}}$  (2)

nasičenje od  $\frac{1}{\gamma^2} \sim (1-\epsilon) \gamma^2 \Rightarrow \gamma \sim \frac{1}{\sqrt{1-\epsilon}}$

$1-\epsilon$  susceptibilnost  $\propto \rho$

nasičenje  $\gamma \sim \frac{1}{\sqrt{\rho}}$

večja gostota, manjši  $\gamma$

večja gostota  $\rightarrow$  prej do nasičenja  
 $\rightarrow$  manjši relativistični dvig

plini  $1,3 \rightarrow 1,7$  (Xe)

emulzije  $1,15$

polvodniki  $1,1$

plastični scint.  $1,01 - 1,02$

# interakcija (virtualnih) fotonov z atomi - fotoabsorpcijski ionizacijski model

dit. presek na posameznem elektronu v atomih v snovi

$$\frac{d\sigma}{dE} = \frac{\alpha}{\pi f^2} \frac{\sigma_p(E)}{E z} \ln \frac{1}{(1 - \epsilon_1^2 f^2)^2 + \epsilon_2^2 f^2} + (a)$$

$$+ \frac{\alpha}{\pi f^2} \frac{\sigma_p(E)}{E z} \ln \left( \frac{2 \pi m_e c^2 f^2}{E} \right) + (b)$$

$$+ \frac{\alpha}{\pi f^2} \frac{1}{E^2} \int_0^E \frac{\sigma_p(E')}{z} dE' + (c)$$

$$+ \frac{\alpha}{\pi f^2} \frac{1}{N h c} \left( f^2 - \frac{\epsilon_1}{k_0 f^2} \right) + (d)$$

↑ vzbujanje  
← ionizacija

Rutherfordovo sipanje + (c)

Čerenkov (prehodno sevanje) (d)

$\sigma_p(E)$  - fotoabsorpcijski presek - glej II. poglavje

$\epsilon$  - faza izraza  $1 - \epsilon_1 f^2 + i \epsilon_2 f^2$

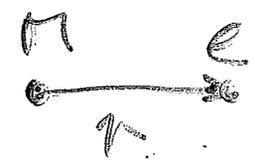
- (a), (b) - vzbujanje, ionizacija
- (c) - Rutherfordovo sipanje →  $\delta$ -elektroni
- (d) - Čerenkov + prehodno sevanje  
( $\theta: 0 \rightarrow \pi$ )  
Prag

b) energijske izgube težkih nabitih delcev<sup>+</sup>

težki : vsi razen  $e^{\pm}$

trki z elektroni - najhuda sprememba energije  
 - veliko tokov ( $\Gamma \sim 10^{14} \text{ cm}^{-2}$ )

maksimalni prenos energije



$$T_{max} = \frac{2 \cdot Z^2 \cdot m_e \cdot c^2 \cdot f_p^2}{1 + 2Z \frac{m_e}{M} + \left(\frac{m_e v}{M}\right)^2} \quad (9)$$

↑  
za visoke E!

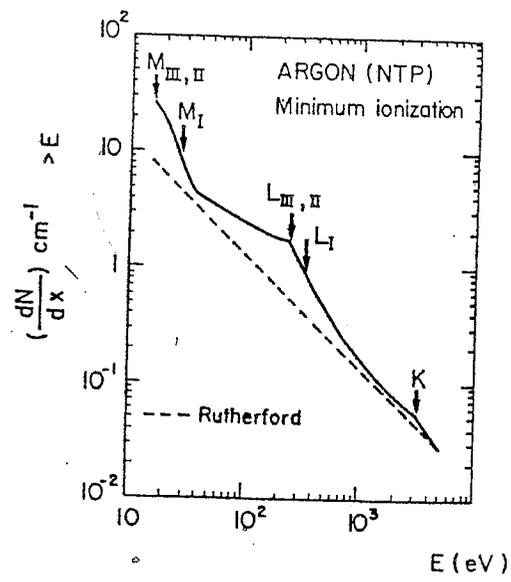


Figure 1 Collisions per unit length, in argon at NTP, with an energy transfer  $\geq E$  as a function of the energy (1).

minimalni prenos energije

$T_{min} \sim E_{eksc}$

# Bethe - Blochova enačba

- smer  $M$  konstantna
- elektron miruje

dobimo je tudi z integracijo enačbe (8) po prenosih energij med  $I$  in  $T_{max}$

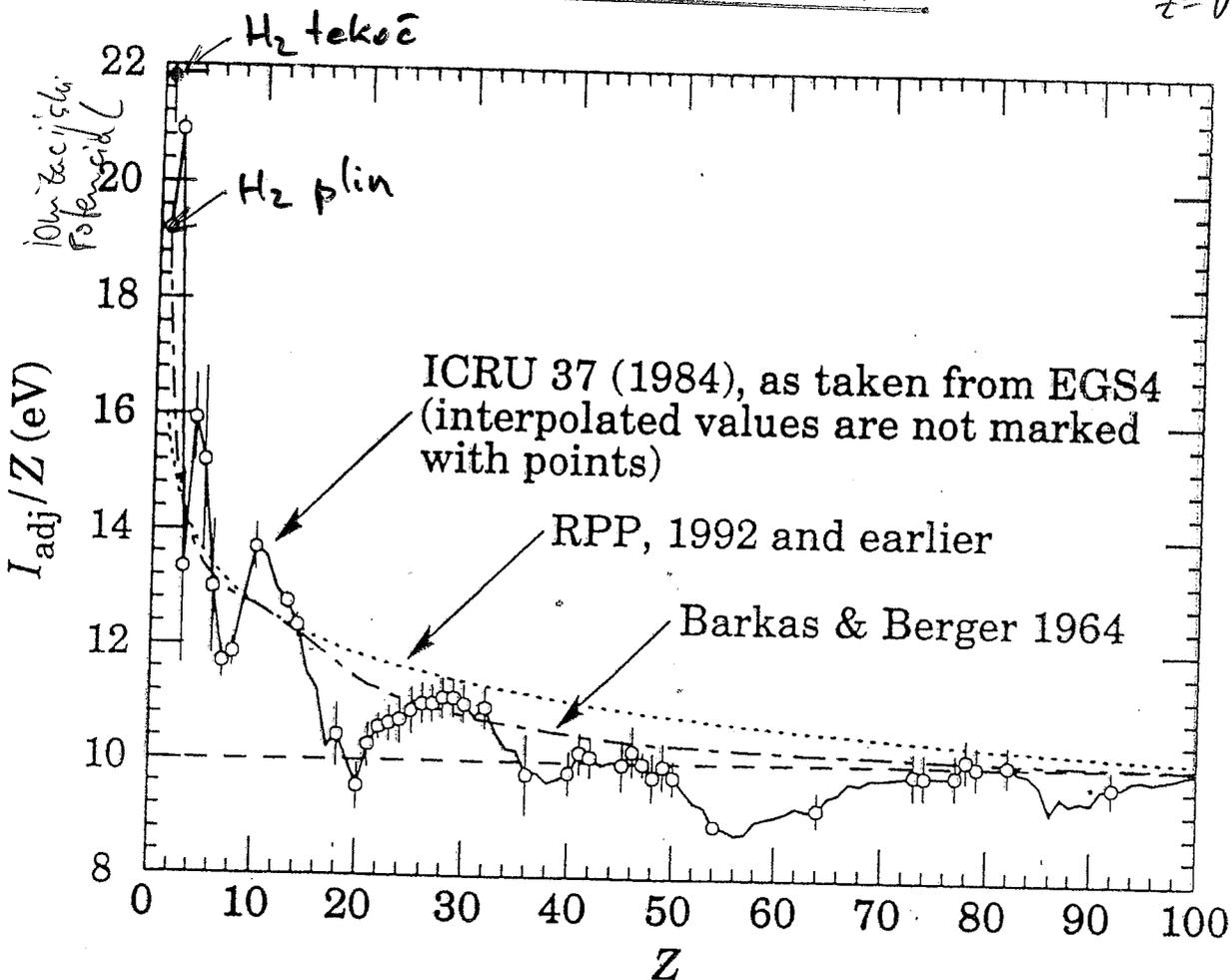
Opisuje povprečne izgube energije težkih delcev v snovi

$I$  - povprečni ionizacijski potencial

$$\frac{I}{Z} \approx 10 \text{ eV}$$

(10)

$Z$  = vrstno število



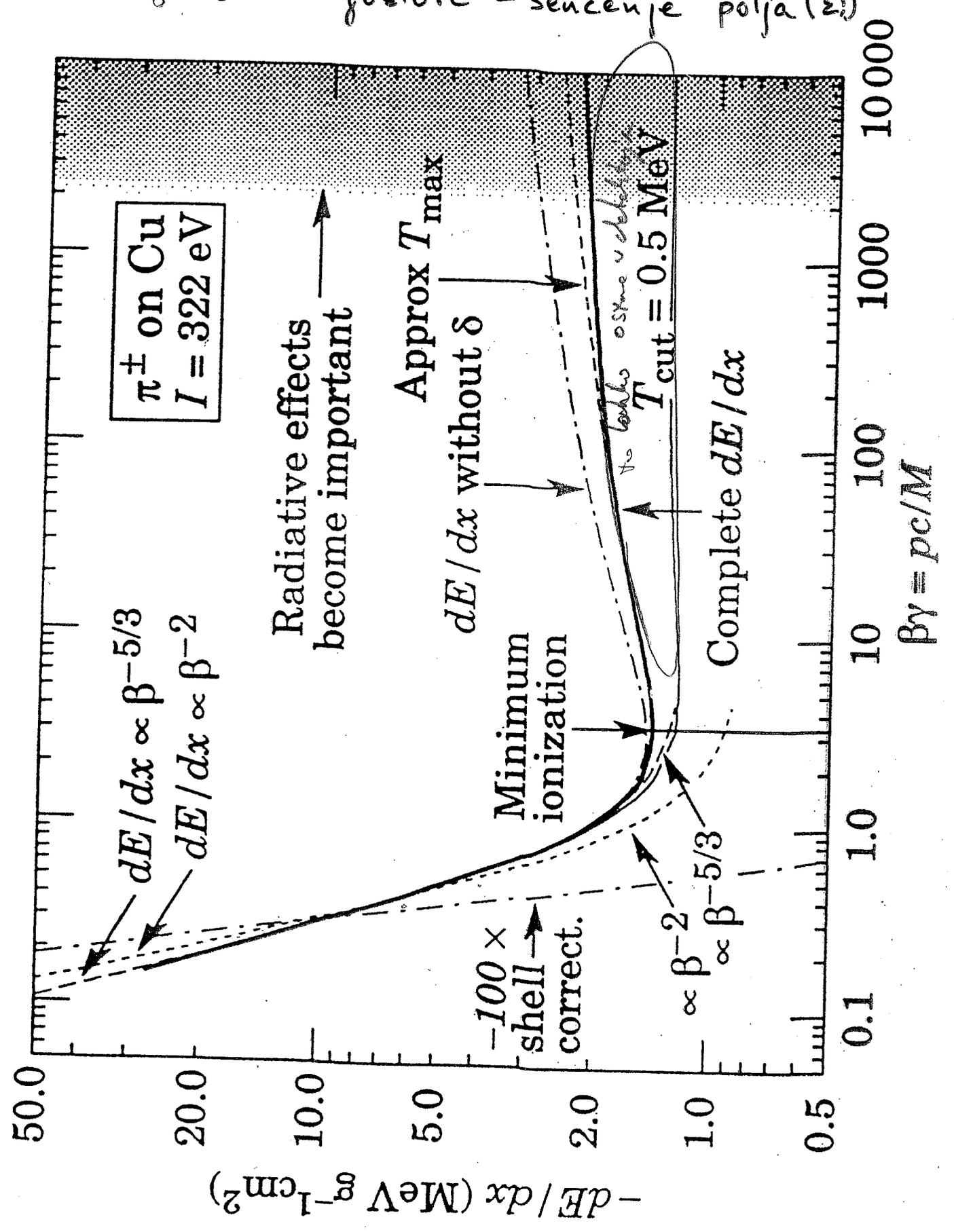
bolj natančno  $\rightarrow$  tabele

$$-\frac{dE}{dx} = k \frac{Z^2}{\beta^2} \frac{1}{A} \left[ \frac{1}{2} \ln \frac{2 m_e c^2 \beta^2}{I} + T_{max} \right] \quad (11)$$

Povprečna ionijska energija ionitacije  
 2. max. e. h.  $T_{max}$

$$k = 4\pi N_A r_e^2 m_e c^2 = 0.307 \text{ MeV} \frac{\text{cm}^2}{\text{g}}$$

$\delta$  - efekt gostote - senčenje polja (E!)



*Zovotno, servezic  
n shouvi,*

*Miobh (informacija o prvotni metalaji)*

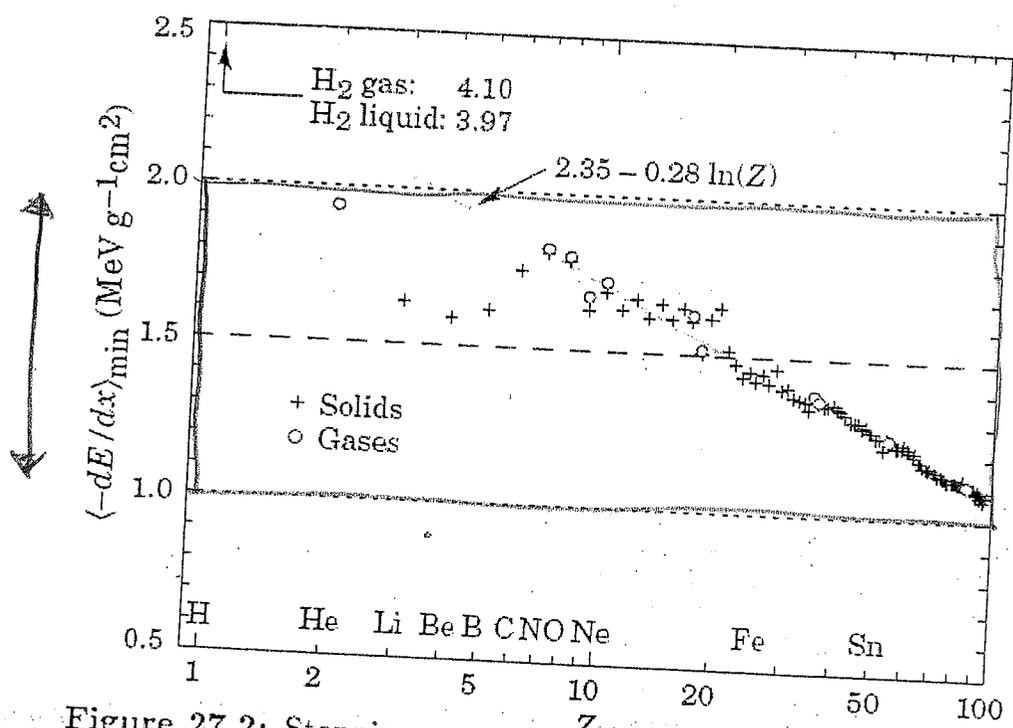
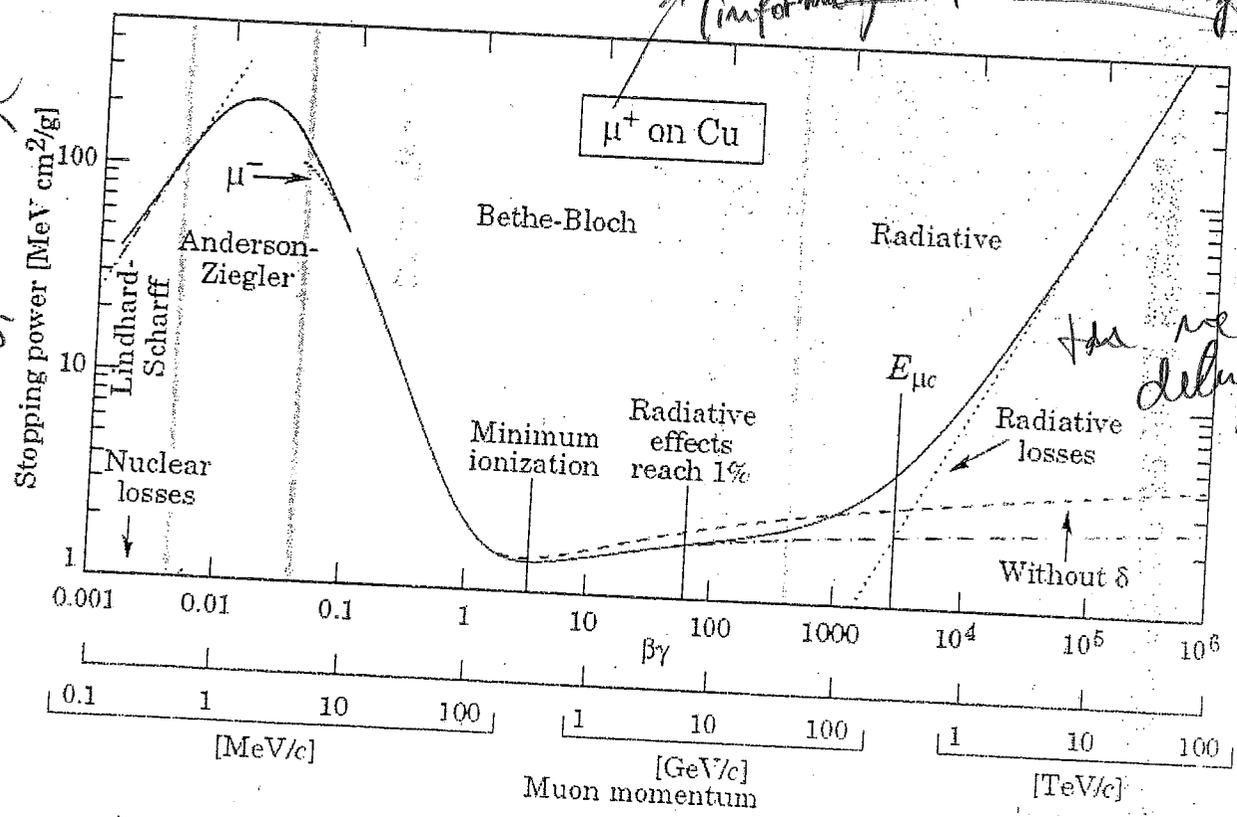


Figure 27.2: Stopping power at minimum ionization for the chemical elements. The straight line is fitted for  $Z > 6$ . A simple functional dependence on  $Z$  is not to be expected, since  $\langle -dE/dx \rangle$  also depends on other variables.

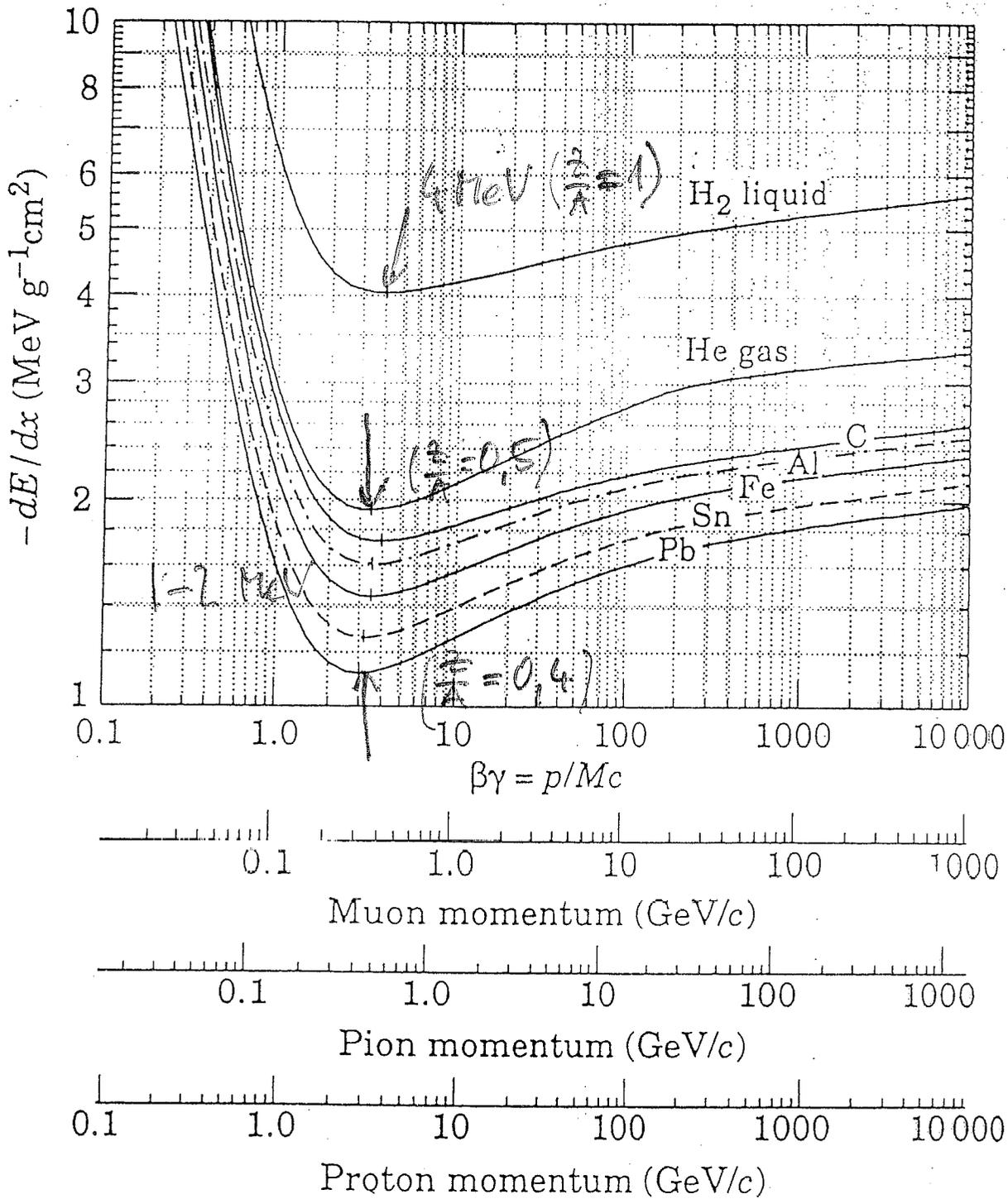


Figure 22.2: Energy loss rate in liquid (bubble chamber) hydrogen, gaseous helium, carbon, aluminum, tin, and lead.

za dan medij  $\rightarrow \frac{dE}{dx} = f(\omega) = g\left(\frac{E}{\hbar\omega}\right) = h\left(\frac{v}{c}\right)$  10

energijska odvisnost

majhni  $\gamma > \frac{2}{137} \rightarrow \frac{dE}{dx} \propto \frac{1}{\gamma^2} \left(\gamma^{-5/2}\right)$

$\gamma \sim 3,5$  širok  
 $\gamma \sim 0,96$  minimum. 1-2. Max  $\frac{c\omega}{\gamma}$

visok:  $\gamma \gg 4$  relati. visticni  
 drvig

- rel. drvig
- počasen  $\sim 2 \ln \gamma \xrightarrow{\gamma \gg 1} \ln \gamma$
  - zmanjšan zaradi gostote  
 $\gamma \gg 1: \delta/2 = \ln(\hbar\omega/\hbar\gamma) + \ln \gamma - 1/2$
  - visokoenergijski elektroni uidejo  
 $\rightarrow$  Fermijeve plati

omejene energijske izgube:  $T < T_{rez}$

$$\frac{-\frac{dE}{dx}}{T_{rez}} = k \frac{Z^2}{A} \frac{Q^2}{\gamma^2} \frac{1}{\gamma^2} \left[ \frac{1}{2} \ln \frac{2 \omega_{max}^2 \gamma^2 T_{max}}{I^2} - \frac{1}{2} \right] \quad (12)$$

$T_u = \min(T_{rez}, T_{max})$  ~deponirana energija

deponirana energija ~ delotraj

EBS program

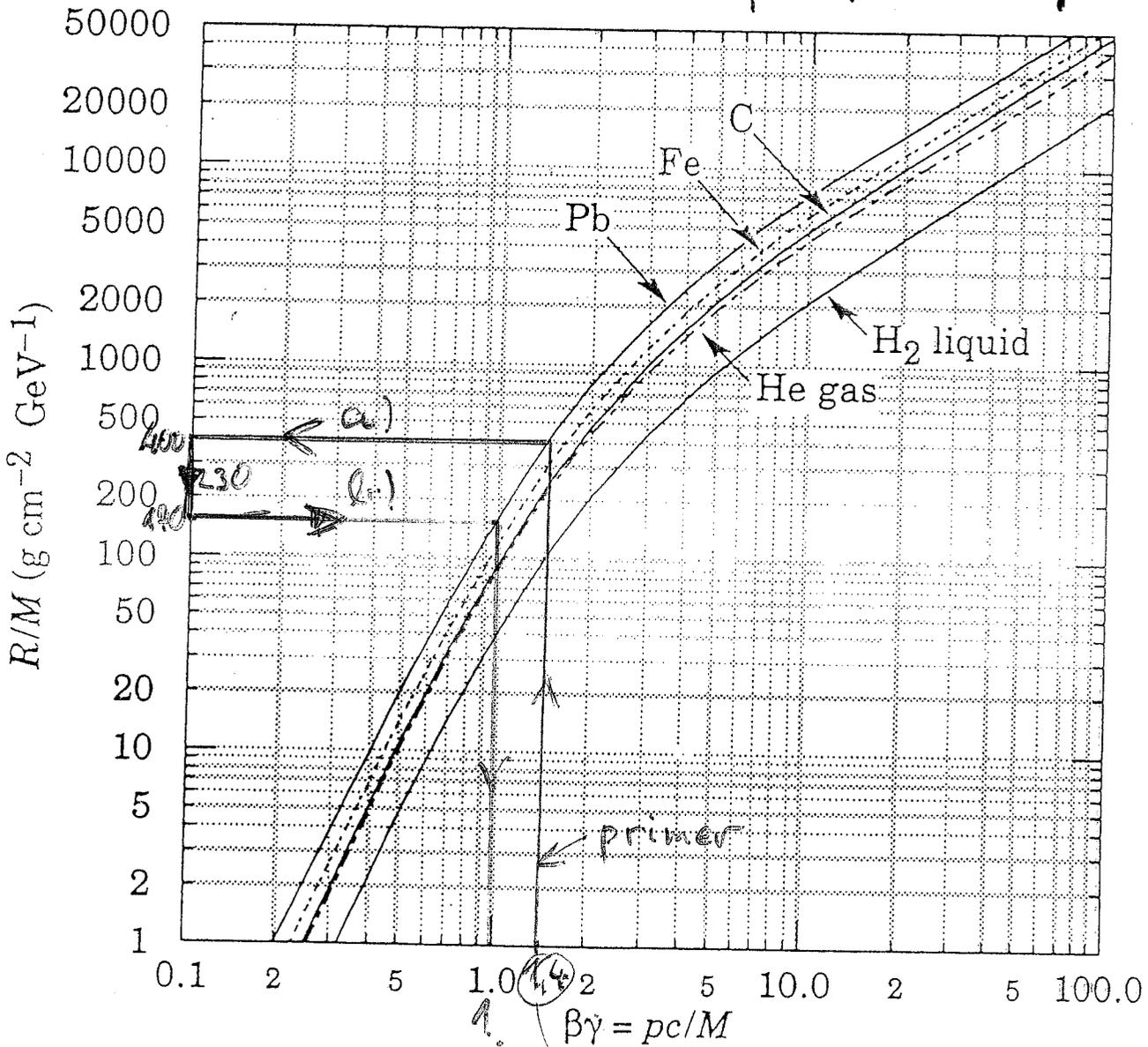


doseg

Befe-Bloccer (odvisen od hitrosti in mase) (15)

$$R(E) = \int_E^{\infty} \frac{dE}{(dE/dx)}$$

v resnici je to pot delca, toda sipanje le malo pokvari relacijo pot = doseg



zveza

$$R_a(M_a, z_a, \left\{ \begin{matrix} p_a \\ T_a \end{matrix} \right\}) = \frac{M_a z_a^2}{M_b z_b^2} R_b(M_b, z_b, \left\{ \begin{matrix} p_b \\ T_b \end{matrix} \right\}) = \left\{ \frac{p_b}{p_a} \right\} \left\{ \frac{T_b}{T_a} \right\} \frac{M_b}{M_a}$$

primer:  $K^+$ ,  $p = 200 \text{ MeV/c}$ , Pb:  $p \Rightarrow \beta\gamma = 1.42$ ; Pb:  $R/M = 400$

$d = 11 \text{ cm} \Rightarrow \frac{R}{A} = 230 \Rightarrow R_{\text{Pb}} = 195 \text{ g/cm}^2 \Rightarrow R = 17.4 \text{ cm}$   
 $\Rightarrow R_{\text{H}} = 140 \Rightarrow \beta\gamma = 1 \Rightarrow p = 500 \text{ MeV/c}$

Doseq

Za težke nabite delce

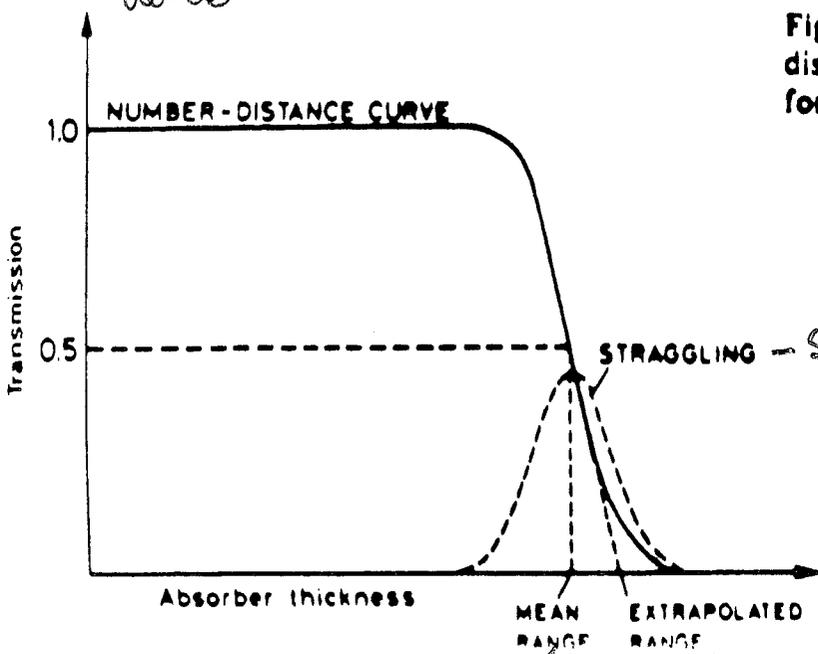


Fig. 2.7. Typical range number-distance curve. The distribution of ranges is approximately Gaussian in form

STRAGGLING - stresanje

↑  
povprečni  
doseq

optično področje  $v > \frac{c_0}{n}$

opis z enačbo (8 d)

$$\cos \theta_c = \frac{1}{\beta n}$$



(12)

$\beta n \geq 1 \rightarrow \theta_c \rightarrow 0$

$\beta \approx 1 \quad \cos \theta_c = \frac{1}{n}$

H<sub>2</sub>O  $n_c = 1.33$

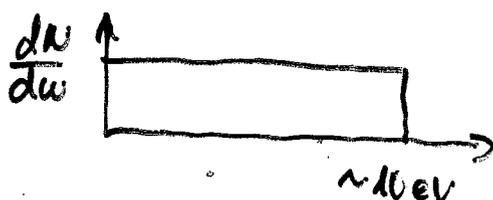
SiO<sub>2</sub>  $n_c = 1.46$

↳ totalni odboj  $\sin \theta_{crit} = \frac{1}{n}$

iz (8):  $\frac{dN}{dE_T} = \frac{d}{hc} \left(1 - \frac{1}{\beta^2 n^2}\right) L \cdot d \cdot \sin^2 \theta_c \cdot L$  (18)

za optično področje

$n(w) \approx \text{konst}$  Snovi



~~število fotonov~~

$\frac{dE}{dx} = \frac{1}{L} \int_{\text{tuo}} \frac{dN}{dE_T} dE_T$  (19)

najhen, za trdno snov  $\approx 10^{-3} \text{ MeV} \frac{\text{cm}^2}{g}$

ali  $\approx 10^3$  fotonov (večina UV)

# c) Energijske izgube $e^\pm$

trki z elektroni v kot teži delci

- veliki odklon it smeri
- identični delci (e)
- $W_{max} = \frac{T_e}{2}$

v Bethe - Bloch

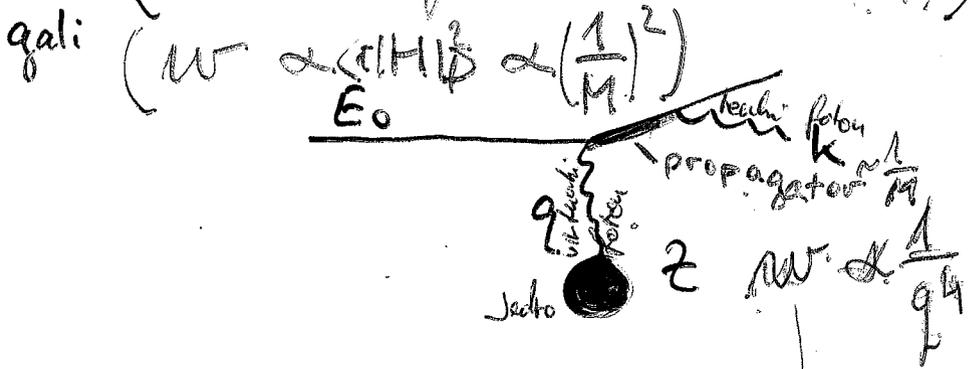
$$\ln \frac{2 m_e c^2 \beta^2 \gamma^2 T_{max}}{I^2} \rightarrow \ln \frac{\beta^2 (\gamma + 2)}{2 (I / m_e c^2)^2}$$

$$\beta = \frac{v}{c}$$

$$-\beta^2 \rightarrow F(\beta) \text{ (Leo str. 35)}$$

lahki delci zavorno sevanje

zama-gali  $(W \propto \mu^2 \propto \frac{1}{M})$  za  $\mu \sim 40000$  manjša



verjetnost izsevanja

sevanje jedra z atomskimi elektroni

najuglednejši q pada z energijo

→ dlja stran → večje sevanje

za  $E_0 > 1.37 \text{ MeV}$   $Z^{1/3}$  popolno senčenje 15

$$\underline{E = E_0 e^{-\frac{x}{X_0}}} \quad (20)$$

$X_0$  - <sup>attenuacijska dolžina</sup> radiacijska dolžina

$$\underline{\frac{1}{X_0} \approx \frac{4Z^2 \rho N_A}{A} \cdot r_e \cdot \ln(1.83 Z^{-1/3})} \quad (21)$$

$$\underline{\frac{1}{X_0} \propto \frac{Z^2}{A}} \quad \begin{matrix} Z^2 \Rightarrow \text{jedro} \\ \text{hole block} \Rightarrow \text{elektroni} \end{matrix} \quad (22)$$

primeri

	$\rho X_0$	$X_0$
C	42,7 g/cm <sup>2</sup>	18,8 cm
Pb	6,37 g/cm <sup>2</sup>	0,56 cm
W	6,76 g/cm <sup>2</sup>	0,35 cm

efekt zavornega sevanja na elektrnih

$$Z^2 \rightarrow Z(Z+1)$$

RPP '96: radiacijska dolžina

$$\underline{\rho X_0 = \frac{16,4 \cdot \rho \cdot A}{Z(Z+1) \ln(204/\sqrt{Z})}} \quad (23)$$

napaka  $\pm 2,5\%$

kritična energija

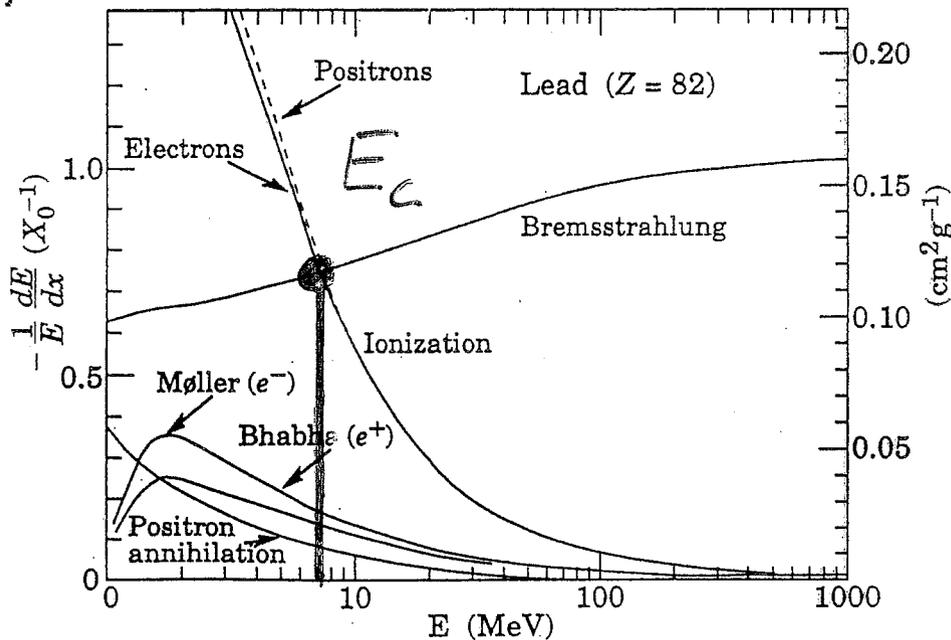
$$\left(\frac{dE}{dx}\right)_{trki} = \left(\frac{dE}{dx}\right)_{rad.}$$

$$E_c \sim \frac{800 \text{ MeV}}{Z + 1,2} \quad (24)$$

Pb  $\sim 9,5 \text{ MeV}$       Al  $\sim 51 \text{ MeV}$

RPP 196 plini  $\leftrightarrow$  tekočine + trdne (I!)

drugačnja definicija plin T+T. 710 MeV / (Z + 0,92) Pb  $\sim 9,5 \text{ MeV}$   
 610 MeV / (Z + 1,24)



Izgube pri elektronih

- trki (zavono sevanje)
- sevalne izgube

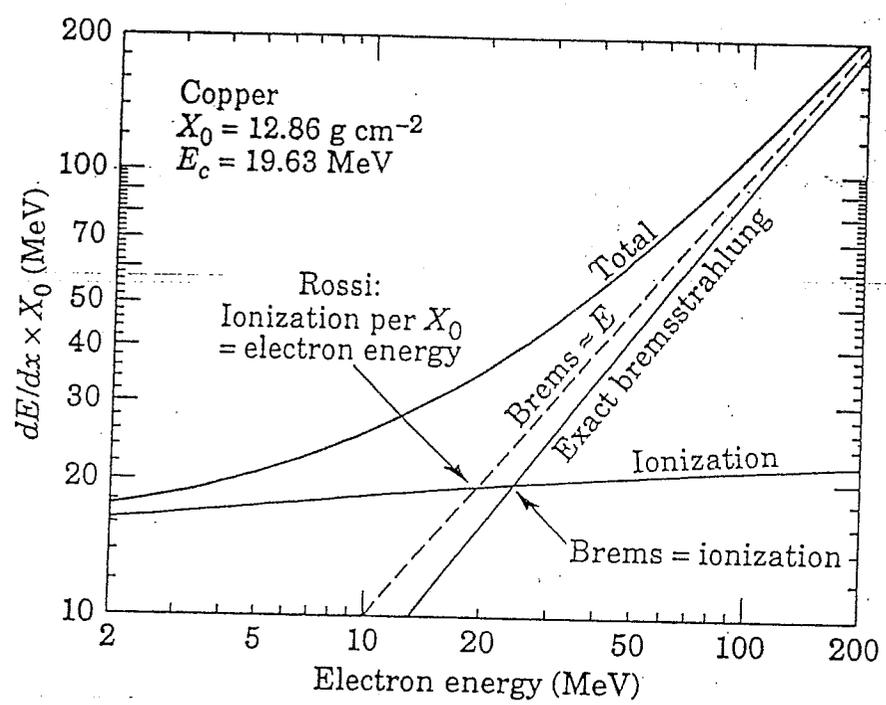


Figure 22.6: Two definitions of the critical energy  $E_c$ .

"nova" (Rossi 1952!) definicija  $E_c$

$$\left(\frac{dE}{dx}\right)_{ion} \cdot X_0 = E (= E_c)$$

definiciji identični za  $\left(\frac{dE}{dx}\right)_{brems} = \frac{E}{X_0}$

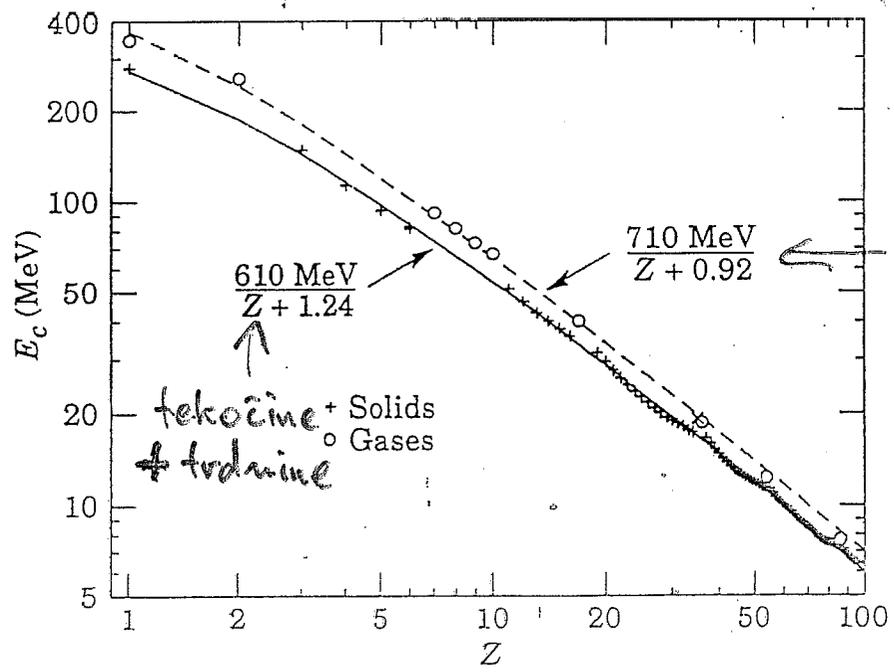


Figure 22.7: Electron critical energy for the chemical elements, using Rossi's definition [1]. The fits shown are for solids and liquids (solid line) and gases (dashed line). The rms deviation is 2.2% for the solids and 4.0% for the gases. (Computed with code supplied by A. Fassó.)

### LPM – Landau-Pomeranchuk-Migdal

Pri visokih energijah potekajo majhni prenos energij preko več atomov, pomembno če

$$E_\gamma < E^2 / (E + E_{LPM})$$

kjer je

$$E_{LPM} = \frac{(m_e c^2)^2 \alpha X_0}{4\pi h c \rho} = (7.7 \text{ TeV/cm}) \times \frac{X_0}{\rho}$$

Formacijska dolžina – interferenca med sevalci (atomi) na tej dolžini (destruktivna)

Senčenje v snovi !

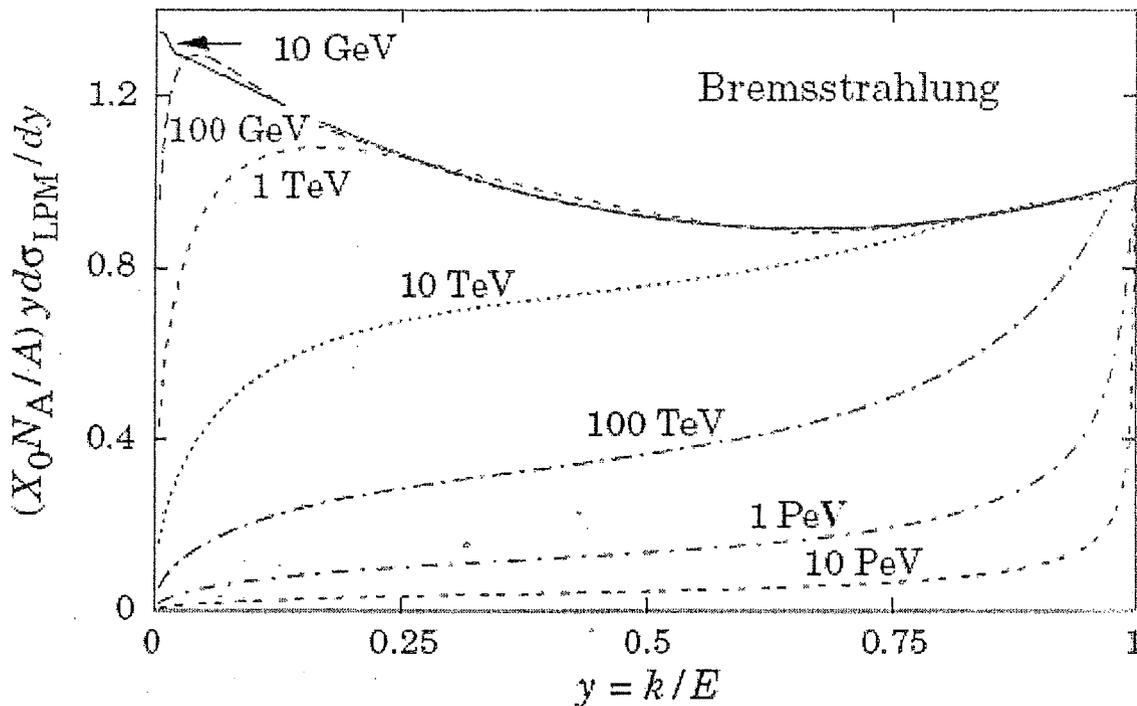


Figure 27.11: The normalized bremsstrahlung cross section  $k d\sigma_{LPM} / dk$  in lead versus the fractional photon energy  $y = k/E$ . The vertical axis has units of photons per radiation length.

# Doseg elektronov

- veliko stresanje zaradi sipanja

- za  $\beta$ -razpad efektivna  $I = I_0 e^{-\mu x}$   
 spekter & doseg  
 le dovoljeniz-prehodi

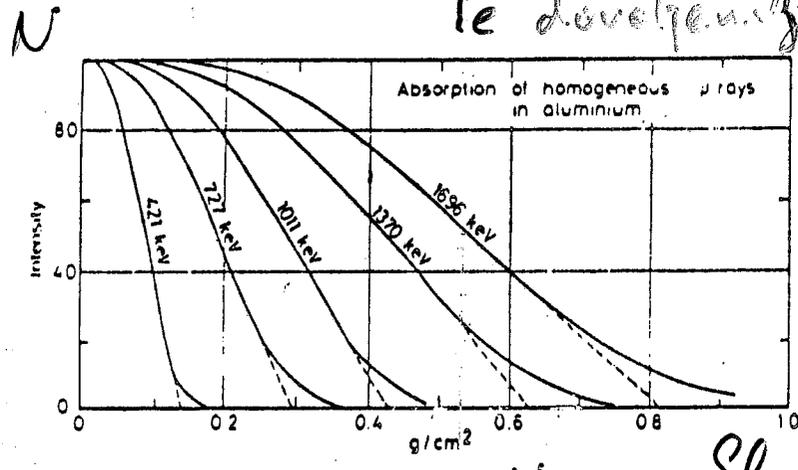


Fig. 2.11. Range number-distance curves for electrons (from Murshull and Wurd (2.15))

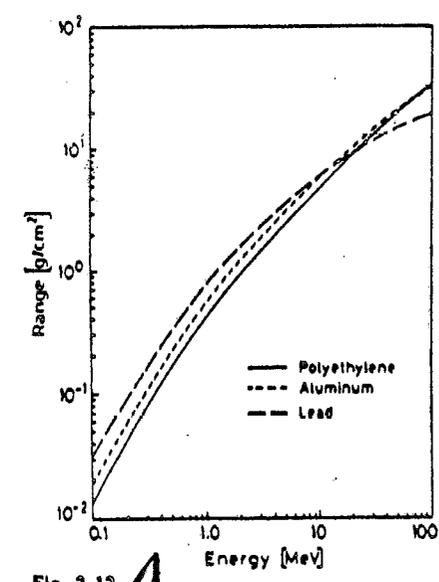


Fig. 2.12

$$R = \int_{E_0}^0 \frac{dE}{dE/dx}$$

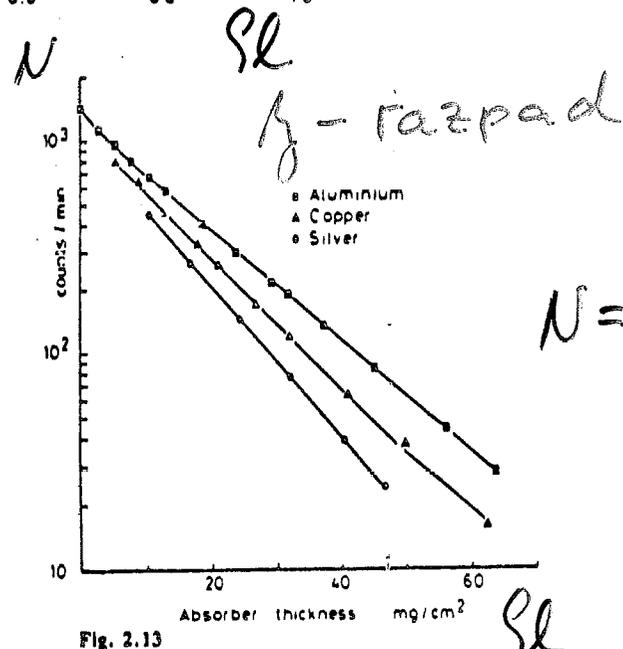


Fig. 2.13

$$N = N_0 e^{-\frac{\mu}{\rho} x}$$

d) Večkratno Coulombsko sipanje  
 sipanje na jedrih  $M_j \gg M$

Rutherford :  $\frac{d\sigma}{d\Omega} = z_1^2 z_2^2 \frac{m_e}{4\epsilon_0^2 \sin^4 \frac{\theta}{2}}$

$\Rightarrow$  majhni koti

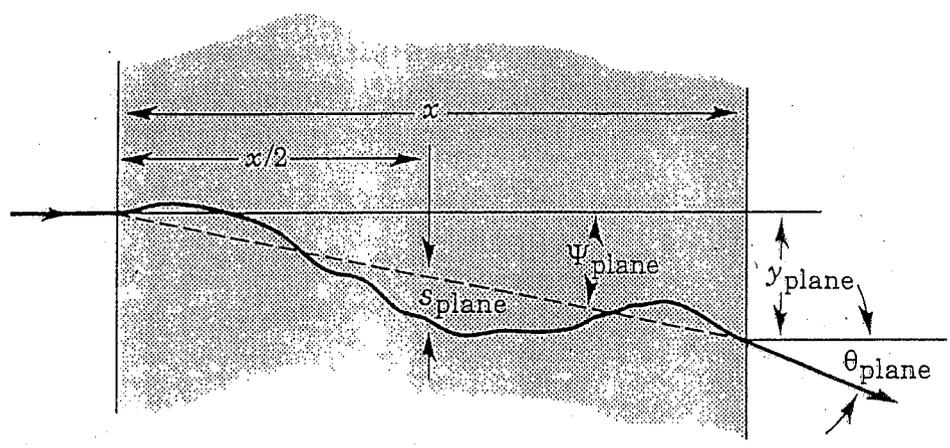
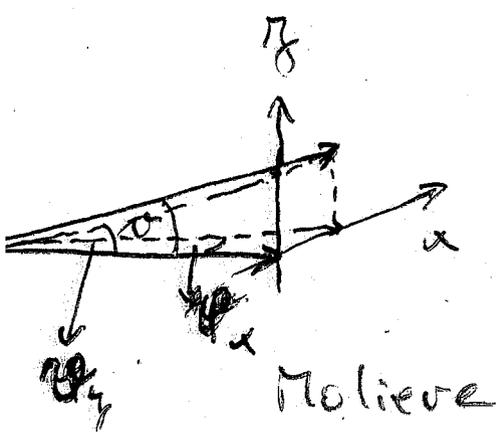


Figure 10.5: Quantities used to describe multiple Coulomb scattering. The particle is incident in the plane of the figure.

trije režimi : - tanek absorber  
 $l_s < 1$  ; Rutherford

- vmesno področje  
 $1 < l_s < 20$  ni statistično

- večkratno sipanje  
 $l_s > 20$  statistično



(25)

$$P(\psi) d\psi = \eta d\eta \left( 2e^{-\eta^2} + \frac{E_1(\eta)}{B} + \frac{E_2(\eta)}{B^2} \right)$$

$$\eta = \frac{\psi}{\alpha \sqrt{B}} \quad \psi_1 = 0,4 \left( \frac{zQ}{p \cdot l} \right) \sqrt{\frac{9L}{A}}$$

B : ln B - B + ln gamma - 0.154 = 0

gamma = 8.831 . 10^3 \* (z^2 Q L) / (f^2 A Delta) ; Delta = 1.13 + 3.76 \* ((z^2) / (134 g))^2

F\_k (eta) = 1/k! \* (int\_0^eta f\_0(eta y) e^(-y^2/4) [y^2/4 ln y^2/4]^k y dy

Q = { sqrt(z(z+1)) / z e^1 orbital

q = { ((z+1) z^1.13) / z^4.13 e^1 orbital

GEANT računa VCS do F2!

oblika -> Gaussova sredica (98%) + repi

Gaussova sredica

P(v) dv = (2v / v\_0^2) e^(-v^2/v\_0^2) dv (26)

v\_0 = sqrt(<v^2>) . v\_0 ~ v\_n sqrt(B)

empirično

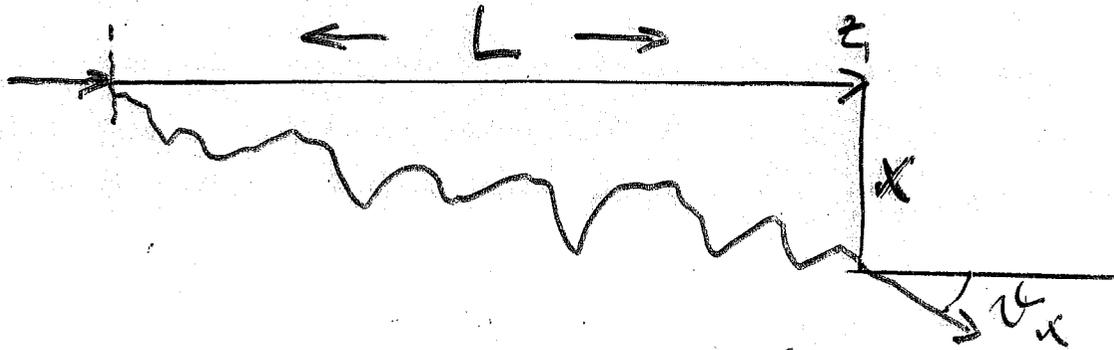
v\_0 = z\_p \* (20 MeV / m.p.c.) \* sqrt(L / X\_0) \* (1 + 1/3 ln((L / X\_0) \* (k / rho))) (27)

gamma=1

projekciji na ravni no :  $v_x, v_y$  20

$$P(v_x) dv_x = \frac{1}{\sqrt{2\pi} v_0} e^{-\frac{v_x^2}{2v_0^2}} \quad (28)$$

enako za  $v_y$ ; majhni koti  $\rightarrow v^2 = v_x^2 + v_y^2$   
 $v_x, v_y$  neodvisna  $\Rightarrow v_0^2 = 2v_0'^2$  (RPP:  $v_0 \rightarrow v_0'$ )

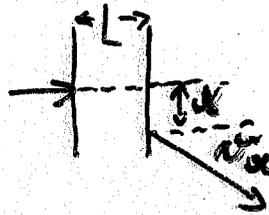


$$P(x) dx = \frac{1}{\sqrt{2\pi} x_0} e^{-\frac{x^2}{2x_0^2}} dx \quad (29)$$

$$x_0 = \frac{L v_0'}{\sqrt{3}}$$

$x$  in  $v_x$  korelinana ( $\rho = \frac{\sqrt{3}}{2}$ )

MC recept



$$z_1, z_2 \in N(0,1)$$

$$x = z_1 L v_0' / \sqrt{2} + z_2 L v_0' / 2$$

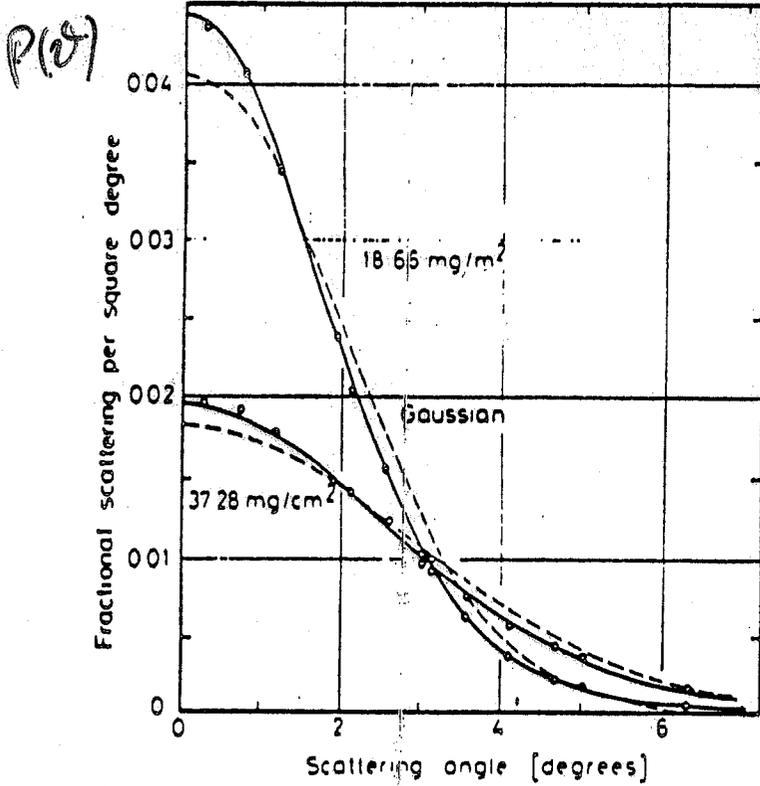
$$v_x = z_2 v_0'$$

enako za  $y, v_y$

površine sipanje

reka; elektronov nazaj -  $f(\nu, E, z)$

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VCS

na zlatu

albedo - verjetnost za sipanje nazaj

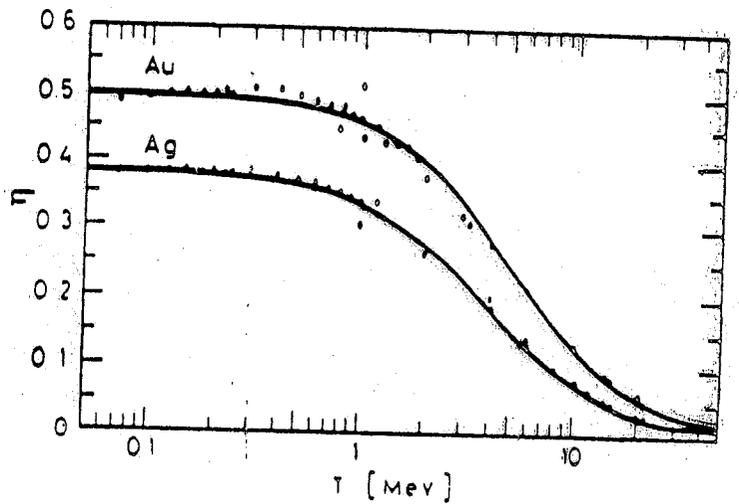
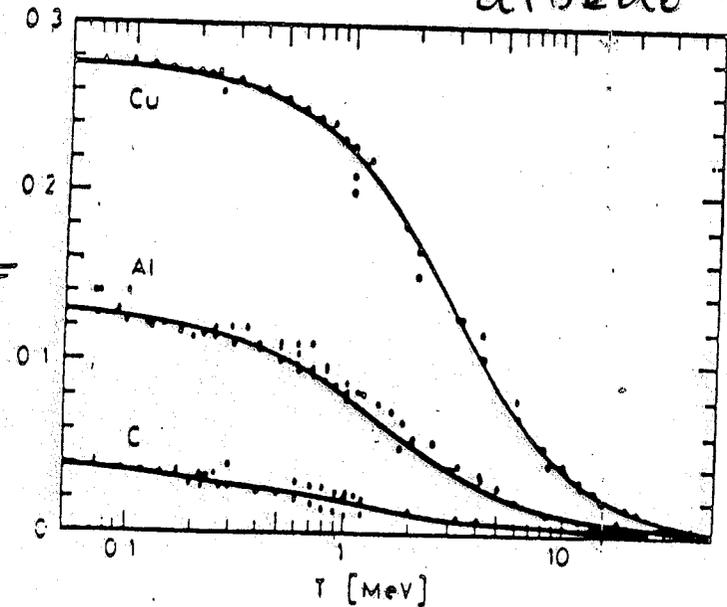


Fig. 2.17. Some measured electron backscattering coefficients for various materials. The electrons are perpendicularly incident on the surface of the sample (from Tabata et al. [2.24])

# e) Energijsko stresanje

22

Bethe Bloch poda le srednjo vrednost  $dE/dx$   
stresanje dosega  $\leftrightarrow$  stresanje en. izgub

debeli absorberji  $\rightarrow$  izrek o srednji vrednosti  $\rightarrow$  Gauss  
tanki absorberji  $\rightarrow$  malo trkov

parameter  $\mathcal{R} = \frac{\bar{\Delta}}{T_{\max}}$   $\bar{\Delta}$  - Bethe Bloch  
 $T_{\max} \approx 2 \text{ m.e.c. } \gamma^2 \beta^2$

$\mathcal{R} > 10$  ( $n > 1$ ) in  $\frac{\Delta}{E_0} \ll 1$  debeli absorberji

$$P(\Delta) = \frac{1}{\sqrt{2\pi}\bar{\sigma}_0} \exp\left[-\frac{(\Delta - \bar{\Delta})^2}{2\bar{\sigma}_0^2}\right] \quad (30)$$

$$\bar{\sigma}_0^2 = \frac{1 - \frac{1}{2}\beta^2}{1 - \beta^2} \cdot \underbrace{0.1569}_{4\pi N_A r_e^2 (\text{m.e.c.})^2} \cdot \frac{\mathcal{R}^2}{A} \cdot L \quad [\text{mev}^2] \quad (31)$$

zelo debeli absorberji  $\frac{\Delta}{E_0} \rightarrow 1$

Gauss ne velja  $\rightarrow$  numerična integracija

tanki absorberji  $T_{\max} > \bar{\Delta}$   
rep proti visokim  $dE/dx$  ( $\delta$ -elektroni!)

$$\bar{\Delta} \neq \Delta_{\text{mp}}$$

zelo tanki absorberji  $X < 0.01$

23

- Landau : -  $T_{max} \rightarrow \infty$  ( $X \rightarrow 0$ )  
Landau  
- prosti elektroni ( $\delta_1 > E_{at}$ )  
-  $\nu$  konstantna  
-  $\bar{\Delta}$  brez ln člena

$$\bar{\Delta} \Rightarrow \xi = 2\pi N_A n_e^2 m_e c^2 \rho \frac{z}{A} \left(\frac{z_0}{z}\right)^2 d$$

$$P(\Delta) = \phi(\lambda) / \xi$$

$$\phi(\lambda) = \frac{1}{\pi} \int_0^{\lambda} e^{-u \ln u - u \lambda} \sin \pi u \, du$$

$$\lambda = \frac{1}{\xi} \left[ \Delta - \xi (\ln \xi - \ln \Sigma + 1 - C) \right]$$

$C$  - Eulerjeva konstanta = 0.577

$$\ln \Sigma = \ln \frac{(1-\beta^2) I^2}{2 m c^2 \beta^2} + \beta^2 \quad \text{minimalni transfer (oh. prosti)}$$

$\phi(\lambda)$  - tabelirana, neodvisna od  $d$ .

$$\underline{\Delta_{mp} = \xi \left[ \ln\left(\frac{\xi}{\Sigma}\right) + 0.198 - \delta \right]} \quad (33)$$

srednje debeli absorberji  $0.01 < X < 10$  (1)

pora izdelitev Vavilova  $\rightarrow$  Landau +  $T_{max}$

limiti  $X \rightarrow 0$  Landau

$X \rightarrow \infty$  Gauss

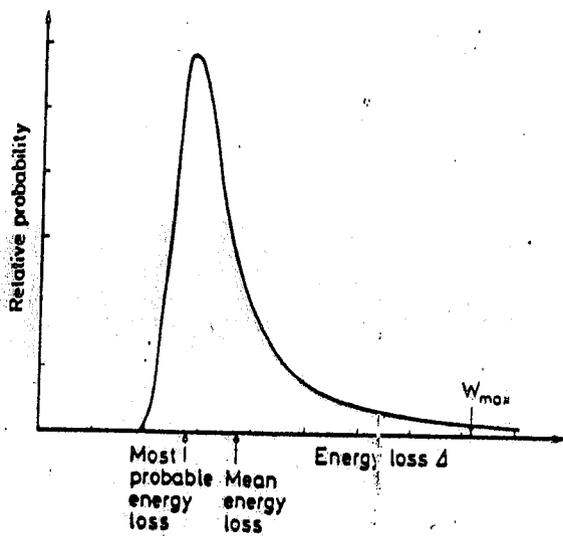


Fig. 2.18. Typical distribution of energy loss in a thin absorber. Note that it is asymmetric with a long high energy tail

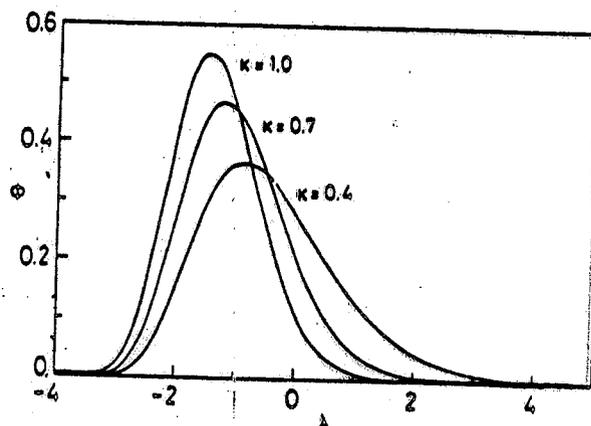
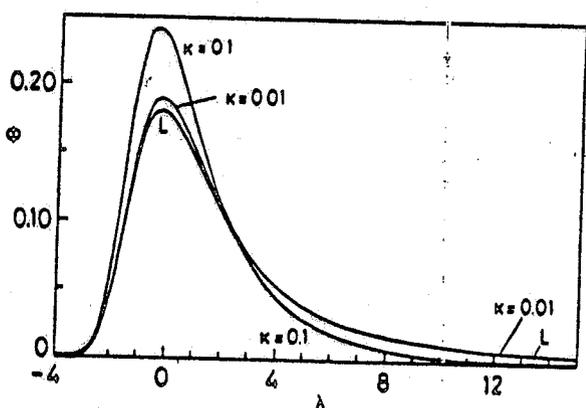
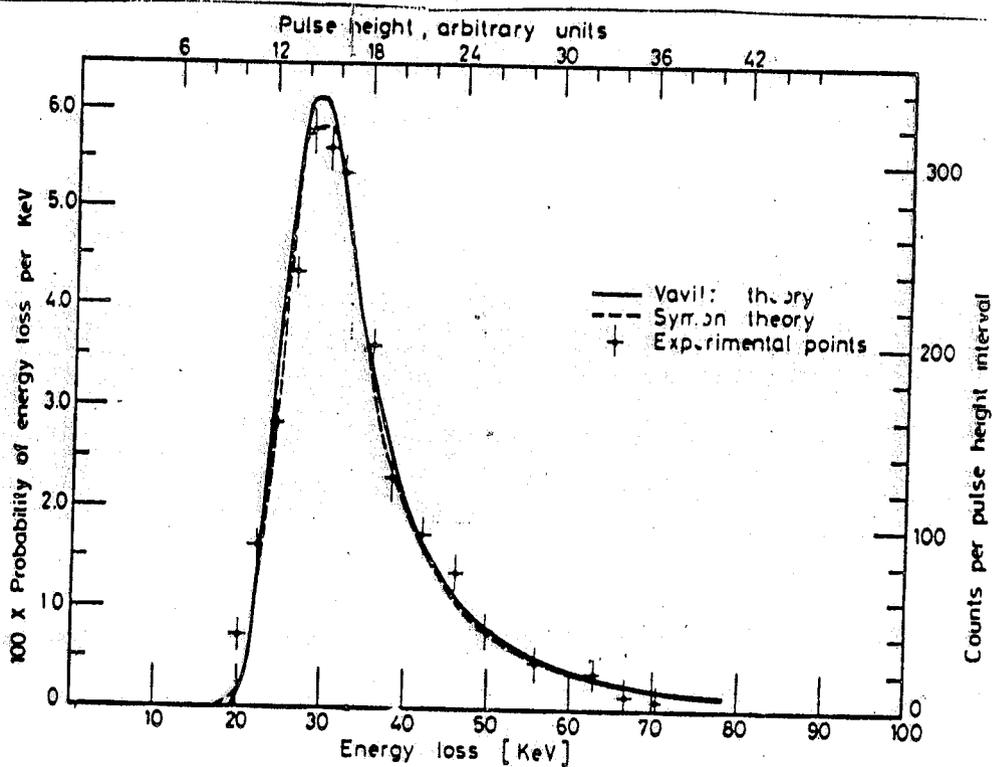


Fig. 2.19. Vavilov distributions for various  $\kappa$ . For comparison, Landau's distribution (denoted by the L) for  $\kappa = 0$  is also shown (from Seltzer and Berger [2.29])



f) Energijske izgube visokoenergijskih muonov. 24a

$$-\frac{dE}{dx} = a(E) + b(E)E \quad (33a)$$

$a(E)$  - ionizacija;  $\approx 2 \text{ MeV/g.cm}^{-2}$   $\approx \text{konst}$   
 - zavorno sevanje  
 - tvorba parov  
 - fotojedrske reakcije }  $\approx \text{konst. za } E_\mu > 1 \text{ TeV}$

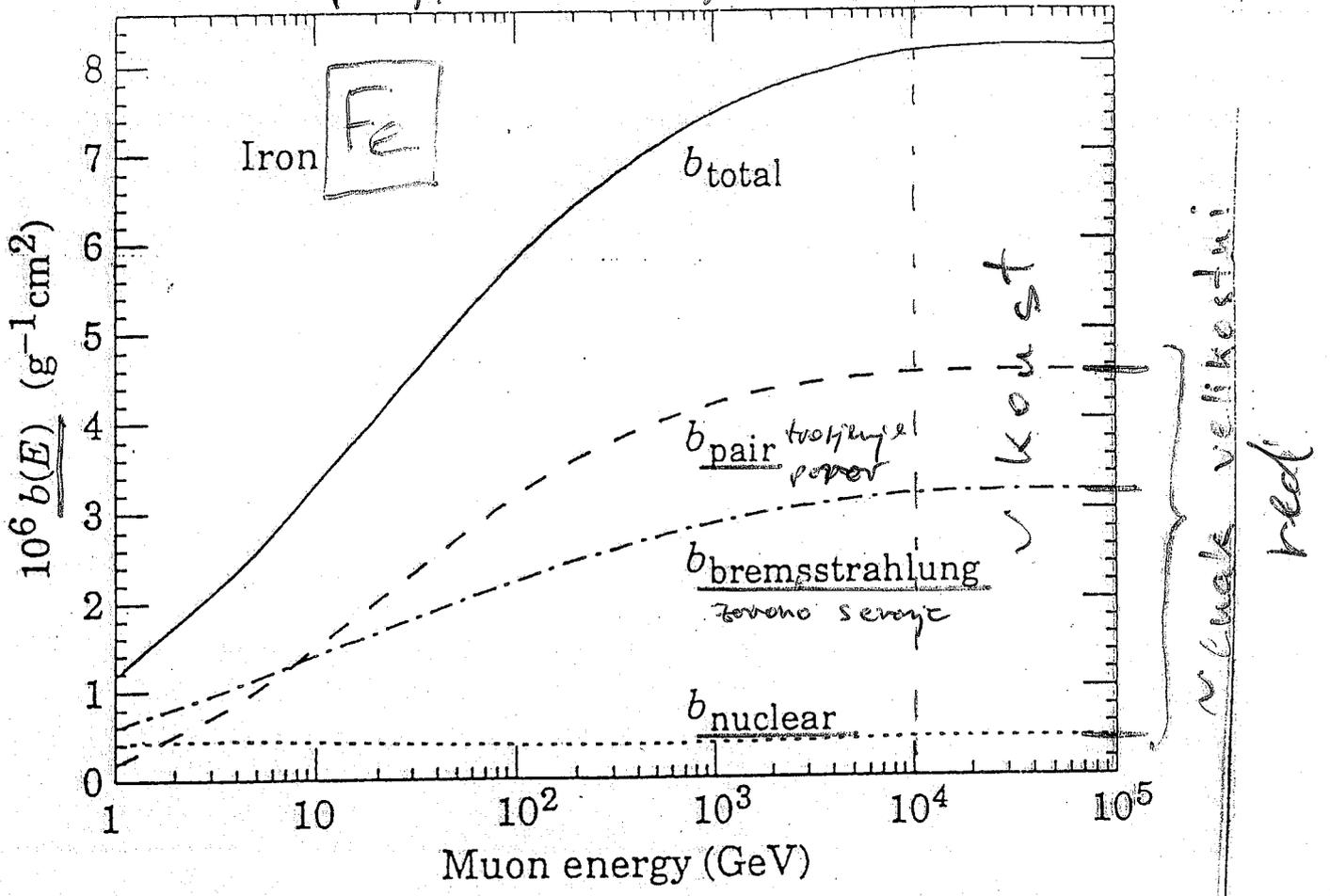
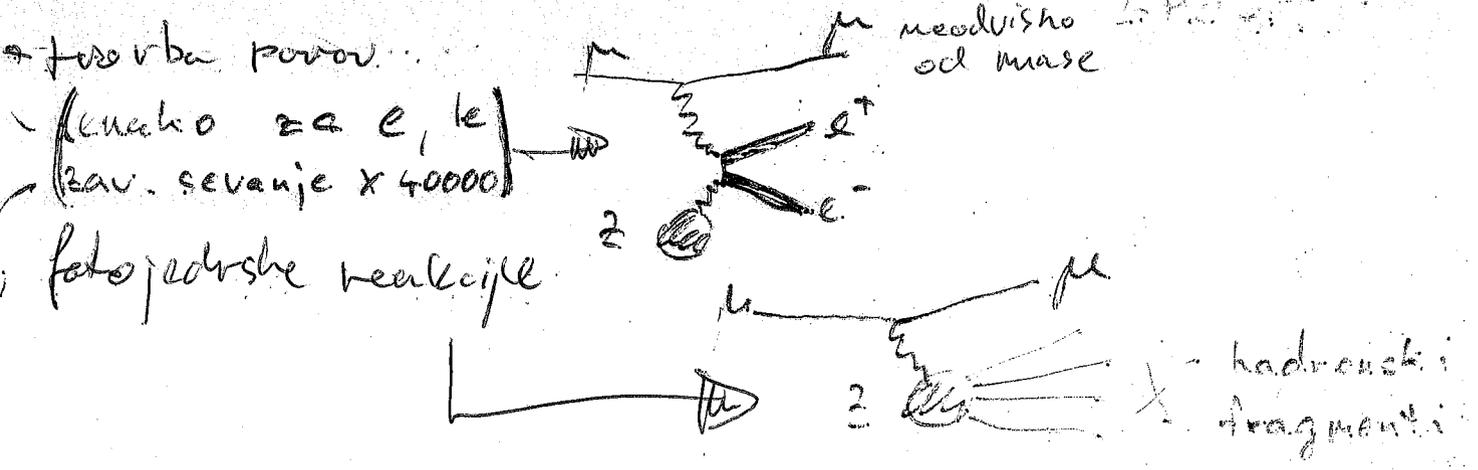


Figure 22.10: Contributions to the fractional energy loss by muons in iron due to  $e^+e^-$  pair production, bremsstrahlung, and photonuclear interactions, as obtained from Lohmann et al. [39].

zavorno sevanje - kot za elektrone  $E_e = E_\mu \left(\frac{m_e}{m_\mu}\right)^2$



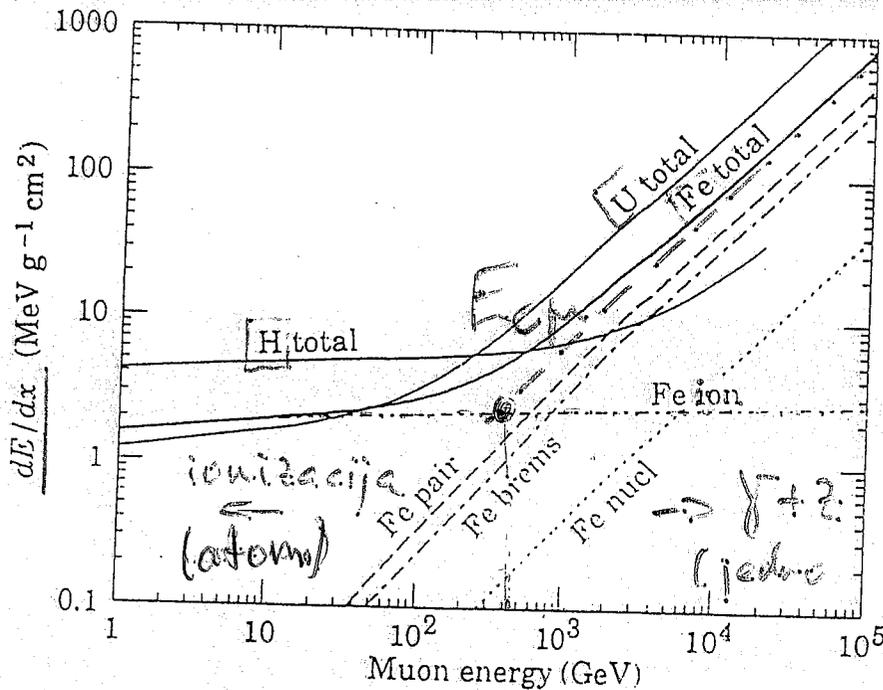


Figure 22.11: The average energy loss of a muon in hydrogen, iron, and uranium as a function of muon energy. Contributions to  $dE/dx$  in iron from ionization and the processes shown in Fig. 22.10 are also shown.

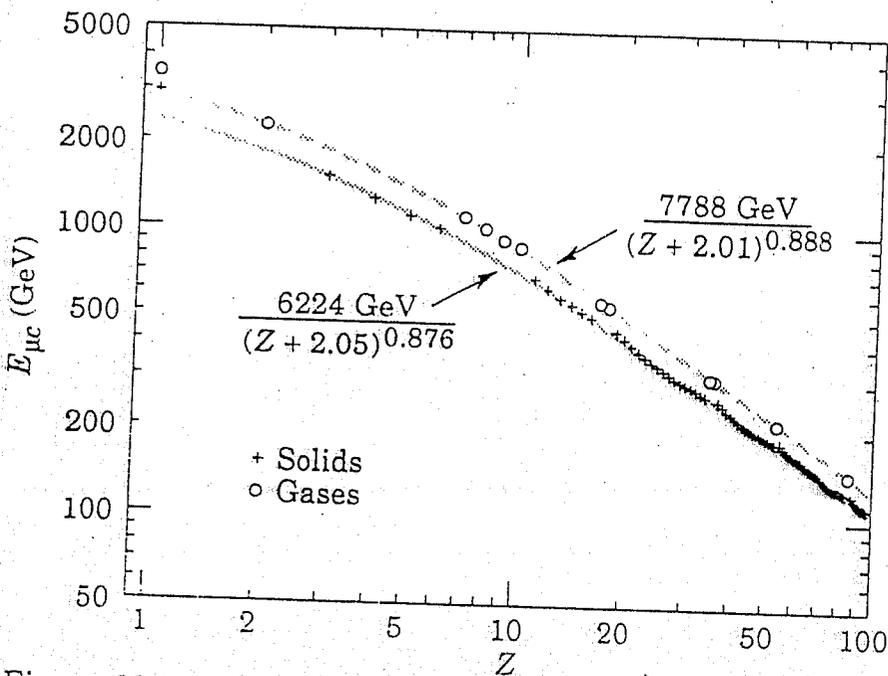


Figure 22.12: Muon critical energy for the chemical elements, defined as the energy at which radiative and ionization energy loss rates are equal. The equality comes at a higher energy for gases than for solids or liquids with the same atomic number because of a smaller density effect reduction of the ionization losses. The fits shown in the figure exclude hydrogen. Alkali metals fall 3-4% above the fitted function for alkali metals, while most other solids are within 2% of the function. Among the gases the worst fit is for neon (1.4% high). (Courtesy of N.V. Mokhov, using the MARS code system [48].)

$$E_{\mu c} = \frac{a(E_c)}{b(E_{\mu c})} \sim \frac{a}{b}$$

$a, b \sim \text{konst}$

doseg

$$x_0 \sim \frac{1}{b} \ln\left(1 + \frac{E_0}{E_{\mu c}}\right)$$

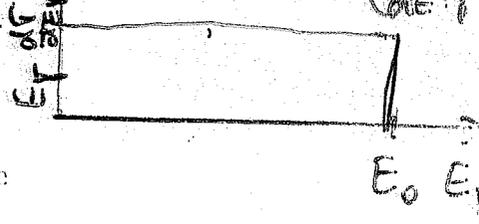
$$E_0 \ll E_c: x_0 = \frac{E_0}{a}$$

le porprie

energije izpube

savorno sevanje

$$E_T \frac{dT}{dE_T} \sim \text{konst} \Rightarrow \left(\frac{dT}{dE_T}\right)_T \sim \frac{1}{E_T}$$



možne velike energije izpube  $\Rightarrow$  stvaranje

$$\frac{dE_{\text{pari}}}{dx} > \frac{dE_r}{dx} > \frac{dE_{\text{fotojedr}}}{dx}$$

- spekter produktov - zelo trd fotojedrske  
 - trd zavorno sevanje  
 - mehkejši tvorba parov

⇒ veliki  $\frac{dE}{dx}$  posledica redkih...  
 - trdi fotonov...  
 - fotojedrske reakcija...

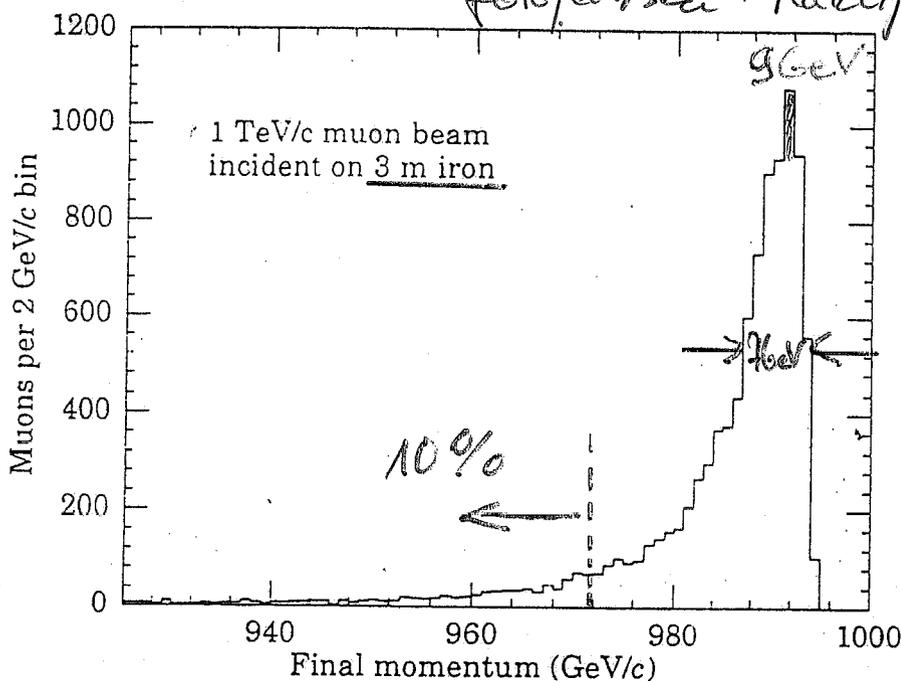


Figure 22.13: The momentum distribution of 1 TeV/c muons after traversing 3 m of iron as obtained with Van Ginniken's TRAMU muon transport code [50].

3 m Fe  $\sim 18 \lambda_I \sim$  material pred  
 muonskimi komorami. LHC detektorjev

1 TeV  $\mu$  :  $\Delta E_{\text{pari}} = 96 \text{ GeV}$  ( $\sim 10\%$ )  
 $\text{FWHM} = 76 \text{ GeV}$  ( $\sim 10\%$ )

$\boxed{\text{rep}}$  : 10%  $\Delta E > 28 \text{ GeV} \sim$  zavorno sevanje  
 3,3%  $\Delta E > 100 \text{ GeV} \sim$  fotojedrske

Samo  $\mu$ -komore niso dovolj } + kalorimeter  
 } + sledilnik !

## II Prehod fotonov skozi snov

25

- fotoefekt
- Comptonski pojav
- tvorba parov

pri fotonih se manjša  
fluks  
pri delcih pa ~~ostane~~  
enaka energija.

razlika proti delcem

ni energijskih izgub -  $\sigma \ll \sigma_{\text{Bali}}$

foton izgine

- "doseg" večji

- manjša se fluks

$$I = I_0 e^{-\mu x}$$

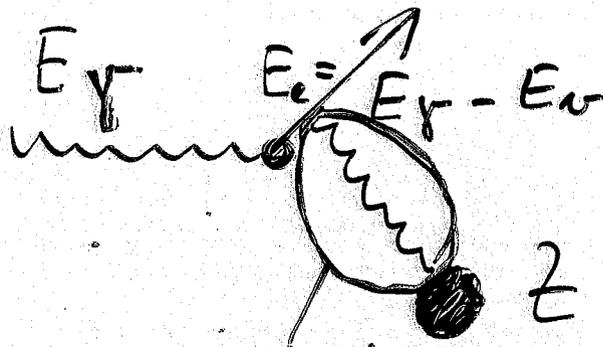
(34)

$\mu$  - absorpcijski koeficient

$\lambda = \frac{1}{\mu}$  - atenuacijska dolžina

a) fotoefekt

vezani elektroni v atomu



velika verjetnost le.  
za K-elektrone

preseki naraste za  $\sim Z^2$  reda, ko  $E_\gamma$  preseže  
 $E_\nu$  za K-elektrone - K rob

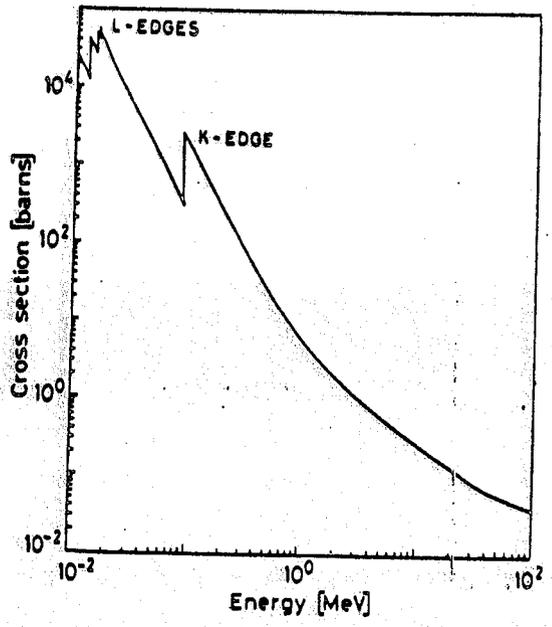


Fig. 2.21. Calculated photoelectric cross section for lead

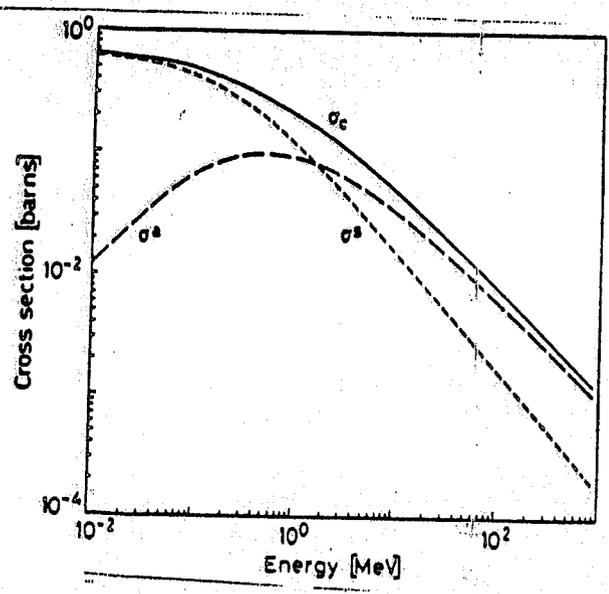


Fig. 2.23. Total Compton scattering cross sections

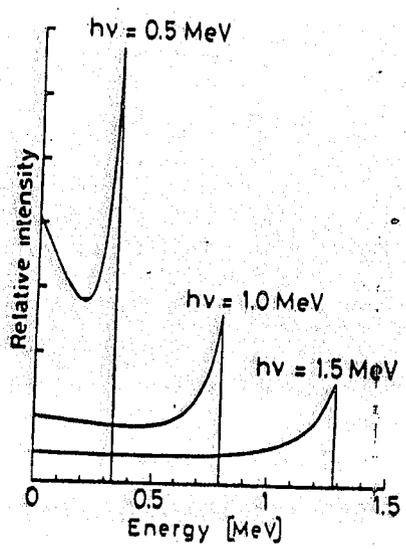


Fig. 2.24. Energy distribution of Compton recoil electrons. The sharp drop at the maximum recoil energy is known as the *Compton edge*

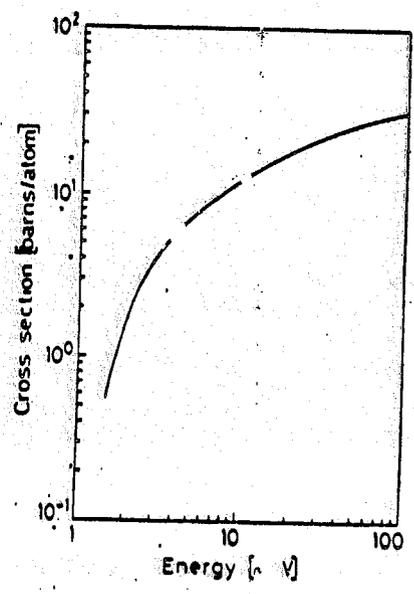


Fig. 2.25. Pair production cross section in lead

odvisnost za  $\Gamma$  nad  $k$ -robom

L4

$E_k \ll E_F \ll m_e c^2$  nerel. račun

$$\Gamma = \frac{32\pi}{3} n_e^2 \sqrt{2} z^5 L^4 \left( \frac{m_e c^2}{E_F} \right)^{7/2} \propto \frac{z^5}{E_F^{7/2}} \quad (35)$$

$$\sigma_{Th} = \frac{8\pi}{3} n_e^2 = 6,65 \cdot 10^{-25} \text{ cm}^2$$

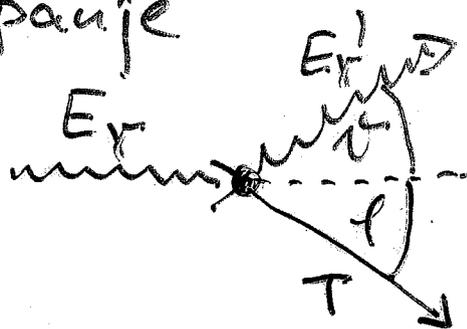
$$\Gamma = 4\sqrt{2} \sigma_{Th} z^5 L^4 \left( \frac{m_e c^2}{E_F} \right)^{7/2} \quad (35a)$$

$E_F \gg m_e c^2$  ultrarel. račun

$$\Gamma = \frac{3}{2} \sigma_{Th} z^5 L^4 \left( \frac{m_e c^2}{E_F} \right) \quad (36)$$

b) Comptonsko sipanje

prost elektron



$$E_F' = \frac{E_F}{1 + \gamma(1 - \cos\theta)} \quad (37)$$

$$\gamma = \frac{E_F}{m_e c^2}$$

$$T = E_F - E_F' = E_F \frac{\gamma(1 - \cos\theta)}{1 + \gamma(1 - \cos\theta)} \quad (38)$$

$$\frac{d\sigma}{d\Omega} = \frac{\pi r_e^2}{2} \frac{1}{[1 + \gamma(1 - \cos\theta)]^2} \left( 1 + \cos^2\theta + \frac{\gamma^2(1 - \cos\theta)^2}{1 + \gamma(1 - \cos\theta)} \right) \quad (39)$$

Integralni presek

$$\sigma_c = 2\pi r_e^2 \left\{ \frac{1+\gamma}{\gamma^2} \left[ \frac{2(1+\gamma)}{1+2\gamma} - \frac{1}{\gamma} \ln(1+2\gamma) \right] + \frac{1}{2\gamma} \ln(1+2\gamma) - \frac{1+3\gamma}{(1+2\gamma)^2} \right\} \quad (40)$$

$\sigma_c \propto \frac{1}{E_\gamma}$  (na elektron;  $\frac{2}{E_\gamma}$  na atom)

$$\sigma_c = \sigma_s + \sigma_a ; \quad \frac{d\sigma_c}{d\Omega} = \frac{E_\gamma'}{E_\gamma} \frac{d\sigma}{d\Omega} \quad (41)$$

za velike energije:  $\sigma_a \rightarrow \sigma$  (absorbicija)

za majhne energije:  $\sigma_s \rightarrow \sigma$  (sipanje)  
foton gredo naprej

elektroni

$$\frac{d\sigma}{d\Omega} = \frac{\pi r_e^2}{m_e c^2 \gamma^2} \left[ 2 + \frac{\lambda^2}{\gamma^2 (1-\lambda)^2} + \frac{\lambda}{1-\lambda} \left( \lambda - \frac{2}{\gamma} \right) \right]$$

$$\lambda = \frac{T}{E_\gamma} ; \quad T_{\max} = E_\gamma \frac{2\gamma}{1+2\gamma} \quad (\text{Comptonovskii rok}) \quad (42)$$

Thompson - prost elektron v klasični limiti

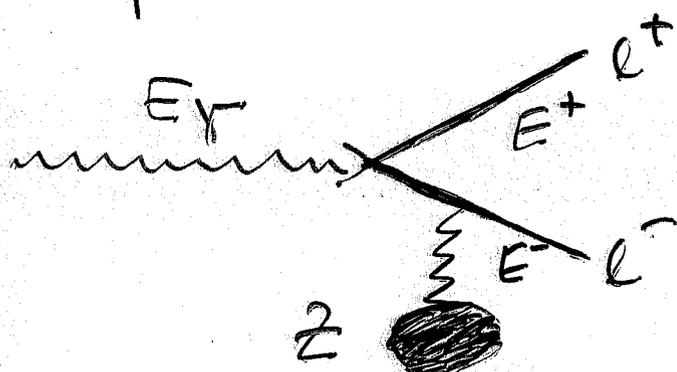
Rayleigh - koherentno sipanje na atomu kot celoti

$E_\gamma' = E_\gamma$  elastično ; zanemarljivo za  $X \ll \gamma$

c) tvorba parov

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na jedrih - obraten proces k zavornemu sevanju



senčenje parameter  $\xi = \frac{100 m_e c^2 E_\gamma}{E^+ E^- Z^{1/3}}$

$$E_\gamma \gg 1.34 m_e c^2 Z^{1/3} \rightarrow \xi \rightarrow 0$$

popolno senčenje

preseka konstanten

$$\underline{\underline{\tau_p = \frac{A}{N_0 \rho} \frac{Q}{9 X_0} \propto Z^2}} \quad (43)$$

$$\underline{\underline{N = N_0 \rho \frac{Z X_0}{9 X_0}}} \quad (44)$$

elektroni vključeni v  $X_0$  ( $Z^2 \rightarrow Z(Z+1)$ )

$$\lambda = \frac{9}{7} X_0$$

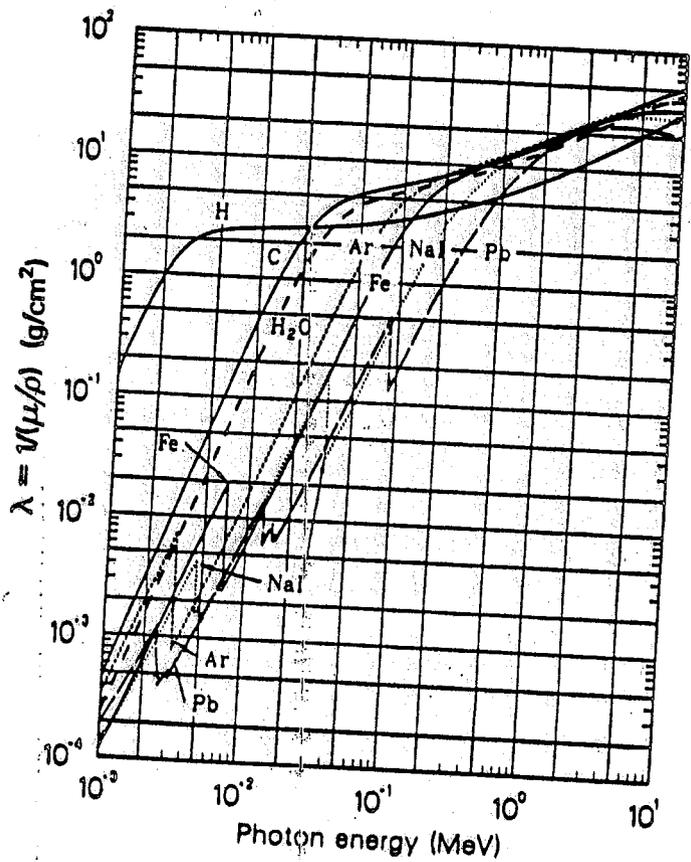
atenuacijska in radiacijska dolžina

skupaj  $\underline{\underline{\tau_{tot} = \tau_{ph} + Z \tau_e + \tau_p}} \quad (45)$

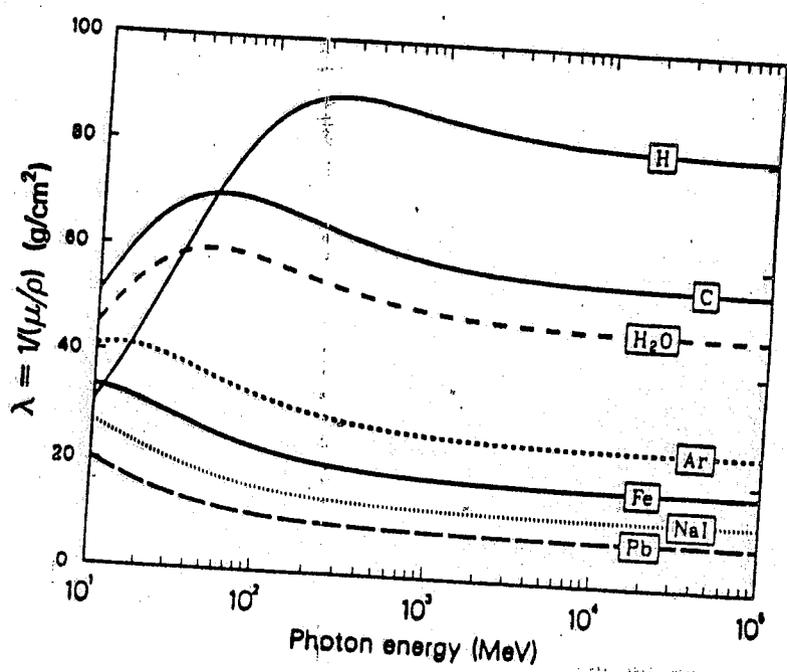
$$\underline{\underline{\mu = N \tau = \left( \frac{N_0 \rho}{A} \right) \tau}} \quad (46)$$

PHOTON AND ELECTRON ATTENUATION

Photon Attenuation Length



Photon Attenuation Length (High Energy)



# Contributions to Photon Cross Section in Carbon and Lead

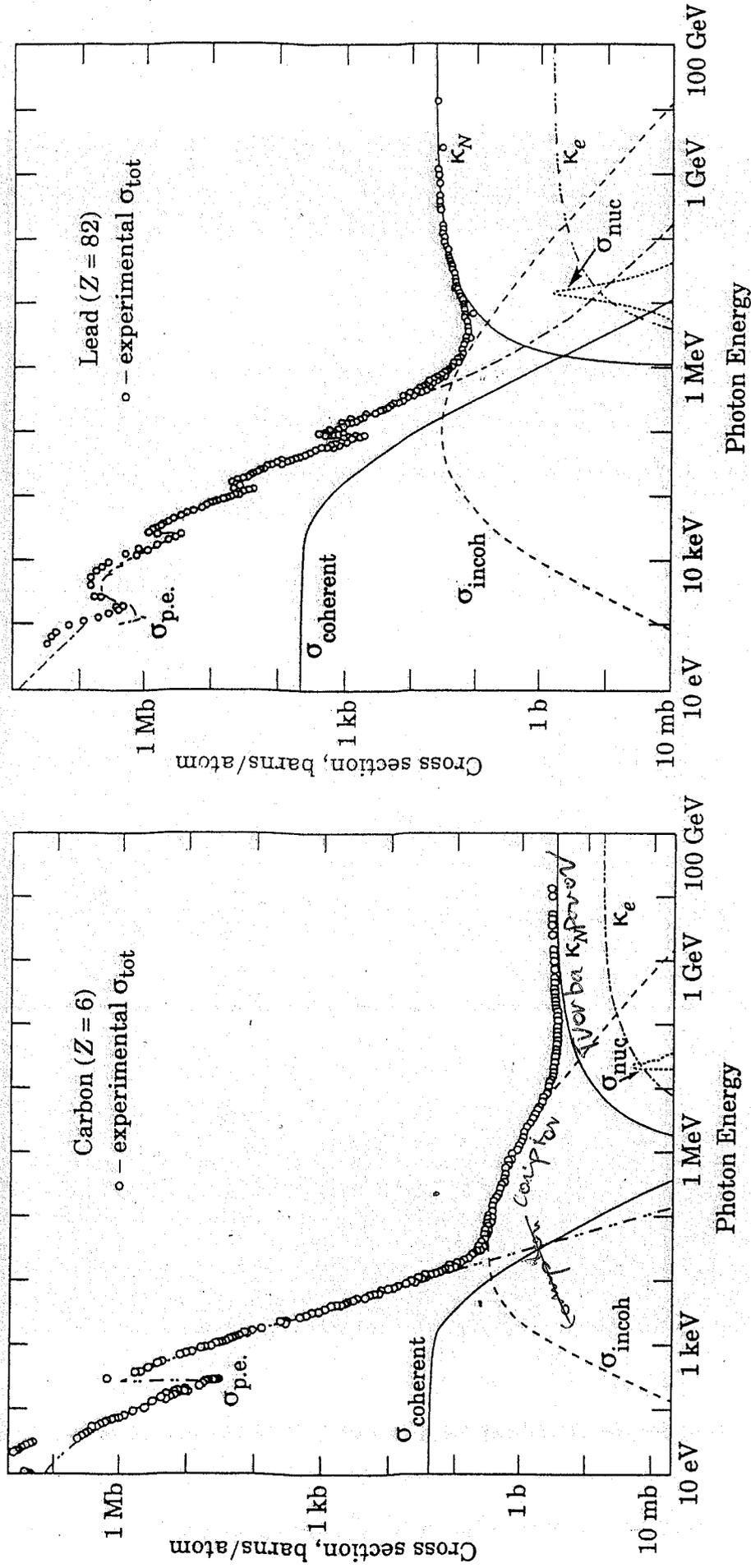


Figure 11.3: Photon total cross sections as a function of energy in carbon and lead, showing the contributions of different processes.

- $\sigma_{p.e.}$  = Atomic photo-effect (electron ejection, photon absorption)
- $\sigma_{coherent}$  = Coherent scattering (Rayleigh scattering—atom neither ionized nor excited)
- $\sigma_{incoherent}$  = Incoherent scattering (Compton scattering off an electron)
- $\kappa_n$  = Pair production, nuclear field
- $\kappa_e$  = Pair production, electron field
- $\sigma_{nuc}$  = Photoneuclear absorption (nuclear absorption, usually followed by emission of a neutron or other particle)

From Hubbell, Gimm, and Øverbø, J. Phys. Chem. Ref. Data 9, 1023 (80). The photon total cross section is assumed approximately flat for at least two decades beyond the energy range shown. Figures courtesy J.H. Hubbell.