



Univerza v Ljubljani



THE UNIVERSITY OF TOKYO

## Flavour Physics at B-factories and Hadron Colliders

### Part 5+6: angle $\phi_1(\beta)$

Peter Križan

*University of Ljubljana and J. Stefan Institute*

June 5-8, 2006

Course at University of Tokyo

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## Contents

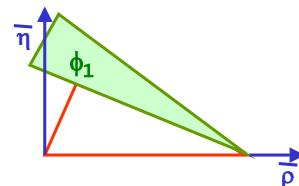
Reconstruction of  $b \rightarrow ccs$  decays

Tagging, calibration

Vertex resolution

Asymmetry parameters,  $\sin 2\phi_1$  and  $|\lambda|$

$\sin 2\phi_1$  from  $b \rightarrow ccd$



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## CP asymmetry

**CP asymmetry:**

$$a_{f_{CP}} = \frac{P(\bar{B}^0 \rightarrow f_{CP}, t) - P(B^0 \rightarrow f_{CP}, t)}{P(\bar{B}^0 \rightarrow f_{CP}, t) + P(B^0 \rightarrow f_{CP}, t)} = \lambda = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

$$= \frac{(1 - |\lambda_{f_{CP}}|^2) \cos(\Delta m t) - 2 \operatorname{Im}(\lambda_{f_{CP}}) \sin(\Delta m t)}{1 + |\lambda_{f_{CP}}|^2}$$

$$\left. \begin{array}{l} \text{CP in decay: } |\bar{A}/A| \neq 1 \\ \text{CP in mixing: } |q/p| \neq 1 \end{array} \right\} |\lambda| \neq 1$$

CP in interference between mixing and decay:  $|\lambda| = 1, \operatorname{Im}(\lambda) \neq 0$

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## Decay asymmetry predictions $\bar{J}/\psi K_S$

b → c̄cs:

Take into account that we measure the  $\pi^+ \pi^-$  component of  $K_S$  – also need the  $(q/p)_K$  for the K system

Tree contribution:

$$\lambda_{\psi K_S} = \eta_{\psi K_S} \left( \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}} \right) \left( \frac{V_{cs}^* V_{cb}}{V_{cs} V_{cb}} \right) \left( \frac{V_{cd}^* V_{cs}}{V_{cd} V_{cs}} \right) =$$

$$= \eta_{\psi K_S} \left( \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}} \right) \left( \frac{V_{cb}^*}{V_{cb}} \frac{V_{cd}}{V_{cd}} \right) \quad \beta \equiv \phi_l \equiv \arg \left( \frac{V_{cd} V_{cb}}{V_{td} V_{tb}} \right)$$

$$\operatorname{Im}(\lambda_{\psi K_S}) = \sin 2\beta$$

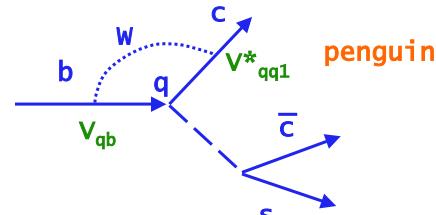
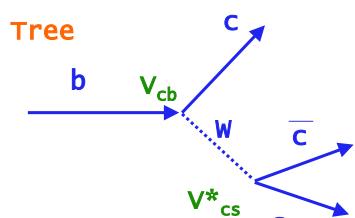
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## Penguins $b \rightarrow c\bar{c}s$ decays?



$$A(c\bar{c}s) = V_{cb}V_{cs}^*(T_{c\bar{c}s} + P_s^c - P_s^t) + V_{ub}V_{us}^*(P_s^u - P_s^t)$$

How much does P contribute?

- Few percent to the first term  
 $V_{cb}V_{cs}^* = \mathcal{O}\lambda^2$

$$r_{penguin} = \frac{P^t - P^u}{T} \approx \frac{\alpha_s}{12\pi} \ln \frac{m_t^2}{m_b^2} \approx \mathcal{O}(0.03)$$

- The second (P only) term contributes  $\sim 0.1\%$

$$r_{penguin} \left( \frac{V_{us}^* V_{ub}}{V_{cb} V_{cs}^*} \right) \approx r_{penguin} \lambda^2 \approx \mathcal{O}(10^{-3})$$

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## Reconstructing chamonium states

Reconstructing final states X which decayed to several particles (x,y,z):

From the measured tracks calculate the invariant mass of the system ( $i=x,y,z$ ):

$$M = \sqrt{(\sum E_i)^2 - (\sum \vec{p}_i)^2}$$

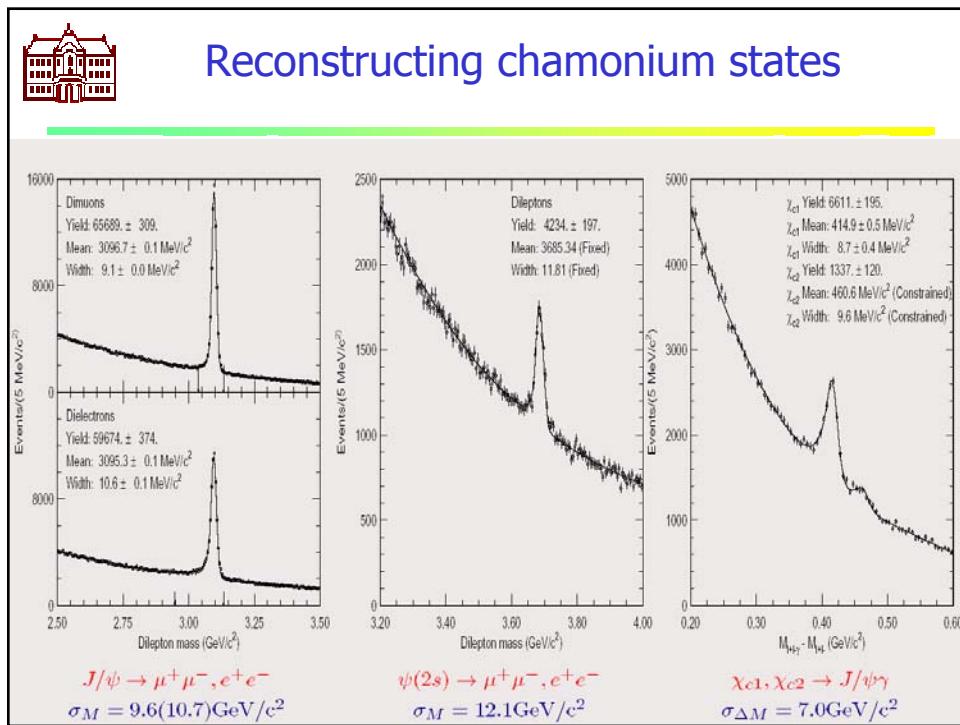
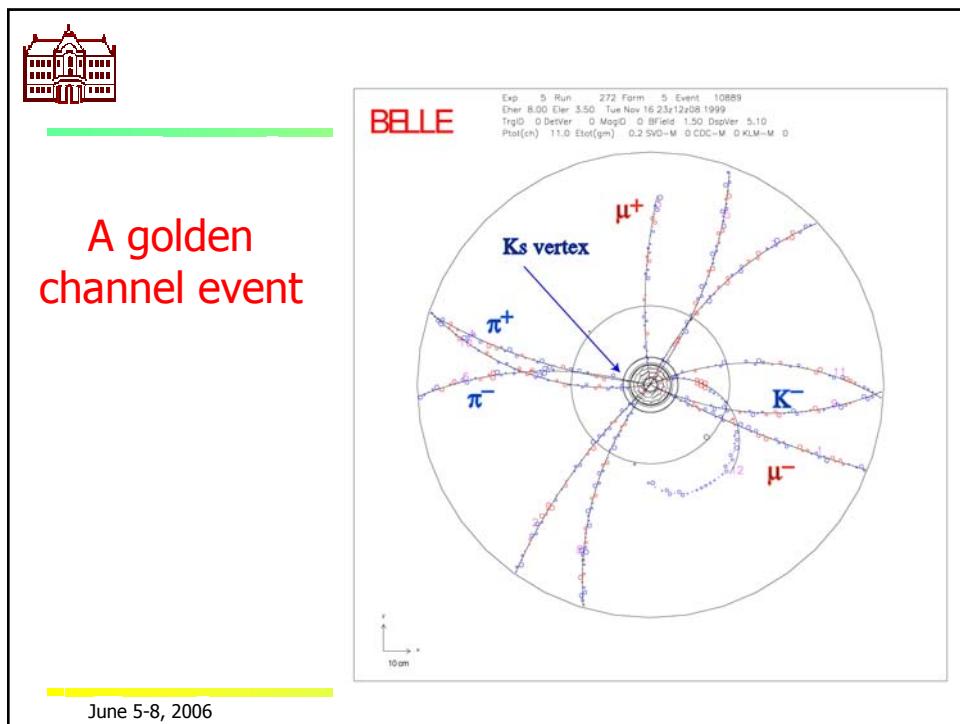
The candidates for the  $X \rightarrow xyz$  decay show up as a peak in the distribution on (mostly combinatorial) background.

The name of the game: have as little background under the peak as possible without loosing the events in the peak (=reduce background and have a small peak width).

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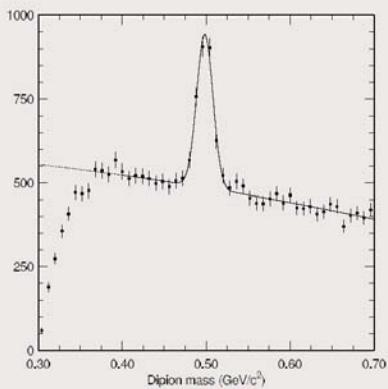
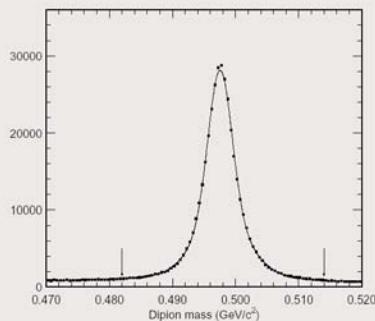




## Reconstructing $K^0_S$

$$K_S \rightarrow \pi^+ \pi^-$$

$$\sigma_M = 4.1 \text{ GeV}/c^2$$



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## Reconstruction B meson decays

Reconstructing B meson decay at Y(4s):

Improve the resolution by taking into account that only two B mesons are produced in an Y(4s) decay.

In the expression for the invariant mass use the energy of the beam in cms (1/2 total energy in cms) instead of the reconstructed energy (which involves information on particle identification)

-> **beam constrained mass  $M_{bc}$**

$$M_{bc} = \sqrt{(E_{CM}/2)^2 - (\sum \vec{p}_i)^2}$$

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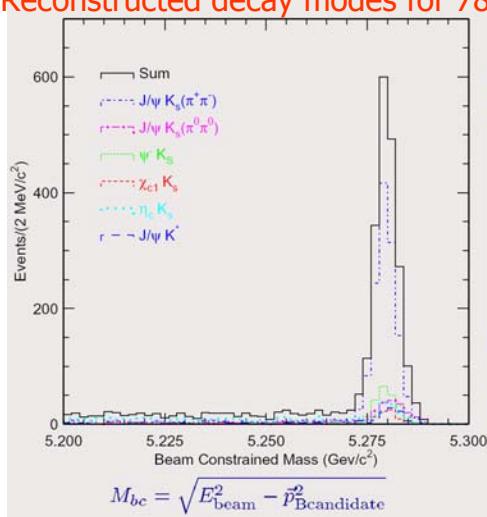
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## Reconstruction of b-> c anti-c s CP=-1 eigenstates

Reconstructed decay modes for 78/fb, 85M B B pairs, Belle 2002  
result



$B^0 \rightarrow$	events	$\frac{S}{S+N}$
$J/\psi K_S(K_S \rightarrow \pi^+\pi^-)$	1285	.976
$J/\psi K_S(K_S \rightarrow \pi^0\pi^0)$	188	.824
$\psi(2S)K_S$		
$(\psi(2S) \rightarrow \ell^+\ell^-)K_S$	91	.957
$(\psi(2S) \rightarrow J/\psi\pi^+\pi^-)$	112	.911
$\chi_{c1}K_S$	77	.958
$\eta_c(\eta_c \rightarrow K_SK\pi)K_S$	72	.646
$\eta_c(\eta_c \rightarrow KK\pi^0)K_S$	49	.725
$\eta_c(\eta_c \rightarrow pp)K_S$	21	.936
$J/\psi K^*(K^* \rightarrow K_S\pi^0)$	101	.917
total $CP = -1$	1996	.935
$J/\psi K_L, CP = +1$	1330	.627
Total	3326	.807

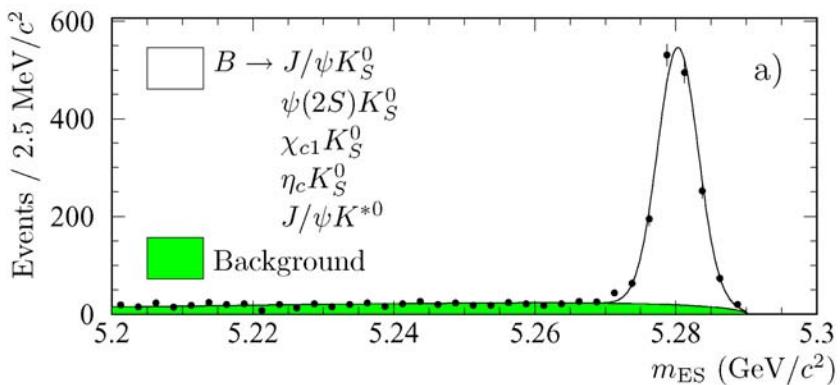
2958 events are used in the fit



## Reconstruction of b-> c anti-c s CP=-1 eigenstates

$J/\Psi(\Psi,\chi_{c1},\eta_c)$   $K_S(K^{*0})$  sample ( $\eta_f = -1$ )  
from  $88(85)\times 10^6$  BB

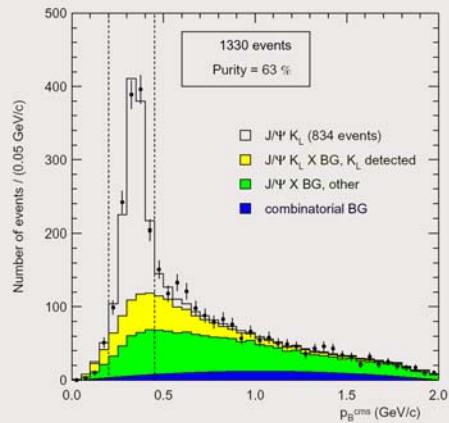
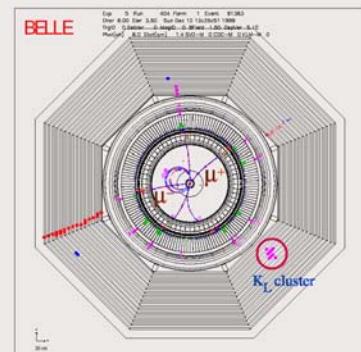
BaBar 2002 result





## Reconstruction of b-> c anti-c s CP=+1 eigenstates

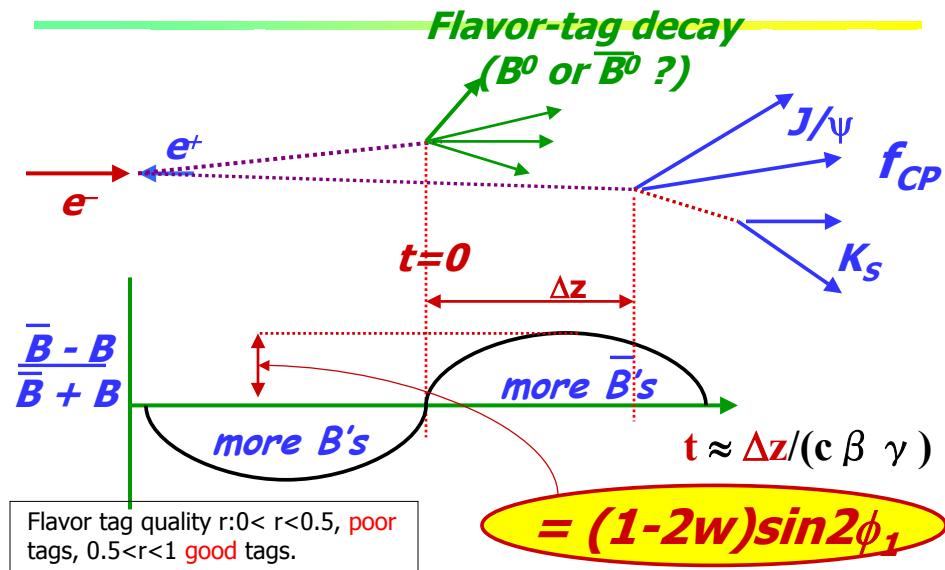
- ◆ detection of  $K_L$  in KLM and ECL
- ◆  $K_L$  direction, no energy



- ◆  $p^* \approx 0.35$  GeV/c for signal events
- ◆ background shape is determined from MC, and its size from the fit to the data



## Principle of CPV Measurement



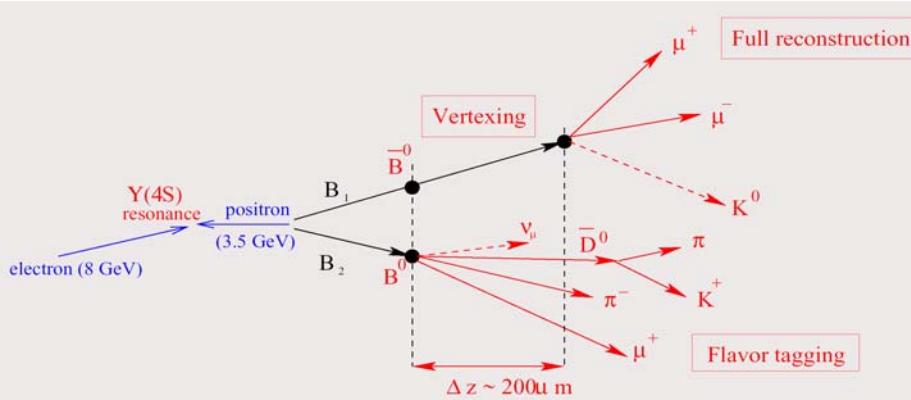
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## Measurement of CP violation - continued



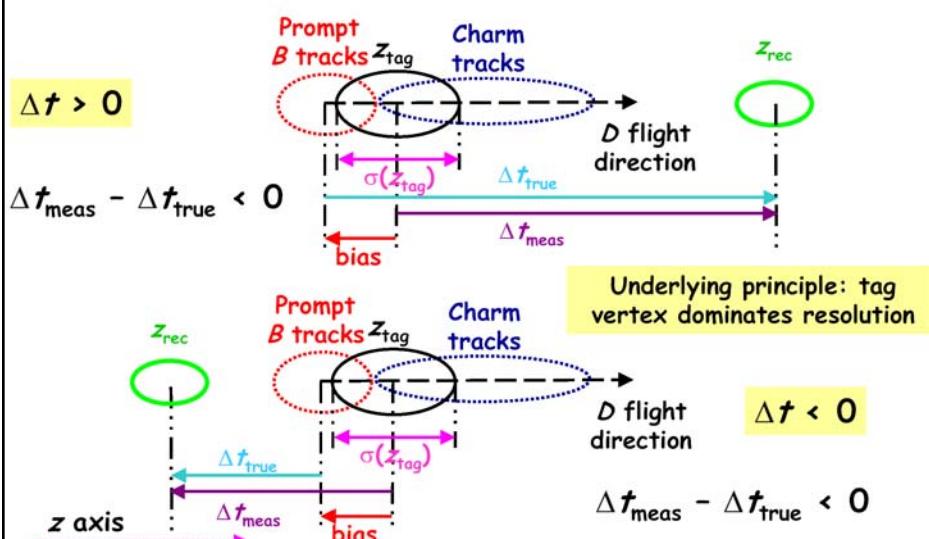
Determine  $\Delta t$  from  $\Delta z = \beta\gamma c\Delta t$ :

- ♦ clock start: resolution on tag side  $140\ \mu m$  ( $\epsilon = 91\%$ ) - charm decays
- ♦ clock stop: resolution on CP side  $75\ \mu m$  ( $\epsilon = 92\%$ )

N.B. typically  $\Delta z = \beta\gamma c\tau_B = 200\ \mu m$



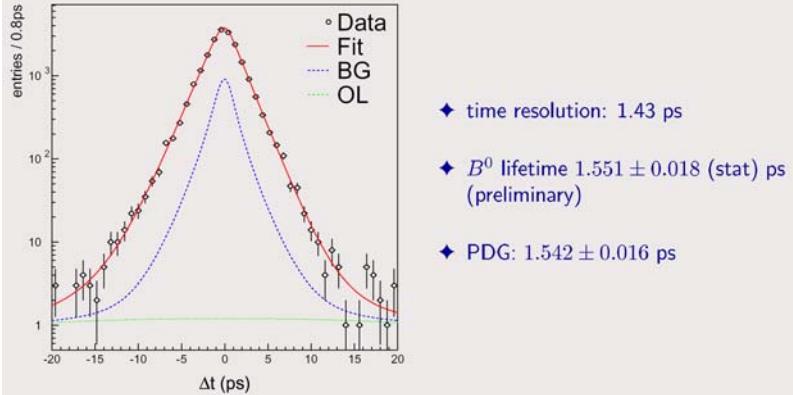
## Effect of charm decays on time resolution





## Vertexing - check with lifetime measurement

Use  $B^0 \rightarrow D^- \pi^+$ ,  $D^{*-} \pi^+$ ,  $D^{(*)-} \rho^+$ ,  $B^0 \rightarrow J/\psi K_S$  and  $B^0 \rightarrow J/\psi K^{*0}$  decays



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## Flavour tagging 1

Identify  $B^0/\bar{B}^0$  by the charges of the decay products of the associated  $B$

### Inclusive leptons

- ◆ high momentum  $\ell^-$
- ◆ intermediate momentum  $\ell^+$

$$b \rightarrow c \ell^- \nu$$
$$c \rightarrow s \ell^+ \nu$$

### Inclusive hadrons

- ◆ high momentum  $\pi^+$
- ◆ intermediate momentum  $K^+$
- ◆ low momentum  $\pi^-$

$$B^0 \rightarrow D^{(*)-} \pi^+, D^{(*)-} \rho^+ (\rho^+ \rightarrow \pi^+ \pi^0), \dots$$
$$\rightarrow K^+ X$$
$$D^{(*)-} \rightarrow \bar{D}^0 \pi^-$$

Efficiency > 99.5%,  $\epsilon_{\text{effective}} = 28.8 \pm 0.5\%$

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## Flavour tagging 2

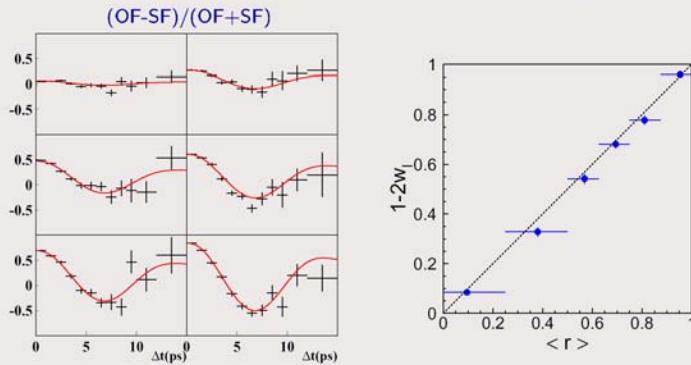
Tagging is not perfect: there is always a chance  $w$  that the tag is fake (less for leptons more for kaons).

→ The asymmetry oscillation is reduced,  $\sin \Delta m_d t \rightarrow (1 - 2w) \sin \Delta m_d t$ .

→ Needed:  $w$  for each event.

Classify events into six categories in a tag quality variable  $r$ .

Calibrate the relation  $(1 - 2w)$  vs.  $r$  with data: measure the  $B^0 \bar{B}^0$  mixing amplitude (using  $\bar{B}^0 \rightarrow D^{*+} \ell^- \nu$ ,  $D^{(*)+} \pi^-$  and  $D^{(*)+} \rho^-$  decays) in 6 intervals in  $r$



## Flavour tagging 3

Relation  $r$  vs.  $(1-2w)$  calibrated with mixing data, ratio of oppositely flavoured (OF) to the same flavoured (SF)  $B$  pairs

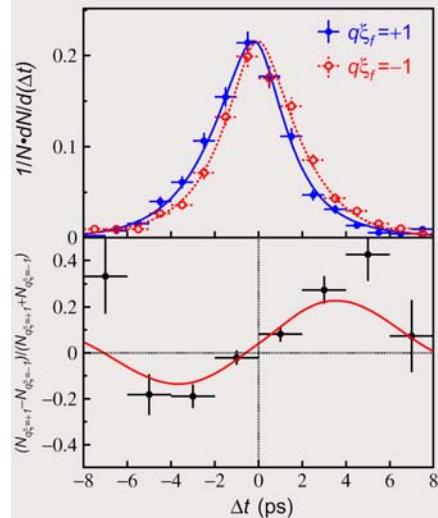
$$\frac{OF(t) - SF(t)}{OF(t) + SF(t)} = (1 - 2w) \cos(\Delta mt)$$

Table: tagging efficiency, wrong tag probability and effective tagging efficiency  $\epsilon(1-2w)^2$  for six intervals in the tagging variable  $r$ .

$l$	$r$ interval	$\epsilon_l$	$w_l$	$\epsilon_{\text{eff}}^l$
1	0.000 – 0.250	0.398	$0.458 \pm 0.006$	$0.003 \pm 0.001$
2	0.250 – 0.500	0.146	$0.336 \pm 0.009$	$0.016 \pm 0.002$
3	0.500 – 0.625	0.104	$0.228 \pm 0.010$	$0.031 \pm 0.002$
4	0.625 – 0.750	0.122	$0.160^{+0.009}_{-0.008}$	$0.056 \pm 0.003$
5	0.750 – 0.875	0.094	$0.112 \pm 0.009$	$0.056 \pm 0.003$
6	0.875 – 1.000	0.136	$0.020 \pm 0.006$	$0.126^{+0.003}_{-0.004}$



## Final result



CP is violated! Red points differ from blue.

Red points: anti- $B^0 \rightarrow f_{CP}$  with  $CP=-1$  (or  $B^0 \rightarrow f_{CP}$  with  $CP=+1$ )

Blue points:  $B^0 \rightarrow f_{CP}$  with  $CP=-1$  (or anti- $B^0 \rightarrow f_{CP}$  with  $CP=+1$ )

Belle, 2002 statistics  
(78/fb, 85M B B pairs)

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## Fitting the asymmetry

**Fitting function:**

$$P_{sig}(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} \left\{ 1 + q(1 - 2w_l) \text{Im } \lambda \sin \Delta mt \right\} \otimes R(t)$$

Miss-tagging probability

$q=+1$  or  $=-1$  ( $B$  or anti- $B$  on the tag side)

Resolution function:  
from self-tagged events  
 $B \rightarrow D^* l\nu, D\pi, \dots$

**Fitting: unbinned maximum likelihood fit event-by-event**

**Fitted parameter:  $\text{Im}(\lambda)$**

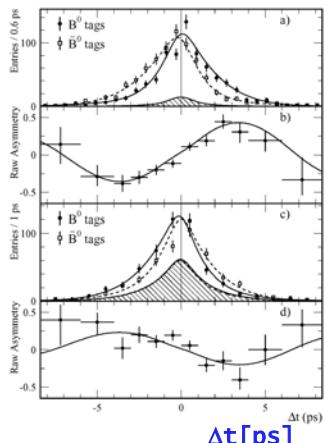
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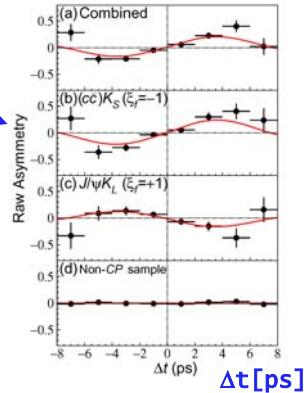
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## BaBar vs Belle $\sin 2\phi_1$



asymmetry



$$\begin{aligned} \sin 2\phi_1 &= 0.741 \pm 0.067 \pm 0.034 \quad (\text{BaBar}) \\ \sin 2\phi_1 &= 0.719 \pm 0.074 \pm 0.035 \quad (\text{Belle}) \end{aligned}$$

2002 statistics

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## $b \rightarrow c \bar{c}$ anti- $c$ s $CP=+1$ and $CP=-1$ eigenstates

$$a_{f_{CP}} = -\text{Im}(\lambda_{f_{CP}}) \sin(\Delta mt)$$

Asymmetry sign depends on the CP parity of the final state  $f_{CP}$ ,  $\eta_{f_{CP}} = +1$

$$\lambda_{f_{CP}} = \eta_{f_{CP}} \frac{q}{p} \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

$J/\psi K_S (\pi^+ \pi^-)$ :  $CP=-1$

•  $J/\psi$ :  $P=-1$ ,  $C=-1$  (vector particle  $J^{PC}=1^-$ ):  $CP=+1$

•  $K_S (->\pi^+ \pi^-)$ :  $CP=+1$ , orbital ang. momentum of pions = 0  $\rightarrow P(\pi^+ \pi^-) = (\pi^- \pi^+)$ ,  $C(\pi^- \pi^+) = (\pi^+ \pi^-)$

• orbital ang. momentum between  $J/\psi$  and  $K_S$   $|l|=1$ ,  $P=(-1)^l = -1$

$J/\psi K_L (3\pi)$ :  $CP=+1$

Opposite parity to  $J/\psi K_S (\pi^+ \pi^-)$ , because  $K_L (3\pi)$  has  $CP=-1$

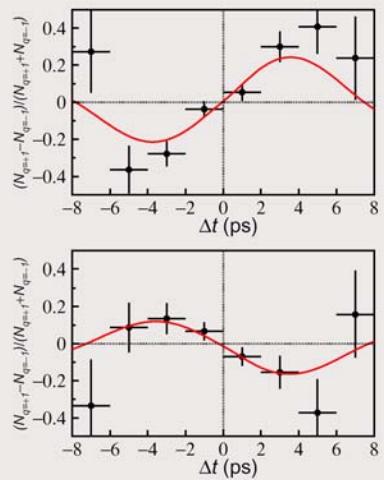
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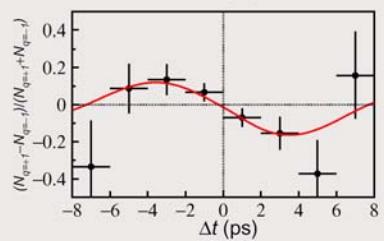


## Comparison between CP=+1 and CP=-1



$CP = -1$  sample

$$\sin 2\phi_1 = 0.716 \pm 0.083$$



$CP = +1$  sample

$$\sin 2\phi_1 = 0.78 \pm 0.17$$

N.B. Plotted: raw asymmetry. The amplitude of  $\pm \sin 2\phi_1 \sin \Delta m_d \Delta t$  is reduced due to wrong tagging by a factor  $(1 - 2w)$ .

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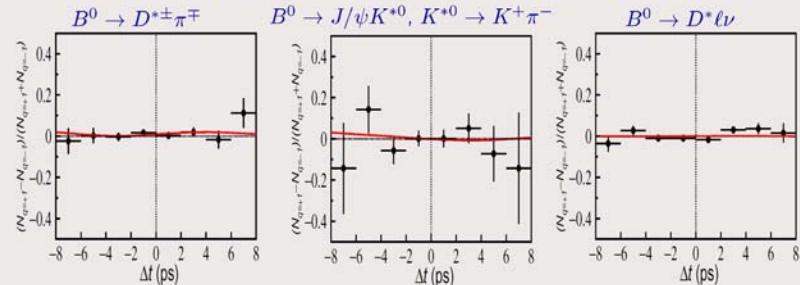
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## Checks, systematic errors

Same analysis for flavour specific final states, where there should be no asymmetry



$$"sin 2\phi_1" = 0.035 \pm 0.032$$

$$"sin 2\phi_1" = -0.021 \pm 0.093$$

$$"sin 2\phi_1" = 0.004 \pm 0.017$$

Systematic errors:

vertexing	0.022	resolution function	0.014
possible bias in $\sin 2\phi_1$ fit	0.011	$J/\psi K_L$ background fraction	0.010
$\Delta m_d$	< 0.010	$\tau_B$	< 0.010

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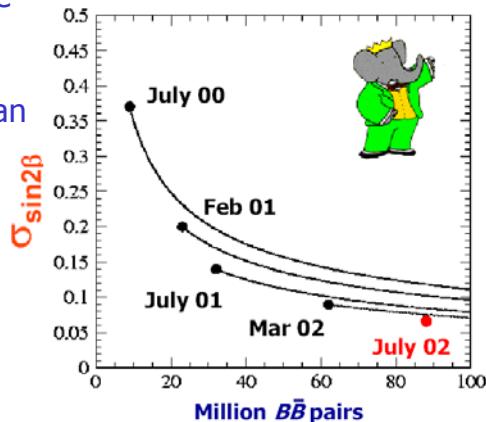


## More data....

Larger sample ->

- smaller statistical error ( $1/\sqrt{N}$ )
- better understanding of the detector, calibration etc

-> error improves better than with  $1/\sqrt{N}$



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## Fit with free $|\lambda|$

time distribution:

$$P_{sig}(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} \left\{ 1 + q(1 - 2w_i) \left[ \frac{2 \operatorname{Im} \lambda}{|\lambda|^2 + 1} \sin \Delta m \Delta t + \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1} \cos \Delta m \Delta t \right] \right\}$$

fit with  
 $\operatorname{Im}\lambda/|\lambda|$  and  $|\lambda|$  as free parameters

direct CP  
 $|\lambda| \neq 1$

$$|\lambda| = 0.950 \pm 0.049 \pm 0.025 \quad (\text{Belle, PRD66, 071102(02)})$$

$$\sin 2\phi_1 = 0.719 \pm 0.074 \pm 0.035$$

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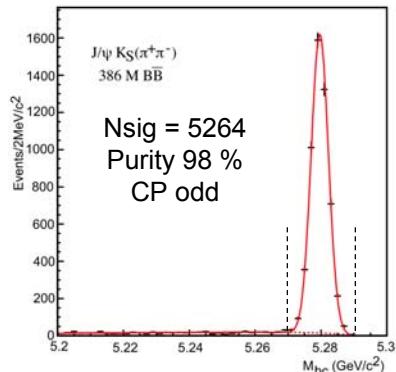
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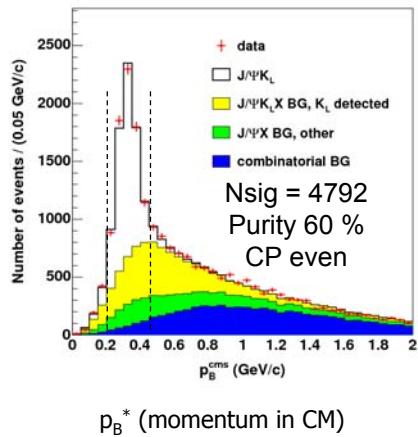


## 2005: $B^0 \rightarrow J/\psi K^0$ with 386 M $B\bar{B}$ pairs

$B^0 \rightarrow J/\psi K_S^0$



$B^0 \rightarrow J/\psi K_L^0$



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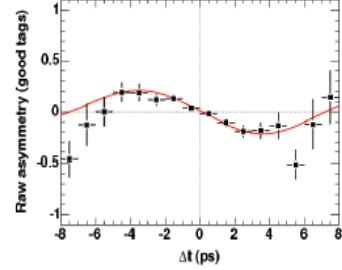
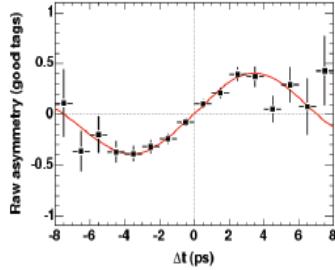
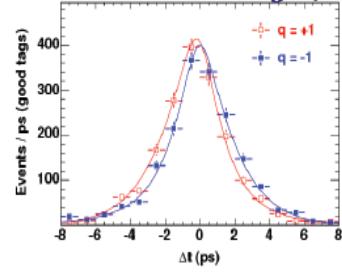
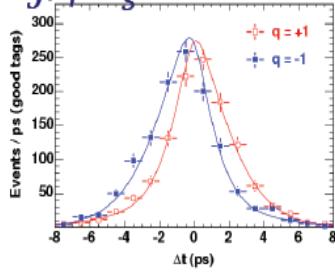
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$J/\psi K_S$  *Belle* ( $386 \times 10^6 B\bar{B}$ )

$J/\psi K_L$



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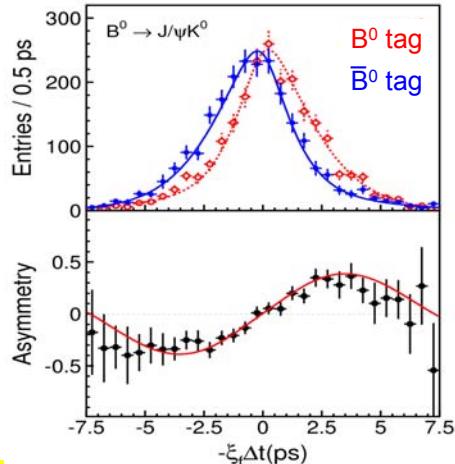


2005:  $B^0 \rightarrow J/\psi K^0$

No  
DCPV

$$\sin 2\phi_1 = 0.652 \pm 0.039 \text{ (stat)} \pm 0.020 \text{ (syst)}$$

$$A = 0.010 \pm 0.026 \text{ (stat)} \pm 0.036 \text{ (syst)}$$



BG subtracted distributions  
(good tag region)

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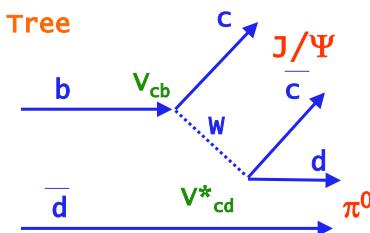
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$\sin 2\phi_1(\beta)$  from other processes

$\sin 2\phi_1$  is the CP asymmetry parameter in

- $b \rightarrow ccd$  (tree+penguin)
- $b \rightarrow sss$  (penguin only)



$$\lambda_{\psi\pi^0} = \eta_{\psi\pi^0} \left( \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \right) \left( \frac{V_{cd}^* V_{cb}}{V_{cd} V_{cb}^*} \right)$$

$$\text{Im}(\lambda_{\psi\pi^0}) = \sin 2\phi_1 = \sin 2\beta$$

$$A(c\bar{c}d) = V_{tb} V_{td}^* (P_d^t - P_d^u) + V_{cb} V_{cd}^* (T_{c\bar{c}d} + P_d^c - P_d^u)$$

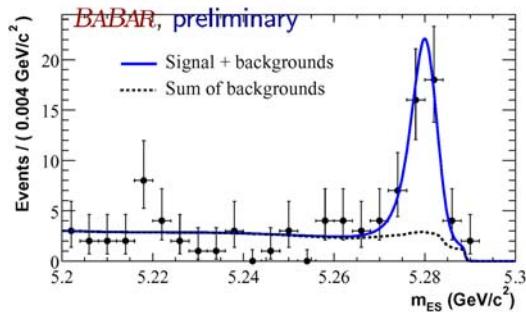
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## $\sin 2\phi_1(\beta)$ from $b \rightarrow ccd$



$B \rightarrow J/\Psi \pi^0$

(BaBar,  
hep-ex/0207058(02);  
Belle,  
hep-ex/0207058(02))

Tree and penguin contrib.  $O(\lambda^3)$ ;  
remove  $|\lambda_{fCP}|=1$  assumption in fit:

$$a_{fCP} = -\frac{2 \operatorname{Im}(\lambda_{fCP})}{1 + |\lambda_{fCP}|^2} \sin(\Delta mt) + \frac{|\lambda_{fCP}|^2 - 1}{|\lambda_{fCP}|^2 + 1} \cos(\Delta mt)$$

$S_f$

$\mathcal{A}_f$

in leading order  
 $S_f = -\eta_f \sin 2\phi_1$   $\mathcal{A}_f = 0$

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## $\sin 2\phi_1(\beta)$ from $b \rightarrow ccd$

$$a_{fCP} = -\frac{2 \operatorname{Im}(\lambda_{fCP})}{1 + |\lambda_{fCP}|^2} \sin(\Delta mt) + \frac{|\lambda_{fCP}|^2 - 1}{|\lambda_{fCP}|^2 + 1} \cos(\Delta mt)$$

$S_f$

$\mathcal{A}_f$

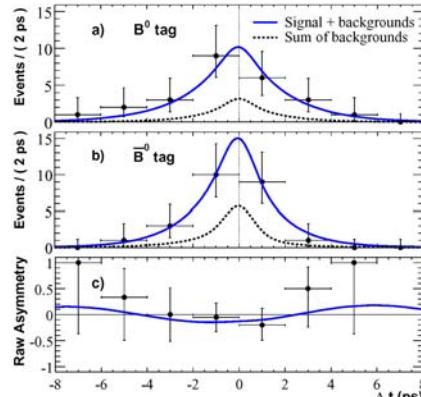
Prediction: in leading order  
 $S_f = -\eta_f \sin 2\phi_1$   $\mathcal{A}_f = 0$

$S_f = 0.05 \pm 0.49 \pm 0.16$  (BaBar)

$\mathcal{A}_f = -0.38 \pm 0.41 \pm 0.09$

$S_f = -0.93 \pm 0.49 \pm 0.11$  (Belle)

$\mathcal{A}_f = -0.25 \pm 0.39 \pm 0.06$



consistent with  $\sin 2\phi_1$  and 0!

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## Backup slides

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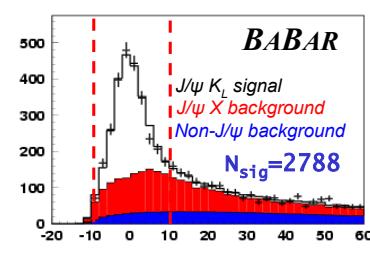
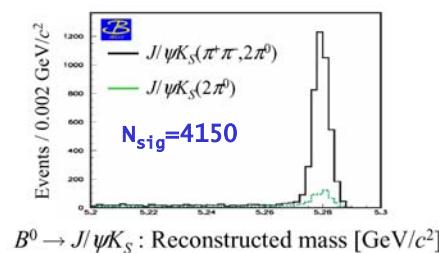
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## $\sin 2\phi_1$ – status 2004

$B \rightarrow J/\psi K_S$

$B \rightarrow J/\psi K_L$



Considerable increase in statistics.

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